## SOCIETY OF ACTUARIES

## AMERICAN SOCIETY OF PENSION ACTUARIES

 JOINT BOARD FOR THE ENROLLEMENT OF ACTUARIES
## MAY 2000 COURSE EA-1, SEGMENT B JOINT BOARD EXAMINATION


#### Abstract

This is the May 2000 examination which has been released to the public by the administering organizations.


## INSTRUCTIONS TO CANDIDATES

1. Write your candidate number here $\qquad$ . Your name must not appear.
2. Do not break the seal of this book until the supervisor tells you to do so.
3. Special conditions generally applicable to all questions on this examination are found at the front of this book.
4. On this examination the symbol " a " will be used to represent an annuity.
5. This examination consists of 20 multiple-choice questions.
6. Each question has equal weight. Your score will be based on the number of questions which you answer correctly. No credit will be given for omitted answers and no credit will be lost for wrong answers; hence, you should answer all questions even those for which you have to guess.
7. A separate answer sheet is inside the front cover of this book. During the time allotted for this examination, record all your answers on side 2 of the answer sheet. NO ADDITIONAL TIME WILL BE ALLOWED FOR THIS PURPOSE. No credit will be given for anything indicated in the examination book but not transferred to the answer sheet. Failure to stop writing or coding your answer sheet after time is called will result in the disqualification of your answer sheet or further disciplinary action.
8. Five answer choices are given with each question, each answer choice being identified by a key letter (A to E). Answer choices for some questions have been rounded. For each question, blacken the oval on the answer sheet which corresponds to the key letter of the answer choice that you select.
9. Use a soft-lead pencil to mark the answer sheet. To facilitate correct mechanical scoring, be sure that, for each question, your pencil mark is dark and completely tills only the intended oval. Make no stray marks on the answer sheet. If you have to erase, do so completely.
10. Do not spend too much time on any one question. If a question seems too difficult, leave it and go on.
11. While every attempt is made to avoid defective questions, sometimes they do occur. If you believe a question is defective, the supervisor or proctor cannot give you any guidance beyond the instructions on the exam booklet.
12. Clearly indicated answer choices in the test book can be an aid in grading examinations in the unlikely event of a lost answer sheet.
13. Use the blank portions of each page for your scratch work. Extra blank pages are provided at the back of the examination book.
14. When the supervisor tells you to do so, break the seal on the book and remove the answer sheet.

On side 1 of the answer sheet, space is provided to write and to code candidate information. Complete Blocks A through G as follows:
(a) in Block A, print your name and the name of this test center;
(b) in Block B, print your last name, first name and middle initial and code your name by blackening the ovals (one in each column) corresponding to the letters of your name; for each empty box, blacken the small rectangle immediately above the "A" oval;
(C) write your candidate number in Block C (as it appears on your ticket of admission for this examination) and write the number of this test center in Block D (the supervisor will supply the number);
(d) code your candidate number and center number by blackening the five ovals (one in each column) corresponding to the five digits of your candidate number and the three ovals (one in each column) corresponding to the three digits of the test center number, respectively. Please be sure that your candidate number and the test center number are coded correctly;
(e) in Block E, code the examination that you are taking by blackening the oval to the left of "Exam P360U (EA1 Segment B);"
(f) in Block F, blacken the appropriate oval to indicate whether you are using a calculator; and
(g) in Block G, sign your name and write today's date. If the answer sheet is not signed, it will not be graded.

On side 2 of your answer sheet, space is provided at the top for the number of this examination book. Enter the examination book number, from the upper right-hand comer of this examination book, in the four boxes at the top of side 2 marked "BOOKLET NUMBER."
15. After the examination, the supervisor will collect this book and the answer sheet separately. DO NOT ENCLOSE THE ANSWER SHEET IN THE BOOK. All books and answer sheets must be returned. THE QUESTIONS ARE CONFIDENTIAL AND MAY NOT BE TAKEN FROM THE EXAMINATION ROOM.

## Conditions Generally Applicable to All EA-1 Segment B Examnination Questions

The following conditions should be considered a part of the data for each question, unless otherwise stated or implied.

## General Conditions Regarding Plan Provisions

(1) "Plan" or "pension plan" means a defined benefit pension plan.
(2) The plan is sponsored by a single employer.
(3) The normal retirement age is 65 .
(4) Retirement pensions commence at normal retirement age and are paid monthly for life at the beginning of each month.
(5) There are no preretirement death or disability benefits.
(6) The plan covers all active employees of the employer; there is no age or service requirement for participation. Thus, when referring to active employees, the terms "employee" and "participant" are synonymous.
(7) There are no mandatory or voluntary employee contributions.
(8) Service for purposes of vesting and benefit accrual is credited on the basis of time elapsed since date of hire.
(9) When the normal retirement benefit is computed as a dollar amount, or as a percentage of compensation, for each year of service, the accrued benefit is defined likewise.
(10) Actuarial equivalence is based on the mortality table and interest rate assumed for funding purposes.
(11) The plan has not been amended since its effective date.

## General Conditions Regarding Funding

(12) Any actuarial valuation encompasses not only all active employees but also retired employees, beneficiaries, and former employees entitled to vested deferred pensions.
(13) The valuation date is the first day of the plan year; i.e., participant data, present values, asset values, etc. are as of that date. Also, normal costs are payable annually, the first being due on the valuation date.
(14) Where the normal cost under an actuarial cost method may be computed as either a level percentage of compensation or a level dollar amount, the level percentage approach is used if the plan benefits are based on compensation, and the level dollar approach is used if they are not.
(15) Under the frozen initial liability method, whenever there is a change in the plan, actuarial assumptions, or asset valuation method, the unfunded liability is adjusted by adding to it the increase (positive or negative) in the unfunded entry age normal accrued liability due to the change. Likewise, under the attained age normal method, the unfunded liability is adjusted by adding to it the increase in the unfunded unit credit accrued liability.
(16) The actuarial cost method and actuarial assumptions have not been changed since the plan effective date.
(17) Expenses are paid directly by the employer, rather than from the assets of the plan, and therefore do not affect the funding of the plan.
(18) Assumed compensation increases first apply to the year immediately following the latest year for which valuation compensation is shown.

The preceding conditions should be considered a part of the data for each question, unless otherwise stated or implied.

## Data for Ouestion 1

Actuarial valuation date: 1/1/2000.

## Normal retirement benefit: $2 \%$ of final average compensation for each year of service.

$$
\begin{array}{ll}
\text { Final average compensation: } \quad \begin{array}{l}
\text { The average of the three calendar year salaries preceding the } \\
\text { date of retirement. }
\end{array}
\end{array}
$$

Actuarial cost method: Projected unit credit.
Actuarial assumptions:

| Preretirement interest: | $8 \%$ per year |
| :--- | :--- |
| Annual salary increases: | $6 \%$ per year |
| Preretirement decrements: | None |
| Retirement age: | 65 |

Selected annuity value:
$\ddot{a}_{65}^{(12)}=8.33$

Data for sole participant:
Date of birth:
1/1/1940
Date of hire: $\quad 1 / 1 / 1980$
Salary during 1999 calendar year: $\quad \$ 35,000$

## Ouestion 1

In what range is the normal cost as of $1 / 1 / 2000$ ?
(A) Less than $\$ 4,800$
(B) $\$ 4,800$ but less than $\$ 5,000$
(C) $\$ 5,000$ but less than $\$ 5,200$
(D) $\$ 5,200$ but less than $\$ 5,400$
(E) $\$ 5,400$ or more

Actuarial valuation date: 1/1/2000.

Actuarial cost method: Entry age normal.
Actuarial assumptions:

| Preretirement decrements: | Mortality only |
| :--- | :--- |
| Retirement age: | 58 |
| Salary scale: | $4 \%$ per year |

Selected commutation functions:
$\mathrm{D}_{55}=16,393$
$\mathrm{D}_{56}=15,709$
$D_{57}=15,035$

Data for participant Smith:
Date of birth:
1/1/1945
Date of hire: 12/31/1999

Let $\mathrm{X}=$ Smith's normal cost as of $1 / 1 / 2000$ if the normal cost is calculated as a level percentage of salary.

Let $\mathrm{Y}=$ Smith's normal cost as of $1 / 1 / 2000$ if the normal cost is calculated as a level dollar amount.

## Question 2

In what range is $\mathrm{X} \div \mathrm{Y}$ ?
(A) Less than 0.9620
(B) 0.9620 but less than 0.9810
(C) 0.9810 but less than 1.0000
(D) $1 . \mathrm{OOOO}$ but less than 1.0190
(E) 1.0190 or more

Actuarial valuation date: 1/1/2000.

Actuarial cost method: Unit credit.

Normal retirement benefit: $\$ 20$ per month per year of service.
Early retirement benefit: Accrued benefit, unreduced for commencement on or after age 60 .
Actuarial assumptions:
Preretirement decrements: None
Annual effective rate of interest: $7 \%$
Retirement age prior to $1 / 1 / 2000$ : 61
On 1/1/2000 the retirement age assumption is changed to the following:

| Age at retirement | Probabilitv of retirement |
| :---: | :---: |
| 61 | 0.4 |
| 62 | 0.6 |
| 63 | 1.0 |

Retirements occur at the beginning of the year.

Selected annuity values:

$$
\begin{aligned}
& \ddot{\mathrm{a}}_{61}^{(12)}=8.333 \\
& \ddot{\mathrm{a}}_{62}^{(12)}=8.167 \\
& \ddot{\mathrm{a}}_{63}^{(12)}=8.000
\end{aligned}
$$

Data for sole participant Smith:
Date of birth: $\quad 1 / 1 / 1960$
Date of hire: $\quad 1 / 1 / 1990$
Question 3
In what range is the absolute value of the change in the actuarial accrued liability as of $1 / 1 / 2000$ due to the change in the retirement age assumption?
(A) Less than $\$ 295$
(B) $\$ 295$ but less than $\$ 310$
(C) $\$ 310$ but less than $\$ 325$
(D) $\$ 325$ but less than $\$ 340$
(E) $\$ 340$ or more

## Data for Question 4

Actuarial valuation date: $1 / 1 / 2000$
Retirement benefit:
$\$ 4,800$ per year, payable at beginning of each year in the form of a 3-year certain and life annuity.

Actuarial assumptions:
Interest rate: 7\% per year
Selected commutation functions:
$\mathrm{N}_{63}=35,623$
$\mathrm{N}_{64}=31,010$
$\mathrm{N}_{65}=26,867$
Data for pensioner Smith:
Date of birth: $\quad 1 / 1 / 1936$
Date of retirement: $\quad 1 / 1 / 1997$
Status as of $1 / 1 / 2000$ : Alive

## ©uestion 4

In what range is the 1999 experience loss as of $1 / 1 / 2000$ due to Smith's survival?
(A) Less than $\$ 1,300$
(B) $\$ 1,300$ but less than $\$ 2,600$
(C) $\$ 2,600$ but less than $\$ 3,900$
(D) $\$ 3,900$ but less than $\$ 5,200$
(E) $\$ 5,200$ or more

## Data for Ouestion 5

Normal retirement benefit: $\$ 20$ per month per year of service.
Early retirement benefit: Accrued benefit reduced by 5\% for each year that retirement precedes age 65.

Normal form of benefit: Life annuity.
Actuarial cost method: Unit credit.

Selected commutation functions:

| Age x | $\mathrm{D}_{\mathrm{X}}$ |  |
| :---: | :---: | :---: |
|  |  | $\mathrm{N}_{\mathrm{X}}-$ |
| 40 |  | 652 |
| 50 | 322 | 8761 |
| 60 |  | 3902 |
| 65 | 99 | 1547 |
|  |  | 904 |

The assumed retirement age is 65 .
Data for participant Green:
Date of birth: $\quad 1 / 1 / 1940$
Date of hire: $\quad 1 / 1 / 1980$
Date of retirement: $\quad 1 / 1 / 2000$

## Question 5

As of $1 / 1 / 2000$, in what range is the change in the accrued liability due to Green's retirement?
(A) Loss of $\$ 6,000$ or more
(B) Loss of more than $\$ 0$, but less than $\$ 6,000$
(C) No gain or loss or a gain less than $\$ 6,000$
(D) Gain of at least $\$ 6,000$ but less than $\$ 12,000$
(E) Gain of $\$ 12,000$ or more

## Data for Question 6

Actuarial valuation date: 1/1/2000.
Actuarial cost method: Unit credit.

Normal retirement benefit: $\$ 25$ per month per year of service.
Actuarial assumptions:
Interest rate:
Valuations before 1/1/2000: 7\%
Valuations after 12/3 1/1 999: 8\%
Preretirement decrements: None
Retirement age: 65
Actual return on assets during 1999: 10\%.
Unfunded accrued liability as of $1 / 1 / 1999$ prior to the 1999 contribution: $\$ 12,000$.
Selected annuity values:

| $\ddot{a}_{65}^{(12)}$ | $\frac{7 \%}{9.70}$ | $\underline{8 \%}$ |
| :--- | :--- | :--- |
| 8.74 |  |  |

Data for sole participant:
Date of birth: $1 / 1 / 1940$
Date of hire: 1/1/1978
The contribution for 1999 was equal to the $1 / 1 / 1999$ normal cost and was contributed on 1/1/1999.

## Question 6

In what range is the unfunded accrued liability as of $1 / 1 / 2000$ ?
(A) Less than $\$ 3,000$
(B) $\$ 3,000$ but less than $\$ 5,000$
(C) $\$ 5,000$ but less than $\$ 7,000$
(D) $\$ 7,000$ but less than $\$ 9,000$
(E) $\$ 9,000$ or more

Actuarial valuation date: 1/1/2000.

Plan effective date: 1/1/1998.
Normal retirement benefit: $\$ 30$ per month per year of service.
Actuarial cost method: Unit credit.
Actuarial assumptions:
Interest rate:
$8 \%$ per year
Preretirement decrements: None
Retirement age: 65

Selected valuation results as of $1 / 1 / 1998$ :
Accrued liability: $\quad \$ 50,000$
Normal cost: $\quad 4,000$
A contribution of $\$ 6,000$ for the 1998 plan year was made on $7 / 1 / 1998$.
A contribution of $\$ 6,200$ for the 1999 plan year was made on $1 / 1 / 1999$.
Since $1 / 1 / 1998$ there have been no retirements and all plan participants are under age 62 as of 1/1/1998.

There have been no new entrants since the 1998 valuation.
The actuarial assumptions have always been exactly realized except that the 1999 investment return was $9.5 \%$.

## Ouestion 7

In what range is the $1 / 1 / 2000$ unfunded liability?
(A) Less than $\$ 48,000$
(B) $\$ 48,000$ but less than $\$ 50,000$
(C) $\$ 50,000$ but less than $\$ 52,000$
(D) $\$ 52,000$ but less than $\$ 54,000$
(E) $\$ 54,000$ or more

Normal retirement benefit: $\$ 50,000$.
Normal form of benefit: Single life annuity, if not married. Unreduced joint and $100 \%$ survivor annuity, if married.

Actuarial cost method: Entry age normal.
Actuarial Assumptions:

Interest rate:
Preretirement decrements:
Postretirement mortality:
Retirement age:
Marital status at retirement:

7\% per year
None
Unisex
65
Same as marital status on valuation date

Selected data for the sole participant:

## Date of birth:

1/1/1936
Date of hire:
1/1/1976
Date of participation: $\quad 1 / 1 / 1976$
On July 1, 1999, the participant got married. Prior to this the participant had never been married.
Selected data for spouse of sole participant:
Date of birth: $\quad 1 / 1 / 1936$
Selected annuity values:

$$
\begin{aligned}
& \ddot{a}_{65}^{(12)}=8.74 \\
& \ddot{a}_{65: 65}^{(12)}=6.90
\end{aligned}
$$

## Buestion 8

In what range is the increase in the normal cost as of $1 / 1 / 2000$ due to the change in marital status?
(A) Less than $\$ 1,500$
(B) $\$ 1,500$ but less than $\$ 3,500$
(C) $\$ 3,500$ but less than $\$ 5,500$
(D) $\$ 5,500$ but less than $\$ 7,500$
(E) $\$ 7,500$ or more

Normal retirement benefit: $\quad 50 \%$ times the average of final 3 calendar years' compensation, less the amount of an annuity from a prior plan.

Plan effective date: 1/1/1999.
Actuarial valuation date: 1/1/2000.
Actuarial cost method: Individual aggregate (level dollar).
Actuarial assumptions:

| Interest rate: | $7 \%$ per year |
| :--- | :--- |
| Compensation increases: | $3.5 \%$ per year |
| Preretirement decrements: | None |
| Retirement age: | 65 |

Valuation data for sole participant:
Date of birth: $\quad 1 / 1 / 1950$
Date of hire: $\quad 1 / 1 / 1995$
1999 compensation: $\$ 50,000$
Paid-up annuity (payable at age 65): $\$ 1,250$ month (from prior plan)
Actuarial value of assets as of $1 / 1 / 2000: \$ 7,500$
Selected annuity value:

$$
\ddot{a}_{65}^{(12)}=8.736
$$

## Question 9

In what range is the normal cost as of $1 / 1 / 2000$ ?
(A) Less than $\$ 6,600$
(B) $\$ 6,600$ but less than $\$ 7,400$
(C) $\$ 7,400$ but less than $\$ 8,200$
(D) $\$ 8,200$ but less than $\$ 9,000$
(E) $\$ 9,000$ or more

## Data for Ouestion 10

Actuarial valuation date: 1/1/2000.
Normal retirement benefit: $\$ 25$ per month per year of service.
Actuarial cost method: Entry age normal.
Actuarial assumptions:

| Interest rate: | $7 \%$ per year |
| :--- | :--- |
| Preretirement decrements other than death: | None |
| Retirement age: | 65 |

Selected valuation data:
Assets as of 1/1/1999:
\$ 3,000
Employer contribution on 12/31/1999: \$ 934
Assets as of 1/1/2000:
\$4,234
Valuation data for sole participant:
Date of birth:
1/1/1959
Date of hire:
1/1/1994
Status on 1/1/2000:
Active
Selected commutation functions:

| Age x | Dx | $\mathrm{N}_{\mathrm{x}}$ |
| :---: | :---: | :---: |
| 35 | 894,190 | 12,364,661 |
| 40 | 632,275 | 8,452,737 |
| 41 | 589,655 | 7,820,462 |
| 65 | 94,414 | 868,053 |

Selected annuity value:

$$
\ddot{a}_{65}^{(12)}=8.736
$$

## Ouestion 10

In what range is the absolute value of the experience gain or loss for 1999 measured as of the valuation date?
(A) Less than $\$ 65$
(B) $\$ 65$ but less than $\$ 75$
(C) $\$ 75$ but less than $\$ 85$
(D) $\$ 85$ but less than $\$ 95$
(E) $\$ 95$ or more

## Data for Ouestion 11

Normal retirement benefit: $\begin{aligned} & \text { Before 2000: } 50 \% \text { of final 3-year average compensation. } \\ & \text { After 1999: } 60 \% \text { of final year's compensation. }\end{aligned}$

Actuarial cost method: Entry age normal (level percentage of compensation).
Actuarial assumptions:

| Interest rate: | $7.0 \%$ per year |
| :--- | :--- |
| Salary scale: | $5.0 \%$ per year |
| Preretirement decrements: | None |
| Retirement age: | 65 |

Valuation data for sole participant Smith as of January 1, 2000:
Date of birth:
1/1/1945
Date of hire:
1/1/1995

Normal cost for Smith as of January 1, 1995: \$10,000
There have been no gains or losses since 1995.

## Question 11

In what range is the increase in accrued liability for Smith as of January 1, 2000 due to the plan amendment?
(A) Less than $\$ 15,000$
(B) $\$ 15,000$ but less than $\$ 17,000$
(C) $\$ 17,000$ but less than $\$ 19,000$
(D) $\$ 19,000$ but less than $\$ 21,000$
(E) $\$ 21,000$ or more

## Data for Ouestion 12

Plan effective date: 1/1/2000.
Normal retirement benefit: $60 \%$ of final year's salary.
Actuarial cost method: Aggregate.
Valuation assumptions:

| Interest: | $7 \%$ per year |
| :--- | :--- |
| Salary increases: | $\mathbf{5 \%}$ per year |
| Preretirement decrements: | None |
| Retirement age: | 65 |

Data for sole participant:
Date of birth $\quad 1 / 1 / 1955$

Annual salary in 1999: $\quad \$ 50,000$
The normal cost determined as of $1 / 1 / 2000$ was contributed on $1 / 1 / 2000$.
Plan experience for 2000:
Investment return: 10\%
Salary increase: 7\%
Selected annuity value:

$$
\ddot{\mathrm{a}}_{65}^{(12)}=8.736
$$

## Ouestion 12

In what range is the normal cost for 2001 as of January 1, 2001?
(A) Less than $\$ 10,750$
(B) $\$ 10,750$ but less than $\$ 10,980$
(C) $\$ 10,980$ but less than $\$ 11,210$
(D) $\$ 11,210$ but less than $\$ 11,440$
(E) $\$ 11,440$ or more

## Data for Ouestion 13

Normal retirement benefit:
Before 1/1/2000: $\quad \$ 20$ per month for each year of service.
After 12/31/1999: $\quad \$ 25$ per month for each year of service.
Early retirement benefit: accrued benefit without reduction.
Actuarial cost method:
Before 1/1/2000: Unit credit.
After 12/31/1999: Entry age normal.
Actuarial assumptions:
Interest rate: $\quad 7 \%$ per year
Preretirement decrements: None
Retirement age: 62
Valuation data for sole participant (active as of $1 / 1 / 2000$ ):
Date of birth: $\quad 1 / 1 / 1945$
Date of hire: $\quad 1 / 1 / 1980$
Selected valuation results as of $1 / 1 / 1999$ :
Accrued liability: $\quad \$ 24,910$

## Ouestion 13

In what range is the increase in the $1 / 1 / 2000$ entry age normal accrued liability due to the plan amendment?
(A) Less than $\$ 7,000$
(B) $\$ 7,000$ but less than $\$ 7,500$
(C) $\$ 7,500$ but less than $\$ 8,000$
(D) $\$ 8,000$ but less than $\$ 8,500$
(E) $\$ 8,500$ or more

Normal retirement benefit: $\$ 20$ per month for each year of service.
Normal form of benefit: Life annuity.
Normal retirement age: 65.
Early retirement benefit: Accrued benefit, reduced by $0.5 \%$ for each month by which the benefit commencement date precedes the normal retirement date.

Actuarial cost method: Unit credit.

Actuarial assumptions:
Interest rate: $\quad 7 \%$ per year
Preretirement decrements:
None
Probability of retirement (retirements are assumed to occur at beginning of year):

| Age | Probability |
| :---: | :---: |
| 60 | $50 \%$ |
| 62 | $75 \%$ |
| 65 | $100 \%$ |

Selected annuity values based on post-retirement assumptions:

| Age x | $\frac{\ddot{\mathrm{a}}_{\mathrm{x}}^{(12)}}{}$ |
| :---: | ---: |
| 60 | 10.248 |
| 62 | 9.849 |
| 65 | 9.206 |

Valuation data for sole participant (active as of $1 / \mathbf{1 / 2 0 0 0}$ ):
Date of birth: $\quad 1 / 1 / 1941$
Date of hire: $\quad 1 / 1 / 1980$

## Question 14

In what range is the $1 / 1 / 2000$ accrued liability?
(A) Less than $\$ 31,300$
(B) $\$ 31,300$ but less than $\$ 32,250$
(C) $\$ 32,250$ but less than $\$ 33,200$
(D) $\$ 33,200$ but less than $\$ 34,150$
(E) $\$ 34,150$ or more

## Data for Ouestion 15

Plan effective date: 1/1/1998.
Normal retirement benefit: $50 \%$ of final year's compensation.
Compensation: Pay rate as of January 1.
Actuarial cost method: Individual level premium.
Actuarial assumptions:

| Interest rate: | $7 \%$ per year |
| :--- | :--- |
| Preretirement deaths and terminations: | None |
| Salary scale: | $0 \%$ |
| Retirement age: | 65 |

Valuation data for sole participant.

## Date of birth: <br> 1/1/1950

Date of hire:
1/1/1990
Year January 1 pav rate
\$50,000
1999 45,000
2000
55,000

Selected annuity value:

$$
\ddot{\mathrm{a}}_{65}^{(12)}=8.736
$$

## Question 15

In what range is the normal cost for 2000 as of $1 / 1 / 2000 ?$
(A) Less than $\$ 7,500$
(B) $\$ 7,500$ but less than $\$ 8,000$
(C) $\$ 8,000$ but less than $\$ 8,500$
(D) $\$ 8,500$ but less than $\$ 9,000$
(E) $\$ 9,000$ or more

## Data for Ouestion 16

Plan effective date: 1/1/1980

Normal retirement benefit: $50 \%$ of final 5 -year average compensation.
Actuarial cost method: Individual entry age normal.

Actuarial assumptions:

| Interest rate: | $7 \%$ per year |
| :--- | :--- |
| Compensation increases: | None |
| Preretirement terminations other than death: | None |
| Normal retirement age: | 65 |

Valuation data for only participants as of $1 / 1 / 2000$ :

Date of birth:
Date of hire:
Monthly compensation:

Smith 1/1/1960
1/1/1995
\$2,500

Brown 1/1/1942 1/1/1982 \$3,500

Selected commutation functions:

| Age | $\mathrm{D}_{\mathrm{x}}$ | $\mathrm{N}_{\mathrm{x}}$ |
| :---: | :---: | :---: |
| 35 | 920 | 12,727 |
| 40 | 651 | 8,701 |
| 58 | 174 | 1,862 |
| 65 | 97 | 893 |

Selected annuity value:

$$
\ddot{\mathrm{a}}_{65}^{(12)}=8.748
$$

## Ouestion 16

In what range is the accrued liability for 2000 as of $1 / 1 / 2000 ?$
(A) Less than $\$ 97,000$
(B) $\$ 97,000$ but less than $\$ 100,000$
(C) $\$ 100,000$ but less than $\$ 103,000$
(D) $\$ 103,000$ but less than $\$ 106,000$
(E) $\$ 106,000$ or more

## Data for Ouestion 17

Normal retirement benefit: $2 \%$ of final year's compensation for each year of service up to 15 years, plus $1 \%$ of final year's compensation for each additional year of service.

Early retirement eligibility: Age 55.
Early retirement benefit: Accrued benefit reduced by $3 \%$ for each year by which early retirement date precedes normal retirement date.

Actuarial cost method: Projected unit credit (based on accrual rates).
Actuarial assumptions:
Interest rate: 7\% per year
Compensation increase: 4\% per year
Decrements prior to age 65: None, other than retirement
Selected probabilities of retirement (beginning-of-year decrement):

|  | $\boldsymbol{q}_{x}^{(r)}$ |
| :--- | :--- |
| $\mathbf{x}$ | 0.25 |
| 55 | 0.10 |
| 56 | 1.00 |

Data for active employee Smith:

Date of birth:
Date of hire:
1999 compensation:

1/1/1955
1/1/1990
\$50,000

Selected annuity value:

$$
\ddot{\mathrm{a}}_{56}=12.400
$$

## Ouestion 17

In what range is the portion of Smith's normal cost as of $1 / 1 / 2000$ attributable to expected retirement at age 56 ?
(A) Less than $\$ 400$
(B) $\$ 400$ but less than $\$ 440$
(C) $\$ 440$ but less than $\$ 480$
(D) $\$ 480$ but less than $\$ 520$
(E) $\$ 520$ or more

## Data for Question 18

Normal retirement benefit: $\$ 1,000$ per month payable at the beginning of each month.
Normal form of benefit: 15 years certain and life.
Actuarial cost method: Unit credit.

Actuarial assumptions:

| Interest rate: | $7 \%$ per year |
| :--- | :--- |
| Preretirement decrements other than death: | None |
| Form of payment for death benefits: | Annuity for remaining term certain |

Data for participant Smith:
Date of birth: $\quad 1 / 1 / 1930$
Date of retirement: $\quad 1 / 1 / 1995$
Date of death: $\quad 12 / 31 / 1999$
Selected commutation functions based on valuation assumptions:

| $\mathbf{x}$ | $\mathrm{D}_{\mathrm{x}}$ | $\mathrm{N}_{\mathrm{x}}^{(12)}$ |
| :---: | :---: | :---: |
| 69 | 64,805 | 507,631 |
| 80 | 17,392 | 91,357 |

The beneficiary elected to receive the lump sum value of the remaining payments due upon Smith's death. The lump sum distribution is calculated using an interest rate of 5\% per year, with the payment to be made on $1 / 1 / 2000$.

## Question 18

In what range is the experience gain during 1999 due to the death of Smith and the beneficiary's form of payment election?
(A) Less than $\$ 12,000$
(B) $\$ 12,000$ but less than $\$ 14,000$
(C) $\$ 14,000$ but less than $\$ 16,000$
(D) $\$ 16,000$ but less than $\$ 18,000$
(E) $\$ 18,000$ or more

## Data for Ouestion 19

Normal retirement age: 65 .

Normal retirement benefit:
Late retirement benefit:
$2 \%$ of final 3-year average compensation for each year of service.
The greater of the retirement benefit calculated using total service until retirement or the actuarial equivalent of the benefit payable at normal retirement age, calculated using the valuation interest rate.

Death benefit: None
Assumed interest rate: $\quad 5 \%$ per year.
Data for participant Smith:

| Date of birth: | $1 / 1 / 1934$ |
| :--- | :--- |
| Date of hire: | $1 / 1 / 1969$ |
| Date of retirement: | $1 / 1 / 2000$ |
| 1996 compensation: | $\$ 56,000$ |
| 1997 compensation: | $\$ 58,000$ |
| 1998 compensation: | $\$ 60,000$ |
| 1999 compensation: |  |

Selected commutation functions:

| Age x | $\mathrm{D}_{\mathrm{x}}$ | $\mathrm{N}_{\mathrm{x}}^{(12)}$ <br>  <br> 65 |
| :---: | :---: | :---: |
| 221,867 |  |  |
| 299,624 | $3,230,371$ |  |
| $2,918,698$ |  |  |

## Ouestion 19

In what range is Smith's annual retirement benefit commencing on $1 / 1 / 2000$ ?
(A) Less than $\$ 36,000$
(B) $\$ 36,000$ but less than $\$ 36,750$
(C) $\$ 36,750$ but less than $\$ 37,500$
(D) $\$ 37,500$ but less than $\$ 38,250$
(E) $\$ 38,250$ or more

Data for Ouestion 20
Valuation date: 1/1/2001.
Normal retirement benefit: $2 \%$ of final 3-year average compensation for each year of service.
Actuarial cost method: Entry age normal.
Actuarial assumptions:

Interest:
Salary scale:
Preretirement decrements other than death:
Retirement age:
Retirement age: 65
Data for sole participant Smith:
Date of birth: $\quad 1 / 1 / 1940$
Date of hire: $\quad 1 / 1 / 1975$
2000 compensation: $\$ 50,000$
Status: Active
Selected commutation functions:

| $\mathbf{x}$ | $\underline{\mathbf{D}_{\mathbf{x}}}$ | ${ }^{\mathrm{s}} \mathbf{D}_{\mathbf{x}}$ | $\mathbf{N}_{\mathbf{x}}$ | ${ }^{\mathbf{s} \mathrm{N}_{\mathbf{x}}}$ |
| :--- | ---: | ---: | ---: | ---: |
| 35 | 894,190 | $4,932,364$ | $12,364,650$ | $138,500,016$ |
| 60 | 144,405 | $2,697,364$ | $1,483,514$ | $42,615,152$ |
| 61 | 133,046 | $2,609,460$ | $1,339,110$ | $39,917,788$ |
| 65 | 94,414 | $2,250,810$ | 868,052 | $30,013,858$ |

Selected annuity value: $\quad \ddot{\mathbf{a}}_{65}^{(12)}=8.7358$
$7 \%$ per year
5\% per year
None
65

## Ouestion 20

In what range is the mortality loss for 2000 due to Smith's survival to $1 / 1 / 2001$ ?
(A) Less than $\$ 2,150$
(B) $\$ 2,150$ but less than $\$ 2,400$
(C) $\$ 2,400$ but less than $\$ 2,650$
(D) $\$ 2,650$ but less than $\$ 2,900$
(E) $\$ 2,900$ or more

## ANSWER KEY

## MAY 2000 COURSE EA-I, B

    1. C
    2. B
    3. D
    4. B
    5. A
    6. C
    7. E
    8. A
    9. C
    10. C
    11. C
    12. D
    13. D
    14. B
    15. B
    16. A
    17. D
18. A
19. E
20. D
