# Comparisons of Modeled Height Predictions to Ocular Height Estimates 

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#### Abstract

Equations used by USDA Forest Service Forest Inventory and Analysis projects to predict individual tree heights on the basis of species and dbh were improved by the addition of mean overstory height. However, ocular estimates of total height by field crews were more accurate than the statistically improved models, especially for hardwood species. Heightpredictionsfrom the improved equations attained the desired measurement quality objective only $57 \%$ of the time, while ocular estimates achieved the desiredaccuracy $75 \%$ of the time. South. J. Appl. For. 22(4):216-221.


Measuring tree heights is costly. For extensive surveys such as those conducted by Forest Inventory and Analysis (FIA), it is not usually cost effective to measure the heights of all sampled trees. Tree heights are ultimately used to compute tree volumes, which are then aggregated to population-level estimates of inventory volume. The use of ocular height estimates by FIA has historically produced acceptable sampling errors associated with reported inventory volumes.

FIA plots in the South are measured by experienced, permanent field crews. Crews are trained to visually estimate the heights of trees after calibrating their estimates at each plot by measuring a few trees with clinometers. FIA has also developed regional height equations, based on species and diameter at breast height (dbh), to predict the heights of mortality and cut trees (because most of these are removed from the woods before field crews can measure them). Ocular estimation of tree heights, although cheaper than measured heights, is still time-consuming. It is not known whether the time spent on this endeavor is worthwhile, since the accuracy of ocular height estimates has not been compared to height predictions obtained from equations. If modeled heights compare favorably to ocular estimates, field crews might be relieved of an unnecessary task. Height equations could be programmed into data recorders for visual verification by field crews, who would override the predicted heights only for trees with unusual form or broken tops.

[^0]The objectives of this analysis were threefold:

1. To evaluate the accuracy of regional height models currently in use by FIA in the South.
2. To use additional variables already recorded by field crews in an attempt to make regional height models more site and stand specific.
3. To determine whether height predictions generated by models can replace or augment field-crew ocular estimates of tree height.

## METHODS

## The Data

Two data sets were used in this analysis-Southern Research Station (SRS) FIA tree-volume data and SRS FIA quality control (QC) data. The FIA volume data set is the result of an ongoing tree-volume study spanning 4 decades across 5 southeastern states (Cost 1978). It contains data for more than 40,000 trees measured in sections from base to tip. These data were used to develop and evaluate the height equations presented in this article.

The QC data were obtained from field checks of FIA crews working in south Georgia. Tree heights estimated by regular field crews were later measured (with poles or clinometers) by QC crews as part of FIA quality-assurance activities (USDA Forest Service 1997). The QC data were used to compare predictions of total tree height from equations with ocular estimates of total tree height by field crews. The portion of the QC data set available for this analysis is relatively small ( 385 observations) because FIA estimated only merchantable height prior to 1995.

Trees at least 5.0 in . dbh were selected for analysis from species common to both the tree-volume data set and the QC data set. The tree-volume data were divided in half on the basis of plot location number. Trees on even-numbered plots were used to develop height equations, and trees on oddnumbered plots were used to validate the models. Dividing the trees by plot location enabled testing of how well equations based on one set of site and stand conditions predict the heights of trees grown on different sites (as opposed to randomly dividing trees from all sites into two groups). These two subsets of the tree-volume data are referred to as the estimation and validation data sets, respectively. After selection of the best height models, the QC data were used to compare model predictions with ocular estimates made by field crews.

## Height M odels

Model (I), the general height equation currently used by SRS FIA, utilizes dbh to predict height:

$$
\begin{equation*}
\mathbf{H}=b_{0}+\mathbf{b}, *\left(\log _{10}(D)\right)^{0.5}+b_{2} * D^{-2} \tag{1}
\end{equation*}
$$

where
$\mathbf{H}=$ total height (ft),
$\mathbf{D}=$ tree diameter (in.) at breast height (dbh), and
$b_{i}=$ regression parameters estimated from the data.
In addition to dbh, other modelers (Matney and Sullivan 1982, Baldwin and Feduccia 1987, Zarnoch et al. 1991) have found some or all of the following independent variables to be significant predictors of tree height: stand age, site index, height of dominants and codominants, and stand density. These or related variables recorded by FIA crews were added to Model (1) in an attempt to make it more site specific. This was accomplished with stepwise regression, where various combinations and transformations of dbh and the following variables were entered into the model:

M ean overstory height (MOH).-For the estimation data set, mean overstory height was computed by averaging the heights of all dominant and codominant trees at each plot location. In the validation and QC data sets, MOH was computed from the heights of the first three overstory trees encountered at each location, which is similar to the ocular calibration procedure used by field crews at each site.

Stand age (A).-The relationship between tree age and tree height is commonly expressed in terms of site index. However, the concept of site index has limited utility for the uneven-aged stands of mixed species to which FIA models must apply (Husch et al. 1972). Site index was rejected as a potential independent variable for this reason, but it seemed promising to utilize the relationship between mean overstory height and mean stand age as a potential surrogate for classic site index. Thus, stand age and combinations of stand age and mean overstory height were considered as candidates for inclusion in the model.

Crown ratio (CR).-Crown ratio is the ratio of live crown length to total tree length, expressed in increments of $10 \%$ (coded as: $1=0-9 \%, 2=10-19 \%, \ldots, 10=90-$
$100 \%$ ). Crown ratio was considered because it provides an indication of competition experienced by individual trees. For many species, open-grown trees tend to have higher crown ratios and are generally shorter than trees of equivalent dbh grown under competition for light. Other measures of competition, such as stand basal area, were not utilized because average stand conditions do not necessarily apply to individual trees; and because such measures would not be available to the field crew until plots are completely surveyed, making the use of height equations on field data recorders logistically difficult.

Crown class (CC).-Mean overstory height roughly fixes the upper height limit at a given plot location. Crown class was added to approximate the position of individual trees in the canopy. Crown class was specified as a dummy variable with four discrete classes: $1=$ dominant; $2=$ codominant; 3 = intermediate; $4=$ overtopped.

## Evaluation Statistics

Statistics used to evaluate model predictions and crew estimates are defined as follows:

Bias.-Bias, the difference between the mean predicted or estimated value and the mean measured (true) value (Cochran 1977), is defined as:

$$
\Sigma\left(\hat{Y}_{i}-Y_{i}\right) / N
$$

where

$$
\begin{aligned}
\hat{Y}_{i}= & \text { the modeled height prediction or ocular estimate for } \\
& \text { the ith value of the validation or QC data set, }
\end{aligned}
$$

$Y_{i}=$ the measured height for the ith value of the validation or QC data set, and
$\mathrm{N}=$ the number of observations in the validation or QC data set.

R oot mean squared error (RMSE).-Mean squared error (MSE) is a relative measure of overall accuracy. The closer it is to 0 , the greater the accuracy of the estimates. MSE has two components-variance and squared bias (Cochran 1977). Differences among MSEs are therefore the result of differences in the variance and/or bias of model predictions. Our analysis utilizes the square root of MSE as an evaluation statistic:

$$
R M S E=\left(\Sigma\left(\hat{Y}_{i}-Y_{i}\right)^{2} / N\right)^{0.5}
$$

Variance is easily obtained by subtracting bias squared from MSE.

Percent absolute deviation (PAD).-PAD is the mean absolute difference between predicted (or estimated) values and measured values, expressed as a percentage of the measured value (Dougherty et al. 1995). It is the average percentage that estimates deviate from measured values (disregarding sign), and is computed as:

$$
P A D=\left(\Sigma\left(\left|\hat{Y}_{i}-Y_{i}\right| Y_{i}\right) / N\right) * 100
$$

W ithin measurement quality objective (WMQO).The southern FIA measurement quality objective for tree height is $\pm 10 \%$. WMQO is the percentage of height predictions or estimates within $10 \%$ of the measured height:

$$
W M Q O=\left(\Sigma W_{i} / \mathbf{N}\right) * 100
$$

where

$$
W_{i}=1 \text { if }\left(\left|\hat{Y}_{i}-\mathrm{Y}_{\mathrm{i}}\right| / Y_{i}\right) * 100=10
$$

or

$$
W_{i}=0 \text { if }\left(\left|\hat{Y}_{i}-Y_{i}\right| / Y_{i}\right) * 100=10
$$

## Results and Discussion

## Model Solutions

Fits of Model (1) to the estimation data set indicate that Model (1) is probably mis-specified (Table 1). Model intercepts and coefficients fluctuate widely from one species to the next, and parameter estimates for $D^{-2}$ are statistically nonsignificant in almost every case. Also, the signs on some of the coefficients are illogical. Height and the reciprocal of dbh should be negatively correlated, yet some of the coefficients for the $D^{-2}$ term are
positive. In general, Model (1) $R^{2}$ 's by species are fairly low, ranging from 0.28 to 0.63 . Despite these problems, examination of model residuals plotted over the independent variables showed no apparent trends.

Attempts to improve the FIA height model by adding variables to make it more site specific were moderately successful. Of the variables and associated transformations included in the stepwise regression, $\left(\log _{10}(D)\right)^{0.5}$ and MOH were by far the most important. The partial sums of squares of these two variables accounted for nearly all of the explained variation in almost every case. In addition to these, crown ratio and crown class improved some of the models slightly. However, the marginal contributions of the two crown variables ultimately convinced us to drop them in favor of a simpler model. Stand age was significant only in the height model for planted loblolly. The general nonsignificance of age is probably a consequence of multicollinearity between mean overstory height and stand age, and the imprecision of age estimates in natural stands. Based on these results, Model (2), specified as follows, is proposed as an alternative to Model (1):

$$
\begin{equation*}
\boldsymbol{H}=b_{0}+\boldsymbol{b}, *\left(\log _{,,,}(D)\right)^{0.5}+b_{2} * \mathbf{M O H} \tag{2}
\end{equation*}
$$

In contrast to Model (1), fits of Model (2) to the estimation data indicate that Model (2) is stable (Table 1).

Table 1. Model statistics and parameter estimates for fits of two height estimation models to the estimation data set.

| Species | Model (1)" |  |  |  |  |  | Model (2) ${ }^{\text {b }}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Model statistics |  |  | Parameter estimates |  |  | Model statistics |  |  | Parameter estimates |  |  |
|  | $R^{2}$ | RMSE ${ }^{\text {c }}$ | $C V^{\text {d }}$ | $b_{0}$ | $b_{1}$ | $b_{2}$ | $R^{2}$ | RMSE ${ }^{\text {c }}$ | $C V^{\text {d }}$ | $b_{0}$ | $b_{1}$ | $b_{2}$ |
| Natural slash | 0.59 | 8.6 | 15.9 | -76.047 | 138.183 | -104.154 | 0.84 | 5.3 | 9.9 | -63.918 | 83.321 | 0.711 |
| $P r>\|t\|$ |  |  |  | 0.001 | 0.001 | 0.368 |  |  |  | 0.001 | 0.001 | 0.001 |
| Planted slash | 0.51 | 7.3 | 14.4 | -92.355 | 153.715 | 71.239 | 0.91 | 3.2 | 6.2 | -38.932 | 51.425 | 0.827 |
| $\operatorname{Pr}>\|t\|$ |  |  |  | 0.056 | 0.001 | 0.794 |  |  |  | 0.001 | 0.001 | 0.001 |
| Longleaf | 0.28 | 9.4 | 15.5 | 41.464 | 25.821 | -577.557 | 0.76 | 5.5 | 9.0 | 43.853 | 58.883 | 0.768 |
| Pr $>\|t\|$ |  |  |  | 0.099 | 0.260 | 0.003 |  |  |  | 0.001 | 0.001 | 0.001 |
| Natural loblolly | 0.49 | 10.3 | 19.5 | -73.067 | 128.472 | -21.661 | 0.83 | 5.9 | II. 2 | -62.917 | 73.717 | 0.826 |
| $\operatorname{Pr}>\|t\|$ |  |  |  | 0.001 | 0.001 | 0.863 |  |  |  | 0.001 | 0.001 | 0.001 |
| Planted loblolly | 0.59 | 6.7 | 13.9 | -1 17.469 | 174.186 | 109.633 | 0.83 | 4.3 | 8.9 | -64.001 | 84.942 | 0.642 |
| $\operatorname{Pr}>\|t\|$ |  |  |  | 0.291 | 0.102 | 0.864 |  |  |  | 0.001 | 0.001 | 0.001 |
| Pondcypress | 0.36 | 9.1 | 16.7 | 39.957 | 23.874 | -596.794 | 0.55 | 7.6 | 14.0 | -66.126 | 80.719 | 0.749 |
| $\operatorname{Pr}>\|t\|$ |  |  |  | 0.318 | 0.512 | 0.053 |  |  |  | 0.001 | 0.001 | 0.001 |
| Red maple | 0.56 | 8.3 | 14.9 | -59.232 | 115.219 | 67.380 | 0.62 | 7.7 | 13.9 | -58.130 | 92.900 | 0.362 |
| $\operatorname{Pr}>\|t\|$ |  |  |  | 0.037 | 0.001 | 0.758 |  |  |  | 0.001 | 0.001 | 0.001 |
| Sweetgum | 0.63 | 8.6 | 14.5 | -1 15.190 | 173.198 | 300.069 | 0.71 | 7.5 | 12.7 | -83.898 | 118.258 | 0.455 |
| $\operatorname{Pr}>\|t\|$ |  |  |  | 0.001 | 0.001 | 0.098 |  |  |  | 0.001 | 0.001 | 0.001 |
| Blackgum | 0.56 | 9.5 | 18.4 | -111.800 | 163.114 | 224.615 | 0.72 | 7.6 | 14.7 | -94.688 | 114.527 | 0.577 |
| $\operatorname{Pr}>\|t\|$ |  |  |  | 0.001 | 0.001 | 0.308 |  |  |  | 0.001 | 0.001 | 0.001 |
| Laurel oak | 0.54 | 8.3 | 15.2 | -73.312 | 123.708 | 314.204 | 0.63 | 7.5 | 13.6 | -50. 185 | 77.885 | 0.458 |
| $\operatorname{Pr}>\|t\|$ |  |  |  | 0.002 | 0.001 | 0.090 |  |  |  | 0.001 | 0.001 | 0.001 |
| Water oak | 0.54 | 8.4 | 14.6 | -78.339 | 132.360 | 273.113 | 0.69 | 6.9 | 12.0 | -58.626 | 86.590 | 0.491 |
| $\operatorname{Pr}>\|t\|$ |  |  |  | 0.002 | 0.001 | 0.191 |  |  |  | 0.001 | 0.001 | 0.001 |

[^1]Table 2. Means and ranges of variables used for fitting tree height estimation models to the estimation data set.

| Species | N | Total tree ht (H) |  |  | Dbh (D) |  |  | Mean overstory ht (MOH) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Mean | Min | Max | Mean | Min | Max | Mean | Min | Max |
|  |  |  | $\cdot(\mathrm{ft})$ |  |  | (in,) |  |  | '(ft) |  |
| Natural slash | 967 | 53.9 | 20.0 | 90.0 | 8.6 | 5.0 | 20.9 | 53.9 | 22.0 | 76.1 |
| Planted slash | 212 | 51.0 | 29.0 | 80.0 | 7.3 | 5.0 | 14.0 | 51.4 | 31.0 | 73.5 |
| Longleaf | 491 | 60.5 | 25.0 | 89.0 | 10.5 | 5.0 | 26.4 | 59.3 | 27.3 | 81.7 |
| Natural loblolly | 874 | 52.9 | 17.0 | 93.0 | 10.0 | 5.0 | 23.0 | 52.5 | 27.3 | 78.5 |
| Planted loblolly | 49 | 47.8 | 27.0 | 67.0 | 7.8 | 5.2 | 11.9 | 50.2 | 27.5 | 62.5 |
| Pondcypress | 143 | 54.7 | 20.0 | 86.0 | 9.7 | 5.1 | 22.3 | 55.8 | 40.0 | 68.4 |
| Red maple | 115 | 55.6 | 29.0 | 95.0 | 10.5 | 5.0 | 41.8 | 60.5 | 43.6 | 84.0 |
| Sweetgum | 257 | 59.2 | 26.0 | 113.0 | 10.0 | 5.0 | 31.7 | 59.3 | 31.5 | 87.6 |
| Blackgum | 195 | 51.9 | 25.0 | 93.0 | 10.1 | 5.0 | 32.7 | 58.8 | 33.8 | 78.5 |
| Laurel oak | 153 | 54.7 | 30.0 | 95.0 | 11.4 | 5.0 | 29.6 | 59.0 | 34.8 | 75.8 |
| Water oak | 165 | 57.3 | 30.0 | 91.0 | 10.9 | 5.0 | 30.1 | 60.2 | 28.5 | 87.6 |

All parameter estimates are significant, they do not fluctuate much among species, and all coefficients behave logically. As expected, tree height is positively correlated with dbh and mean overstory height. Model (2) $R^{2}$ ' $s$, root mean squared errors, and coefficients of variation are better than corresponding values from Model (1) in every case. As with Model (1), no trends were apparent in the residuals from Model (2).

Distributions of the variables used in Models (1) and (2) are provided in Table 2.

## M odel Validation

Comparisons of the two models using the validation subset of the tree-volume data provide further evidence that Model (2) is superior (Table 3). The following results are significant:

1. For all species combined, the $R M S E$ for Model (2) is 2.2 ft less than the $R M S E$ for Model (1), indicating an improvement in statistical accuracy. This improvement can be attributed to reduction in variance, because the bias associated with both models is about the same ( 0.7 ft ).
2. Model (2) height predictions deviate from measured heights by an average of $9.7 \%$, while the corresponding PAD for Model (1) is $14.2 \%$. Model (2) yields better height predictions for all species evaluated, with the largest improvement noted for softwoods.
3. Nearly two-thirds $(63.6 \%)$ of Model (2) height predictions were within $10 \%$ of measured height, while less than half ( $47.0 \%$ ) of Model (1) predictions were comparably accurate.

Table 3. Comparisons of predictions from two height estimation models using the validation data set.

| Species | N | Measured ht |  |  | Model (1)" ht predictions |  |  |  | Model (2) ${ }^{\text {b }}$ ht predictions |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Mean | Min | Max | RMSE ${ }^{\text {c }}$ | B i a s | $P A D{ }^{\text {d }}$ | $W M Q O^{+}$ | RMSE ${ }^{\text {c }}$ | Bias | PAD ${ }^{\text {d }}$ | $W M Q O^{+}$ |
|  |  |  |  |  | (ft)* |  |  | (\%) ${ }^{-}$ | - (ft) | - |  | (\%) $\cdots$ |
| Natural slash | 982 | 51.9 | 21.0 | 95.0 | 8.2 | 0.9 | 14.0 | 48.0 | 5.8 | 0.2 | 8.8 | 66.0 |
| Planted slash | 198 | 48.8 | 27.0 | 72.0 | 6.6 | 1.6 | 11.6 | 57.1 | 3.9 | 1.0 | 6.6 | 83.8 |
| Longleaf | 542 | 56.3 | 28.0 | 87.0 | 9.4 | 3.5 | 15.0 | 47.8 | 6.3 | 2.1 | 9.0 | 67.2 |
| Natural loblolly | 806 | 54.6 | 19.0 | 98.0 | 9.1 | -1.2 | 14.4 | 42.9 | 7.0 | 0.7 | 10.1 | 62.5 |
| Planted loblo | lly 19 | 53.4 | 25.0 | 78.0 | 7.2 | -0.4 | 12.5 | 42.1 | 3.5 | -0.8 | 6.0 | 89.5 |
| Pondcypress | 119 | 52.5 | 22.0 | 93.0 | 13.0 | 2.6 | 23.6 | 31.9 | 7.3 | 1.5 | 12.1 | 56.3 |
| Red maple | 90 | 51.2 | 31.0 | 87.0 | 7.8 | 1.5 | 12.8 | 48.9 | 6.9 | 0.8 | 11.0 | 56.7 |
| Sweetgum | 228 | 57.8 | 27.0 | 105.0 | 8.4 | -1.5 | 11.8 | 48.2 | 7.3 | -0.8 | 10.8 | 55.3 |
| Blackgum | 155 | 54.1 | 22.0 | 88.0 | 8.4 | -0.2 | 13.4 | 49.0 | 8.0 | 0.5 | 13.0 | 51.0 |
| Laurel oak | 133 | 55.6 | 22.0 | 91.0 | 9.5 | 0.1 | 15.0 | 44.4 | 8.1 | 0.3 | 12.5 | 55.6 |
| Water oak | 103 | 52.8 | 27.0 | 80.0 | 8.1 | 2.1 | 13.1 | 60.2 | 8.0 | 0.5 | 12.8 | 50.5 |
| All softwoods | 2,666 | 53.4 | 19.0 | 98.0 | 8.9 | 0.9 | 14.6 | 46.3 | 6.2 | 0.8 | 9.2 | 66.2 |
| All hardwoods | 709 | 55.0 | 22.0 | 105.0 | 8.5 | 0.0 | 13.0 | 49.5 | 7.7 | 0.1 | 11.9 | 53.9 |
| All species | 3,375 | 53.7 | 19.0 | 105.0 | 8.8 | 0.7 | 14.2 | 47.0 | 6.6 | 0.7 | 9.7 | 63.6 |

[^2]Table 4. Comparisons of Model (2) ${ }^{a}$ height predictions and ocular height estimates using the quality control data set.

| Species | N | Measured ht |  |  | Model (2) ht predictions |  |  |  | Ocular ht estimates |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Mean | Min | Max | RMSE ${ }^{\text {b }}$ | Bias | PAD' | $W M Q O^{d}$ | RMSE ${ }^{\text {b }}$ | Bias | PAD' | $W M Q O^{\text {d }}$ |
|  |  | - . |  | .(ft)... | ... |  | $\ldots$ | \%)........ | ........ | ) ${ }^{\text {ana.... }}$ | $\ldots$ | )........... |
| Natural slash | 172 | 57.5 | 24.0 | 86.0 | 6.6 | -1.5 | 8.3 | 69.8 | 6.0 | 0.3 | 7.7 | 76.2 |
| Planted slash | 11 | 25.9 | 21.0 | 30.0 | 3.6 | -2.0 | 11.5 | 45.5 | 2.2 | -0.2 | 7.1 | 72.7 |
| Longleaf | 8 | 53.3 | 38.0 | 71.0 | 8.3 | 4.7 | 14.9 | 37.5 | 4.2 | -3.0 | 7.2 | 62.5 |
| Natural loblolly | 63 | 35.0 | 25.0 | 86.0 | 4.0 | -2.8 | 9.3 | 57.1 | 2.9 | -2.2 | 7.4 | 71.4 |
| Planted loblolly | 11 | 38.5 | 32.0 | 43.0 | 4.7 | -3.5 | 10.2 | 54.5 | 1.9 | -0.5 | 4.5 | 100.0 |
| Pondcypress | 13 | 48.0 | 35.0 | 65.0 | 5.3 | -0.8 | 8.3 | 61.5 | 3.5 | -0.2 | 6.0 | 84.6 |
| Red maple | 24 | 53.8 | 30.0 | 78.0 | 12.5 | -1.7 | 19.3 | 33.3 | 5.4 | -2.0 | 8.3 | 70.8 |
| Sweetgum | 12 | 56.6 | 43.0 | 84.0 | 10.6 | 5.0 | 18.4 | 25.0 | 6.2 | -1.4 | 9.7 | 50.0 |
| Blackgum | 26 | 47.4 | 26.0 | 78.0 | 8.2 | -0.5 | 14.9 | 46.2 | 5.4 | -2.3 | 6.4 | 80.8 |
| Laurel oak | 12 | 52.8 | 36.0 | 78.0 | 9.5 | -0.9 | 16.0 | 25.0 | 8.4 | 0.3 | 10.8 | 58.3 |
| Water oak | 33 | 53.1 | 32.0 | 80.0 | 8.6 | -2.6 | 12.3 | 48.5 | 4.7 | 0.5 | 6.9 | 75.8 |
| All softwoods | 278 | 49.9 | 21.0 | 86.0 | 5.9 | -1.7 | 8.9 | 64.0 | 5.1 | -0.4 | 7.4 | 75.9 |
| All hardwoods | 107 | 52.2 | 26.0 | 84.0 | 9.8 | -0.8 | 15.6 | 39.3 | 5.7 | -1.0 | 7.8 | 71.0 |
| All species | 385 | 50.5 | 21.0 | 86.0 | 7.2 | -1.4 | 10.8 | 57.1 | 5.3 | -0.6 | 7.5 | 74.5 |

a $H=b_{0}+\mathrm{b}, *\left(\log _{10}(D)^{0.5}+b_{2}\right.$. MOH: where $H=$ tree height ( ft ), $D=$ diameter at $4.5 \mathrm{ft}(\mathrm{in}$.) and MO/i= mean overstory height
b $R M S E=$ root mean squared error.
c $P A D=$ percent absolute deviation.
d $W M O O=$ percentage of predictions within $10 \%$ measurement quality objective.

Table 5. Comparisons of volume predictions based on Model (2) ${ }^{\mathbf{a}}$ heights with volume predictions based on ocular heights, using the quality-control data set.

| Species | N | Vol by measured ht |  |  | Vol by Model (2) ht |  |  |  | Vol by ocular ht |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Mean | Min | Max | $R M S E^{\text {b }}$ | Bias | $P A D{ }^{\text {, }}$ | WMOO ${ }^{\text {d }}$ | RMSE ${ }^{\text {d }}$ | Bias | $P A D^{\prime}$ | $W M O O^{d}$ |
|  |  |  |  |  |  |  | ...........(\%)........ |  | $\ldots . . . . . . .(\mathrm{ft}) \times . . . . . .$. |  | ......... (\%)......... |  |
| Natural slash | 172 | 8.6 | 0.5 | 44.7 | 1.6 | -0.4 | 9.9 | 66.3 | 1.5 | 0.0 | 9.2 | 69.2 |
| Planted slash | 11 | 0.8 | 0.4 | 1.2 | 0.2 | -0.1 | 24.2 | 9.1 | 0.1 | 0.0 | 15.7 | 36.4 |
| Longleaf | 8 | 10.3 | 1.9 | 20.3 | 1.2 | 0.5 | 19.2 | 37.5 | 0.9 | -0.5 | 9.2 | 62.5 |
| Natural loblolly | 63 | 3.7 | 0.6 | 72.0 | 0.7 | -0.3 | 14.6 | 28.6 | 0.5 | -0.1 | I1. 8 | 42.9 |
| Planted loblolly | 11 | 2.5 | 1.2 | 5.1 | 0.4 | -0.3 | 14.7 | 36.4 | 0.2 | 0.0 | 6.4 | 90.9 |
| Pondcypress | 13 | 5.6 | 1.8 | 15.6 | 0.9 | -0.2 | 8.7 | 61.5 | 0.6 | -0.1 | 6.2 | 92.3 |
| Red maple | 24 | 9.3 | 1.5 | 43.1 | 2.5 | 0.0 | 20.3 | 33.3 | 1.1 | -0.3 | 8.7 | 70.8 |
| Sweetgum | 12 | 9.5 | 1.3 | 28.8 | 2.1 | 0.6 | 24.0 | 16.7 | 1.1 | -0.4 | 12.6 | 41.7 |
| Blackgum | 26 | 10.7 | 1.4 | 85.2 | 2.0 | 0.3 | 17.5 | 46.2 | 1.9 | -0.8 | 6.9 | 69.2 |
| Laurel oak | 12 | 17.5 | 2.9 | 88.1 | 4.0 | 0.2 | 16.5 | 33.3 | 4.0 | 1.6 | 11.4 | 50.0 |
| Water oak | 33 | 13.6 | 1.6 | 114.3 | 2.0 | -0.5 | 12.5 | 45.5 | 0.8 | 0.1 | 7.1 | 75.8 |
| All softwoods | 278 | 6.8 | 0.4 | 72.0 | 1.4 | -0.3 | 11.9 | 53.2 | 1.2 | 0.0 | 9.8 | 63.7 |
| All hardwoods | 107 | I1. 9 | 1.3 | 114.3 | 2.4 | 0.0 | 17.2 | 38.3 | 1.8 | -0.1 | 8.5 | 66.4 |
| All species | 385 | 8.3 | 0.4 | 114.3 | 1.7 | -0.2 | 13.4 | 49.1 | 1.4 | -0. 1 | 9.4 | 64.4 |

[^3]
## M odeled Heights vs. Crew 0 cular E stimates

Although Model (2) is an improvement over Model (1), ocular height estimates from field-crews are superior to Model (2), as evidenced by the following comparisons from the QC data set (Table 4):

1. Across all species, the RMSE associated with the ocular estimates is 1.9 ft less than the corresponding value for Model (2).
2. Field crews out-performed the model for all species evaluated, but the difference is more pronounced for the hardwoods. For all softwoods combined, the PAD from measured height was $8.9 \%$ for Model (2) predictions and $7.4 \%$ for the ocular estimates. Viewing all hardwoods combined, the PAD for Model (2) predictions was twice the PAD of the crew estimates ( $15.6 \%$ vs. $7.8 \%$ ).
3. Model (2) height predictions met the target measurement quality objectives only $57.1 \%$ of the time while field crews achieved the desired measurement quality objective $74.5 \%$ of the time.

Based on these results, the use of height equations on data recorders is not recommended. The availability of inferior height predictions from models would adversely influence field crew's ocular estimates.

## Effect of M odeled and $\mathbf{O}$ cular H eights on Volume Predictions

Ultimately, FIA height estimates are used in the computation of volume. FIA calculates gross cubic-foot volume ( $V$ ) with the equation:

$$
V=b_{0}+b_{1} * D^{2} * \mathrm{H}
$$

Measured, predicted, and crew-estimated heights from the QC data set were processed through this equation to determine if better height estimates from field crews translate into improved tree-volume predictions. Only one value for $D$ was assigned to each tree (the $D$ measured by the QC crew), so
differences in volume predictions shown in Table 5 are solely the result of differences among height estimates.

Results of the volume comparisons reinforce the conclusions drawn from the height comparisons. Tree-volume predictions based on ocular height estimates are more accurate than those based on modeled heights, especially for hardwoods.

## Conclusions

Regional total-height models based on species and dbh are substantially improved by adding mean overstory height as an independent variable. Even so, the enhanced equations are inferior to ocular height estimates from field crews, particularly for hardwood species. Height predictions from the improved equations attained the desired measurement quality objective $57 \%$ of the time, while ocular estimates achieved the desired accuracy $75 \%$ of the time. Unless an $18 \%$ marginal reduction in measurement quality is tolerable ( $32 \%$ for hardwoods), height equations should not replace independent ocular estimates by welltrained, experienced field crews.

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[^1]:    a $H=b_{0}+b_{1} \cdot\left(\log _{10}(D)\right)^{0.5}+b_{2} \cdot D^{-2}$; where $H=$ tree height (ft), and $D=$ diameter at 4.5 ft (in.).
    a $H=b_{0}+b_{1} \cdot\left(\log _{10}(D)\right)^{0.5}+b_{2} \bullet D^{-2}$; where $H=$ tree height $(\mathrm{ft})$, and $D=$ diameter at $4.5 \mathrm{ft}(\mathrm{in}).$.
    $\mathrm{b}=b_{0}+b, \cdot\left(\log _{10}(D)^{0.5}+b_{2} \bullet M O H\right.$; where $H=$ tree height (ft), $D=$ diameter at 4.5 ft (in.) and $M O H=$ mean overstory height.
    c $R M S E=$ root mean squared error from the regression solution.
    d $C V=$ coefficient of variation from the regression solution: $($ RMSE $/ \bar{Y}) 100$.

[^2]:    a $H=b_{0}+\mathrm{b} \cdot(\log ,,(\mathrm{D}))^{0.5}+b_{2}{ }^{*} \mathrm{D}^{-2}$; where $H=$ tree height $(\mathrm{ft})$, and $D=$ diameter at $4.5 \mathrm{ft}(\mathrm{in}$.$) .$
    b $H=b_{0}+b$, • $\left(\log _{10}(D)^{0.5}+b_{2} \cdot M O H\right.$; where $H=$ tree height ( ft ), $D=$ diameter at 4.5 ft (in.) and $M O H=$ mean overstory height.
    c $R M S E=$ root mean squared error.
    $\mathrm{d} P A D=$ percent absolute deviation.
    e $W M O O=$ percentage of predictions within $10 \%$ measurement quality objective.

[^3]:    a $H=b_{0}+\mathbf{b}, \cdot\left(\log _{10}(D)\right)^{0.5}+b_{2} \cdot M O H$; where $H=$ tree height ( ft ), $D=$ diameter at 4.5 ft (in.) and $M O H=$ mean overstory height.
    ${ }^{\mathrm{b}}$ RMSE $=$ root mean squared error.
    c $P A D=$ percent absolute deviation.
    d $W M Q O=$ percentage of predictions within $10 \%$ measurement quality objective.

