# UNITED STATES DEPARTMENT OF AGRICULTURE <br> Rural Utilities Service <br> BULLETIN 1724E-150 

## SUBJECT: Unguyed Distribution Poles - Strength Requirements

TO: RUS Electric Borrowers and RUS Electric Staff
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OFFICE OF PRIMARY INTEREST: Distribution Branch, Electric Staff Division
FILING INSTRUCTIONS: This bulletin replaces Chapter V-4, "Pole Strength Calculations and Guides," of RUS Bulletin 160-2, "Mechanical Design Manual for Overhead Distribution Lines," dated April 1982.

AVAILABILITY: This bulletin is available on the Rural Utilities Service website at http://www.usda.gov/rus/electric.

PURPOSE: This guide bulletin presents equations, data, and other information needed to determine: (1) the loads applied to unguyed wood distribution poles; (2) a pole's strength requirements to sustain applied loads; and (3) maximum horizontal spans based on pole strengths. Sample solved problems are included in this bulletin to help the reader understand and apply the presented equations. At the end of this bulletin is a table of calculated ground line moments caused by wind on various species of wood poles and also a table of permitted moments at the ground line of various species of wood poles commonly used for distribution construction.


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## ABBREVIATIONS

ACSR Aluminum conductor, steel reinforced
ANSI American National Standards Institute
CFR Code of Federal Regulations
EQ Equation
IEEE Institute of Electrical and Electronics Engineers
MOR Modulus of rupture
NESC National Electrical Safety Code
RUS Rural Utilities Service
SYP Southern Yellow Pine (a type of wood pole)

## UNITS OF MEASURE

in $\quad$ inch or inches $(1$ inch $=2.54$ centimeters $=0.0254$ meters $)$
in-lb inch-pounds (inch $x$ pounds) ( 1 inch-pound $=0.370685$ newtons)
$\mathrm{ft} \quad$ foot or feet $(1$ foot $=0.3048$ meters $)$
$\mathrm{ft}-\mathrm{lb} \quad$ foot-pounds (feet x pounds) ( 1 foot-pound $=4.448222$ newtons)
kcmil $\quad 1,000$ circular mils $\left(1 \mathrm{kcmil}=5.067075 \times 10^{-6}\right.$ square meters $)$
kV kilovolts [1 kilovolt $=1,000$ volts]

## UNGUYED DISTRIBUTION POLES - STRENGTH REQUIREMENTS

## 1. INTRODUCTION

1.1 Purpose of Bulletin: This guide bulletin presents equations, data, and other information needed to determine:

- The loads applied to unguyed wood distribution poles,
- A pole's strength requirements to sustain applied loads, and
- Maximum horizontal spans based on pole strengths.

Sample solved problems are included in this bulletin to help the reader understand and apply the presented equations. A table of calculated ground line moments caused by wind on wood poles and a table of calculated permitted moments at the ground line of commonly used wood poles are included in Exhibit A at the end of this bulletin.
1.2 Scope of Bulletin: The presentation in this bulletin is limited to the horizontal loading of unguyed wood distribution poles acting as simple cantilever beams or slender columns. Unguyed poles, according to RUS distribution construction standards, have a maximum line angle of 5 degrees. (The determination of the strength requirements of guyed poles is presented in Section 15 of RUS Bulletin 1724E-153, "Electric Distribution Line Guys and Anchors.") ${ }^{1 /}$ The loading effect of transformers and other heavy equipment on poles is not included in this bulletin.
1.3 National Electrical Safety Code (NESC): Throughout this bulletin are references to rules and selected data contained specifically in the 2002 Edition of the NESC. At the time this bulletin was written, the 2002 Edition was the latest edition of the NESC. Users of this bulletin should use the rules and data, as may be periodically updated, revised and renumbered, from the most recent edition of the NESC. The NESC is published by the Institute of Electrical and Electronics Engineers, Inc., (IEEE). ${ }^{\underline{2} /}$
1.4 American National Standards Institute (ANSI): This bulletin also references ANSI 05.1-2002, Specifications and Dimensions for Wood Poles. ${ }^{3 /}$ This standard provides specifications for quality and dimensions of wood poles that are to be used in single-pole utility structures.

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## 2. CLASSIFICATION AND STRENGTH OF WOOD POLES

2.1 Classification of Wood Poles: ANSI 05.1-2002 designates the fiber stress and dimensions of natural wood poles and also classifies poles by wood species, length, and class. Usually a pole's height and classification are abbreviated. For example, a pole identified as "35-6" indicates a 35 -foot, (ANSI) Class 6 pole.
2.2 Strength of Wood Poles by Class: Annex B of ANSI 05.1-2002 defines pole classes so that poles of various species and lengths will have approximately equal load-carrying capability. The minimum circumferences specified at 6 feet from the butt, (shown in Tables 3 through 10) have been calculated such that each species in a given class will not exceed the groundline stresses tabulated in Annex B, when a given horizontal load is applied 2 feet from the top of the pole. For example, all Class 6 poles are capable of holding a 1,500-pound load applied transversely 2 feet from the top of the pole. The ground line circumferences of different species of poles in the same class will deviate because of the differences in allowable fiber stress.

## 3. EXPLANATION OF APPLIED LOADS AND MOMENTS

3.1 NESC Loading Requirements: Section 25 of the NESC requires that wind and ice loads on conductors and poles be determined according to the location (Heavy, Medium, or Light loading district) of construction. Assumed ice and wind loads have to be increased if they are expected to be greater than the minimum requirements of the NESC. Extreme wind loading has to be considered if any part of a pole or the conductors attached to it is 60 feet or more above the ground. Extreme wind loading has to be applied, using the formulas and data of Rule 250C of the NESC, if it is greater than the otherwise calculated wind and ice loading based on loading districts. Loads applied to wood poles have to be multiplied by the appropriate overload factors of NESC Table 253-1.
3.2 Combined Loading Equation: All of the loads that can be expected to be applied to a pole have to be considered in order to determine the pole's strength requirements to sustain the loads. Loads are simultaneously applied to poles in both the horizontal and vertical directions. Poles need to have sufficient strength such that the following relationship is satisfied:

$$
\begin{equation*}
\frac{M_{\text {applied }}}{S}+\frac{P_{\text {applied }}}{A} \leq M O R \tag{EQ 3.1}
\end{equation*}
$$

Where,

```
\(M_{\text {applied }}=\) Moments induced in the pole (in-lb)
\(P_{\text {applied }}=\) Vertical loads on the pole (lbs)
\(S \quad=\) Section of modulus (in \({ }^{3}\) )
\(A \quad=\) Cross section area of pole \(\left(\mathrm{in}^{2}\right)\)
\(M O R \quad=\) Modulus of rupture \(\left(\mathrm{lb} / \mathrm{in}^{2}\right)\)
```

Usually the P/A portion of Equation 3.1 is negligible in comparison with the $\mathrm{M} / \mathrm{S}$ portion of the equation and thus is ignored in the distribution pole strength calculations of this bulletin.
3.3 Direction of Critical Loading: By using vector algebra, all horizontal loads applied to a pole can be calculated in 2 component directions: longitudinal (parallel to the direction of the line) and transverse (perpendicular to the line). Usually there is only one direction of loading that dictates the minimum class of pole required to sustain all of the loads expected to be applied. This direction is called the direction of critical loading. Computations for pole strength requirements only need be made for the direction of critical loading when that direction is known. The direction of critical loading for unguyed poles is in the transverse direction.

## 4. HORIZONTAL MOMENTS ON A POLE

4.1 Equations for Applied Moments: In this bulletin, an applied moment is the multiplication product of an applied load or force times the distance from its centroid to the ground line of the pole. The unit of measure used in this bulletin for moments is foot-pounds ( $\mathrm{ft}-\mathrm{lb}$ ). The sum of all of the applied moments multiplied by the appropriate NESC overload factors, has to be determined before a pole of sufficient strength (i.e., class) can be selected. The total of all the ground line moments induced in a pole, $M_{g}$, is expressed as follows:

$$
\begin{equation*}
M_{g}=S_{h} M_{w c}+M_{w p}+M_{w e}+M_{t c}+M_{v o}+M_{p-\delta} \tag{EQ 4.1}
\end{equation*}
$$

Where:
$S_{h} \quad=$ Horizontal wind span ( = the sum of $1 / 2$ the lengths of the adjacent spans) (ft)
$M_{w c}=$ Summation of moment loads due to wind on each conductor expressed as moment per unit length of conductor ( $\mathrm{ft}-\mathrm{lb} / \mathrm{ft}$ )
$=F_{o w}\left\{\Sigma\left(W_{c} H_{c}\right)\right\} \cos (\theta / 2)$
$M_{w p}=$ The moment due to wind on the pole ( $\mathrm{ft}-\mathrm{lb}$ )
$=F_{o w} W_{p}\left(\frac{2 C_{t}+C_{g}}{K_{c}}\right) H_{p}^{2}$
Note: $M_{w p}$ is calculated for several commonly used poles and tabulated in Table 1 in Exhibit A at the end of this bulletin.
$M_{w e}=$ The moment due to wind on the material and equipment attached to the pole (ft-lb)
$M_{t c}=$ Summation of moments due to the tension of the conductors ( $\mathrm{ft}-\mathrm{lb}$ )
$=2 F_{o t}\left\{\Sigma\left(T_{c} H_{c}\right)\right\} \sin (\theta / 2)$
$M_{v o}=$ The moment due to unbalanced vertical loads (ft-lb)
$M_{p-\delta}=$ The moment due to pole deflection (ft-lb)

And where:
$F_{\text {ow }}=$ NESC (Table 253-1) overload factor for wind loads
$F_{o t}=$ NESC (Table 253-1) overload factor for longitudinal (tension) loads
$H_{p} \quad=$ Height of pole above ground (ft)
$H_{c}=$ Height of each conductor attachment above ground line (ft)

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$$
\begin{aligned}
W_{c} & =\text { Wind load per unit length of each conductor }(\mathrm{lb} / \mathrm{ft}) \\
W_{p} & =\text { Wind load per unit area surface of pole }\left(\mathrm{lb} / \mathrm{ft}^{2}\right) \\
T_{c} & =\text { Tension in each conductor }(\mathrm{lb}) \\
\theta & =\text { Line angle at pole (degrees) } \\
C_{t} & =\text { Pole circumference at top (in) } \\
C_{g} & =\text { Pole circumference at ground line (in) } \\
K_{c} & =\text { Calculation constant }=72 \pi
\end{aligned}
$$

4.2 Simplification of Applied Moment Equation: The following force moment terms of Equation 4.1 can usually be omitted for the following reasons:
4.2.1 $M_{w e}$ can usually be ignored because the transverse moment due to wind on pins, insulators and the ends of crossarms is typically less than $500 \mathrm{ft}-\mathrm{lb}$. However, $M_{\text {we }}$ should be considered for attached transformers or other large equipment. Throughout this bulletin it is assumed that no large equipment is attached to the pole.
4.2.2 $M_{t c}$ is zero on tangent poles where the line angle $\boldsymbol{\theta}=\mathbf{0}$ because the sine of $(\theta / 2)=0$ and thus $M_{t c}=2 F_{o t}\left\{\Sigma\left(T_{c} H_{c}\right)\right\} \sin (\theta / 2)=0$. The nearly equal and opposite longitudinal conductor tensions essentially cancel each other.
4.2.3 $M_{v o}$ is usually small and can be ignored. RUS standard crossarm assemblies are symmetrical (looking in the longitudinal direction). Thus, the moments induced in the pole by conductor weights supported by crossarms cancel one another. The remaining conductors are attached directly to the pole. Therefore, the moment induced in the pole due to offset conductor weights is negligible. (Vertical conductor weights alone seldom dictate the required pole class.)
4.2.4 $M_{p-\delta}$ are small ground line moments. Transverse loads cause an unguyed pole to deflect a small distance. Vertical loads on the pole times this deflection distance cause additional moments to be induced in the pole. These additional moments are small compared to the other moments of Equation 4.1 and compensated for in Equation 5.2.
4.3 Simplified Equation for Applied Moments: After applying the assumptions and omissions of paragraph 4.2 of this bulletin, Equation 4.1 can be simplified to:

$$
\begin{equation*}
M_{g}=S_{h} M_{w c}+M_{w p}+M_{t c} \tag{EQ 4.5}
\end{equation*}
$$

4.4 Example Problem 1: Total Horizontal Moment: Given the following information and data, calculate the moment, $M_{g}$, at the ground line of a 35 -foot unguyed pole adjacent to a highway crossing span that supports a 3-phase, crossarm assembly. The horizontal wind span $\left(S_{h}\right)$ is 300 feet. The line angle $(\theta)$ is 2 degrees.

### 4.4.1 Given pole data:

Pole: Southern Yellow Pine (SYP); 35-foot (set 6 foot deep); Class 5
$C_{t}=19$ in
$C_{g}=29$ in
$H_{p}=29 \mathrm{ft}$

### 4.4.2 Given conductor data:

3 Primary Conductors; 266.8 kcmil ACSR ("Waxwing"), $\quad W_{c}=0.5363 \mathrm{lb} / \mathrm{ft}$
1 Neutral Conductor: \#1/0 ACSR ("Raven"), $\quad W_{c}=0.4660 \mathrm{lb} / \mathrm{ft}$
Conductor attachment heights above ground line:

$$
H_{c}(\mathrm{ft})=\frac{\text { A phase }}{28.25} \quad \frac{\text { B phase }}{29.87} \quad \frac{\text { C phase }}{28.25} \quad \frac{\text { Neutral }}{25.50}
$$

Phase conductor design tension: $\quad T_{c}=2,408 \mathrm{lb}$
Neutral conductor design tension: $\quad T_{c}=1,731 \mathrm{lb}$

### 4.4.3 Given NESC data:

NESC Heavy Loading District; NESC Grade C construction (crossing span)
$F_{\text {ow }}=2.20$
$F_{o t}=1.30$
$W_{p}=4 \mathrm{lbs} / \mathrm{ft}^{2}$
4.4.4 The summation of moments per unit length of conductor, $M_{w c}$, due to wind on each conductor can be tabulated as follows:

| Phase |  |  |  |
| :---: | ---: | :--- | :--- |
| A | $W_{c} \underline{H}_{c}$ |  |  |
| $(0.5363)(28.25)$ | $=$ | 15.15 |  |
| B | $(0.5363)(29.87)$ | $=$ | 16.02 |
| C | $(0.5363)(28.25)$ | $=$ | 15.15 |
| N | $(0.4660)(25.50)$ | $=$ | 11.88 |
| Total | $\sum\left(W_{c} H_{c}\right)$ | $=58.20$ |  |

$$
M_{w c}=F_{o w\{ }\left\{\left(W_{c} H_{c}\right)\right\} \cos (\theta / 2)=(2.20)(58.20)(0.999)=127.91 \mathrm{ft}-\mathrm{lb} / \mathrm{ft}
$$

4.4.5 The moment due to wind on the pole is calculated using Equation 4.3 as shown below, or alternatively determined from Table 1 in Exhibit A at the end of this bulletin.

$$
\begin{aligned}
& M_{w p}=F_{o w} W_{p}\left(\frac{2 C_{t}+C_{g}}{K_{c}}\right) H_{p}^{2} \\
& M_{w p}=(2.20)(4)\left(\frac{(2)(19)+29}{72 \pi}\right)\left(29^{2}\right)=2,192 \mathrm{ft}-\mathrm{lb}
\end{aligned}
$$

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4.4.6 The summation of moments due to the tension of each conductor, $M_{t c}$, can be calculated as follows:

4.4.7 The total moment on the pole is calculated using Equation 4.5 as follows:

$$
\begin{aligned}
& M_{g}=S_{h} M_{w c}+M_{w p}+M_{t c} \\
& M_{g}=300(\mathrm{ft}) \times 127.91(\mathrm{ft}-\mathrm{lb} / \mathrm{ft})+2,192(\mathrm{ft}-\mathrm{lb})+11,440 \mathrm{ft}-\mathrm{lb}=52,004 \mathrm{ft}-\mathrm{lb}
\end{aligned}
$$

## 5. POLE STRENGTH AND REQUIREMENTS

5.1 NESC Strength Requirements of Poles: The NESC requires that a support structure be able to withstand a load equivalent to all of the expected applied loads (multiplied by the appropriate NESC overload factors) without exceeding the permitted load of the support structure. The permitted load is the designated strength of the support structure multiplied by the appropriate NESC strength factor of NESC Table 261-1A. In this bulletin "support structure" means a single, wood distribution pole. For purposes of this bulletin, the NESC strength requirement for a support structure means: the permitted moment, $M_{r}$, for a pole at the ground line has to be equal to or exceed the total ground line moment, $M_{g}$, induced in the pole. This relationship is expressed in the following equation:

$$
\begin{equation*}
M_{g} \leq M_{r} \tag{EQ 5.1}
\end{equation*}
$$

5.2 RUS Increased Moment Recommendation: RUS recommends that moment, $M_{g}$, in Equation 5.1 be increased by a minimum of 5 percent to compensate for the approximations and omissions presented in paragraph 4.2 of this bulletin. Thus, RUS recommends the following relationship be satisfied:

$$
\begin{equation*}
1.05 \times M_{g} \leq M_{r} \tag{EQ 5.2}
\end{equation*}
$$

5.3 Pole Circumference at the Ground Line: The permitted moment, $M_{r}$, for a pole at the ground line can be calculated if the pole's circumference at the ground line is known. However, pole tables tabulate pole circumferences at a fixed distance (usually 6 feet as per ANSI 05.1) from the bottom of each pole which may not be at the ground line. A pole's circumference at its ground line, based on its circumference 6 feet from its bottom, can be calculated by using following Equation 5.3:

$$
\begin{equation*}
C_{g}=\frac{\left(L_{p}-L_{g}\right)\left(C_{b}-C_{t}\right)}{\left(L_{p}-L_{b}\right)}+C_{t} \tag{EQ 5.3}
\end{equation*}
$$

Where:

$$
\begin{aligned}
C_{g} & =\text { Pole circumference at ground line (in) } \\
L_{p} & =\text { Length of pole (ft) } \\
L_{g} & =\text { Distance from pole bottom to ground line (ft) } \\
L_{b} & =\text { Distance from pole bottom to classification point per ANSI 05.1-2002 (6 feet) } \\
C_{b} & =\text { Pole circumference at distance } L_{b} \text { from bottom per ANSI 05.1-2002 (in) } \\
C_{t} & =\text { Pole circumference at top (in) }
\end{aligned}
$$

The calculated ground line circumferences $\left(C_{g}\right)$ for several commonly used distribution poles are tabulated in Table 1 in Exhibit A at the end of this bulletin.
5.4 Permitted Moment of Pole at the Ground Line: The permitted moment of a pole at its ground line can be calculated using the following equation:

$$
\begin{equation*}
M_{r}=S_{f} K_{r} F_{b} C_{g}^{3} \tag{EQ 5.4}
\end{equation*}
$$

Where:

$$
\begin{aligned}
& M_{r}=\text { Permitted moment at ground line }(\mathrm{ft}-\mathrm{lb}) \\
& K_{r}=\text { Calculation constant }=2.64 \times 10^{-4}(\mathrm{ft} / \mathrm{in}) \\
& F_{b}=\text { Designated fiber stress }\left(\mathrm{lb} / \mathrm{in}^{2}\right) \\
& S_{f} \quad=\text { NESC strength factor (NESC Table 261-1A) }
\end{aligned}
$$

The calculated permitted ground line moments $\left(M_{r}\right)$ for several commonly used distribution poles are tabulated in Table 2 in Exhibit A at the end of this bulletin.
5.5 Example Problem 2: Determine Pole Resisting Moment: Given the following pole data, determine if a 35 -foot, Class 5, Southern Yellow Pine pole ( $35-5$ SYP) is adequate to sustain the total moment of $52,004 \mathrm{ft}-\mathrm{lb}$ calculated in Example Problem 1 in paragraph 4.4 of this bulletin multiplied by 1.05 as recommended by RUS (equals $54,604 \mathrm{ft}-\mathrm{lb}$ ).

### 5.5.1 Given pole and NESC data:

$$
\begin{array}{lll}
C_{b}=29 \mathrm{in} & L_{p}=35 \mathrm{ft} & F_{b}=8,000 \mathrm{1b} / \mathrm{in}^{2} \\
C_{t}=19 \mathrm{in} & L_{g}=6 \mathrm{ft} & S_{f}=0.85 \\
& L_{b}=6 \mathrm{ft} &
\end{array}
$$

5.5.2 The pole circumference at the ground line $\left(C_{g}\right)$ does not need to be calculated for this particular pole height because $L_{g}=L_{b}=6$ feet and therefore $C_{g}=C_{b}=29 \mathrm{in}$. Normally, for other

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pole heights and classes, $C_{g}$ needs to be calculated using Equation 5.3 or determined using Table 1 in Exhibit A at the end of this bulletin.
5.5.3 The permitted moment at the ground line of a $35-5$ SYP pole can be calculated using Equation 5.4 as follows (or determined using Table 2 in Exhibit A at the end of this bulletin):

$$
\begin{aligned}
M_{r} & =S_{f} K_{r} F_{b} C_{g}^{3} \\
& =(0.85)(0.000264 \mathrm{ft} / \mathrm{in})\left(8,000 \mathrm{lb} / \mathrm{in}^{2}\right)\left(29^{3} \mathrm{in}^{3}\right) \\
M_{r} & =43,780 \mathrm{ft}-\mathrm{lb}
\end{aligned}
$$

Since the induced moment of $54,604 \mathrm{ft}-\mathrm{lb}$ is greater than the resisting moment of a SYP 35-5 pole, a pole of greater strength (higher class) needs to be selected to sustain the given loads and conditions of Example Problem 1 in paragraph 4.4 of this bulletin.
5.6 Repeat Comparison Procedure: If calculations show that a selected pole does not have adequate strength to sustain the calculated loads, then another, stronger pole needs to be selected. The permitted moment ( $M_{r}$ ) of any (new) selected pole needs to be determined and ascertained that the $M_{r}$ of the new selected pole is greater than the total moment expected to be induced in the pole. Use the equations and procedure included in paragraphs 5.1 through 5.4 of this bulletin.
5.7 Moments Above Guy Attachments: Where horizontal loads are applied at some distance above a guy attachment, it is advisable to check for the pole strength at the guy attachment location. The portion of a pole below a guy attachment is considered to be a strut with only vertical loads applied. The loads above the top guy attachment and the strength of the pole at the guy attachment location are calculated in the same manner as an unguyed pole with the following two modifications.
5.7.1 The moments above a guy attachment can be calculated and summed using the same equations and procedure presented in Section 4 of this bulletin. However, the distances from the applied loads to the pole's ground line, $H_{c}$ in Equation 4.2, has to be replaced with the distances from the applied loads to the top guy attachment location on the pole.
5.7.2 The circumference of the pole at the top guy attachment location can be calculated by replacing the distance $L_{g}$ in Equation 5.3 with the distance from the bottom of the pole to the guy attachment location. Thus $M_{r}$, in Equation 5.4 becomes the permitted moment at the guy attachment location and can be calculated and compared to the calculated moment at the guy attachment location.

## 6. DETERMINATION OF MAXIMUM HORIZONTAL SPANS

6.1 Maximum Horizontal Span: The maximum permitted horizontal span for an unguyed pole based on a pole's species, height, and class span can be calculated by essentially reversing the procedure presented in Sections 4 and 5 of this bulletin. Usually the pole height and class are known or given. When unknown, the pole's species should be assumed to be the type with the lowest fiber stress for calculation purposes.
6.2 Equation for the Maximum Horizontal Span: The (simplified) equation for the total ground line moment induced in an unguyed pole with no large or heavy equipment attached was presented in paragraph 4.1 in this bulletin as:

$$
M_{g}=S_{h} M_{w c}+M_{w p}+M_{t c} \quad(\mathrm{EQ} 4.5)
$$

Equation 4.5 can be rearranged as follows to determine the horizontal span, $S_{h}$, as a function of the induced moments in the pole:

$$
\begin{equation*}
S_{h}=\frac{M_{g}-M_{w p}-M_{t c}}{M_{w c}} \tag{EQ 6.1}
\end{equation*}
$$

By replacing $M_{g}$ in EQ 6.1 with $M_{r}$, the permitted moment of the pole at its ground line, the equation becomes an expression for the maximum horizontal span, $S_{h(\max )}$, as follows:

$$
\begin{equation*}
S_{h(\max )}=\frac{M_{r}-M_{w p}-M_{t c}}{M_{w c}} \mathrm{ft} \tag{EQ 6.2}
\end{equation*}
$$

The definitions of the moment terms in Equation 6.2 are provided in paragraphs 4.1 and 5.3 of this bulletin. $M_{t c}$ is zero where the line angle $\theta=0$, because the sine of $(\theta / 2)=0$ and thus $M_{t c}=2 F_{o t}\left\{\Sigma\left(T_{c} H_{c}\right)\right\} \sin (\theta / 2)=0$.
6.3 Example Problem 3: Determination of Maximum Span: Determine the maximum horizontal span, $S_{h(\max )}$, for a 35-5 SYP pole using the moments calculated in Example Problem 1 in paragraph 4.4 of this bulletin.

### 6.3.1 Given (previously calculated) moments:

$$
\begin{array}{lll}
M_{w p} & =2,192 \mathrm{ft}-\mathrm{lb} & \text { See paragraph 4.4.5 of this bulletin } \\
M_{t c} & =11,440 \mathrm{ft}-\mathrm{lb} & \text { See paragraph 4.4.6 of this bulletin } \\
M_{w c} & =127.91 \mathrm{ft}-\mathrm{lb} / \mathrm{ft} & \text { See paragraph 4.4.4 of this bulletin } \\
M_{r} & =41,695 \mathrm{ft}-\mathrm{lb} & \text { See paragraph 5.5.3 of this bulletin and note below. }
\end{array}
$$

Note that $M_{r}$ has been reduced by 5 percent (previously calculated at $43,789 \mathrm{ft}-\mathrm{lb}$ ) in accordance with the RUS recommendation presented in paragraph 5.2 of this bulletin.

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### 6.3.2 Maximum horizontal span:

$$
\begin{aligned}
& S_{h(\max )}=\frac{M_{r}-M_{w p}-M_{t c}}{M_{w c}} \quad(\text { EQ 6.2) } \\
& S_{h(\max )}=\frac{41,695(f t-l b)-2,192(f t-l b)-11,440(f t-l b)}{127.91(f t-l b / f t)}
\end{aligned}
$$

$$
S_{h(\max )}=219 \mathrm{ft}
$$

TABLE 1: GROUND LINE MOMENTS CAUSED BY WIND ON WOOD POLES
NESC Medium and Heavy Loading Districts (See Note 1)
NESC Grade C Construction - Non Crossing Spans (See Notes 2 and 3)

| Length <br> (ft) | GL <br> (ft) | $\begin{aligned} & \mathbf{C}_{\boldsymbol{T}} \\ & \text { (in) } \end{aligned}$ | Southern Yellow Pine \& Douglas Fir |  | Lodgepole Pine \& Red Pine |  | Western Larch |  | Western Red Cedar |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Cgl <br> (in) | $\begin{gathered} \text { Mwp } \\ (\mathrm{ft}-\mathrm{lb}) \end{gathered}$ | Cgl <br> (in) | $\begin{gathered} \text { Mwp } \\ \text { (ft-lb) } \end{gathered}$ | Cgl <br> (in) | $\begin{gathered} \text { Mwp } \\ (\mathrm{ft}-\mathrm{lb}) \end{gathered}$ | Cgl <br> (in) | $\begin{gathered} M_{w p} \\ (\mathrm{ft}-\mathrm{lb}) \end{gathered}$ |
| Class 1 |  | 27 |  |  |  |  |  |  |  |  |
| 35 | 6.0 |  | 39.0 | 2,430 | 41.5 | 2,490 | 38.0 | 2,400 | 42.5 | 2,520 |
| 40 | 6.0 |  | 41.0 | 3,410 | 44.0 | 3,520 | 40.0 | 3,370 | 45.0 | 3,550 |
| 45 | 6.5 |  | 42.8 | 4,450 | 45.8 | 4,590 | 41.8 | 4,410 | 47.2 | 4,660 |
| 50 | 7.0 |  | 44.6 | 5,660 | 47.5 | 5,820 | 43.6 | 5,600 | 49.0 | 5,910 |
| 55 | 7.5 |  | 45.9 | 6,990 | 48.8 | 7,200 | 44.9 | 6,920 | 50.8 | 7,330 |
| 60 | 8.0 |  | 47.2 | 8,490 | 50.6 | 8,770 | 46.3 | 8,410 | 52.5 | 8,930 |
| Class 2 |  | 25 |  |  |  |  |  |  |  |  |
| 35 | 6.0 |  | 36.5 | 2,260 | 38.5 | 2,310 | 35.5 | 2,230 | 40.0 | 2,350 |
| 40 | 6.0 |  | 38.5 | 3,180 | 41.0 | 3,270 | 37.5 | 3,140 | 42.5 | 3,320 |
| 45 | 6.5 |  | 40.3 | 4,150 | 42.8 | 4,270 | 39.3 | 4,110 | 44.3 | 4,340 |
| 50 | 7.0 |  | 41.6 | 5,260 | 44.5 | 5,420 | 40.6 | 5,200 | 46.0 | 5,510 |
| 55 | 7.5 |  | 42.9 | 6,510 | 45.8 | 6,710 | 42.0 | 6,440 | 47.8 | 6,840 |
| 60 | 8.0 |  | 44.3 | 7,910 | 47.1 | 8,150 | 43.3 | 7,830 | 49.1 | 8,310 |
| Class 3 |  | 23 |  |  |  |  |  |  |  |  |
| 35 | 6.0 |  | 34.0 | 2,090 | 36.0 | 2,140 | 33.0 | 2,060 | 37.5 | 2,180 |
| 40 | 6.0 |  | 36.0 | 2,940 | 38.0 | 3,020 | 35.0 | 2,910 | 39.5 | 3,070 |
| 45 | 6.5 |  | 37.3 | 3,830 | 39.8 | 3,950 | 36.8 | 3,810 | 41.3 | 4,010 |
| 50 | 7.0 |  | 38.6 | 4,860 | 41.6 | 5,020 | 38.1 | 4,830 | 43.0 | 5,110 |
| 55 | 7.5 |  | 40.0 | 6,020 | 42.9 | 6,220 | 39.5 | 5,980 | 44.3 | 6,320 |
| 60 | 8.0 |  | 41.3 | 7,320 | 44.2 | 7,560 | 40.3 | 7,240 | 45.6 | 7,690 |
| Class 4 |  | 21 |  |  |  |  |  |  |  |  |
| 35 | 6.0 |  | 31.5 | 1,920 | 33.5 | 1,970 | 31.0 | 1,910 | 34.5 | 2,000 |
| 40 | 6.0 |  | 33.5 | 2,710 | 35.5 | 2,780 | 32.5 | 2,670 | 36.5 | 2,820 |
| 45 | 6.5 |  | 34.8 | 3,530 | 36.8 | 3,630 | 33.8 | 3,490 | 38.3 | 3,690 |
| 50 | 7.0 |  | 36.1 | 4,480 | 38.6 | 4,620 | 35.2 | 4,430 | 39.6 | 4,680 |
| 55 | 7.5 |  | 37.5 | 5,560 | 39.9 | 5,730 | 36.5 | 5,500 | 41.4 | 5,840 |
| 60 | 8.0 |  | 38.3 | 6,740 | 41.2 | 6,980 | 37.9 | 6,700 | 42.7 | 7,100 |
| Class 5 |  | 19 |  |  |  |  |  |  |  |  |
| 35 | 6.0 |  | 29.0 | 1,750 | 31.0 | 1,800 | 28.5 | 1,740 | 32.0 | 1,830 |
| 40 | 6.0 |  | 31.0 | 2,480 | 33.0 | 2,550 | 30.0 | 2,440 | 34.0 | 2,590 |
| 45 | 6.5 |  | 32.3 | 3,240 | 34.3 | 3,330 | 31.3 | 3,190 | 35.8 | 3,400 |
| 50 | 7.0 |  | 33.7 | 4,110 | 35.6 | 4,220 | 32.7 | 4,060 | 37.1 | 4,310 |
| Class 6 |  | 17 |  |  |  |  |  |  |  |  |
| 35 | 6.0 |  | 27.0 | 1,600 | 28.5 | 1,630 | 26.5 | 1,580 | 30.0 | 1,670 |
| 40 | 6.0 |  | 28.5 | 2,240 | 30.5 | 2,320 | 28.0 | 2,230 | 31.5 | 2,350 |
| 45 | 6.5 |  | 29.8 | 2,940 | 31.8 | 3,030 | 28.8 | 2,890 | 32.8 | 3,070 |
|  |  | GL= | Distance | bottom | ole to gro | line (feet) |  |  |  |  |
|  |  | $\mathrm{C}_{\text {t }}=$ | Circumf | e of pole | p (inch |  |  |  |  |  |
|  |  | Cgl $=$ | Circumf | e of pole | round lin | (inches) |  |  |  |  |
|  |  | $M_{\text {wp }}=$ | Ground 1 | moment in | ed by wi | on pole (f | ounds) |  |  |  |
|  |  |  | Multiply | by 2.25 | NESC Li | loading d |  |  |  |  |
|  |  | (2) | Multiply | by 1.43 | NESC G | B constru | (Cross | and non-c | ssing span |  |
|  |  | (3) | Multiply | by 1.25 | crossing |  |  |  |  |  |

TABLE 2: PERMITTED ${ }^{(1)}$ MOMENTS AT GROUND LINE OF WOOD POLES
NESC Grade C Construction (Multiply M ${ }_{\text {R-GL }}$ by 0.75 for Grade B construction)

| DFS = |  | $\begin{array}{\|c} \hline \text { Southern } \\ \text { Yellow } \\ \text { Pine } \\ \hline \end{array}$ | $\begin{gathered} \text { Douglas } \\ \text { Fir } \end{gathered}$ | $\begin{array}{\|c\|} \hline \text { Lodgepole } \\ \text { Pine } \end{array}$ | $\begin{aligned} & \text { Red } \\ & \text { Pine } \end{aligned}$ | Western Larch | Western <br> Red Cedar |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 8,000 | 8,000 | 6,600 | 6,600 | 8,400 | 6,000 |
| Length (ft) Class | $1^{(\mathrm{ft})}$ | $\begin{gathered} \hline \mathrm{MR}_{\mathrm{R}-\mathrm{GL}} \\ (\mathrm{ft}-\mathrm{lb})) \end{gathered}$ | $\begin{aligned} & \hline M_{R-G L} \\ & (\mathrm{ft}-\mathrm{lb})) \end{aligned}$ | $\begin{aligned} & \hline M_{R-G L} \\ & (\mathrm{ft}-\mathrm{bb})) \end{aligned}$ | $\begin{gathered} \hline \text { MR-GL } \\ (\mathrm{ft}-\mathrm{lb})) \end{gathered}$ | $\begin{aligned} & \hline M_{R-G L} \\ & (\mathrm{ft}-\mathrm{bb})) \end{aligned}$ | $\begin{gathered} \hline \mathrm{MR}_{\mathbf{R}-\mathrm{GL}} \\ (\mathrm{ft}-\mathrm{lb})) \end{gathered}$ |
| 35 | 6.0 | 106,400 | 106,400 | 105,800 | 105,800 | 103,400 | 103,300 |
| 40 | 6.0 | 123,700 | 123,700 | 126,100 | 126,100 | 120,600 | 122,600 |
| 45 | 6.5 | 140,700 | 140,700 | 142,200 | 142,200 | 137,600 | 141,500 |
| 50 | 7.0 | 159,200 | 159,200 | 158,700 | 158,700 | 156,200 | 158,400 |
| 55 | 7.5 | 173,600 | 173,600 | 172,100 | 172,100 | 170,600 | 176,500 |
| 60 | 8.0 | 188,700 | 188,700 | 191,800 | 191,800 | 187,000 | 194,800 |
| Class 2 |  |  |  |  |  |  |  |
| 35 | 6.0 | 87,200 | 87,200 | 84,500 | 84,500 | 84,300 | 86,100 |
| 40 | 6.0 | 102,400 | 102,400 | 102,000 | 102,000 | 99,400 | 103,300 |
| 45 | 6.5 | 117,400 | 117,400 | 116,100 | 116,100 | 114,400 | 117,000 |
| 50 | 7.0 | 129,200 | 129,200 | 130,500 | 130,500 | 126,100 | 131,000 |
| 55 | 7.5 | 141,700 | 141,700 | 142,200 | 142,200 | 139,600 | 147,000 |
| 60 | 8.0 | 156,000 | 156,000 | 154,700 | 154,700 | 153,000 | 159,300 |
| Class 3 |  |  |  |  |  |  |  |
| 35 | 6.0 | 70,500 | 70,500 | 69,000 | 69,000 | 67,700 | 71,000 |
| 40 | 6.0 | 83,700 | 83,700 | 81,200 | 81,200 | 80,800 | 82,900 |
| 45 | 6.5 | 93,100 | 93,100 | 93,300 | 93,300 | 93,900 | 94,800 |
| 50 | 7.0 | 103,200 | 103,200 | 106,600 | 106,600 | 104,200 | 107,000 |
| 55 | 7.5 | 114,800 | 114,800 | 116,900 | 116,900 | 116,100 | 117,000 |
| 60 | 8.0 | 126,400 | 126,400 | 127,800 | 127,800 | 123,300 | 127,600 |
| Class 4 |  |  |  |  |  |  |  |
| 35 | 6.0 | 56,100 | 56,100 | 55,600 | 55,600 | 56,100 | 55,200 |
| 40 | 6.0 | 67,400 | 67,400 | 66,200 | 66,200 | 64,700 | 65,400 |
| 45 | 6.5 | 75,600 | 75,600 | 73,800 | 73,800 | 72,700 | 75,600 |
| 50 | 7.0 | 84,400 | 84,400 | 85,100 | 85,100 | 82,200 | 83,600 |
| 55 | 7.5 | 94,600 | 94,600 | 94,000 | 94,000 | 91,600 | 95,500 |
| 60 | 8.0 | 100,800 | 100,800 | 103,500 | 103,500 | 102,600 | 104,800 |
| Class 5 |  |  |  |  |  |  |  |
| 35 | 6.0 | 43,700 | 43,700 | 44,100 | 44,100 | 43,600 | 44,100 |
| 40 | 6.0 | 53,400 | 53,400 | 53,200 | 53,200 | 50,800 | 52,900 |
| 45 | 6.5 | 60,400 | 60,400 | 59,700 | 59,700 | 57,800 | 61,700 |
| 50 | 7.0 | 68,700 | 68,700 | 66,800 | 66,800 | 65,900 | 68,700 |
| Class 6 |  |  |  |  |  |  |  |
| 35 | 6.0 | 35,300 | 35,300 | 34,200 | 34,200 | 35,000 | 36,300 |
| 40 | 6.0 | 41,500 | 41,500 | 42,000 | 42,000 | 41,300 | 42,000 |
| 45 | 6.5 | 47,500 | 47,500 | 47,600 | 47,600 | 45,000 | 47,500 |

(1) "Permitted" means strength factor of NESC Table 261-1A has been factored in values of Mr-GL
$\mathbf{G L}=$ Distance from bottom of pole to ground line (feet)
Mr-gL $=$ Resistive moment of pole at ground line (foot-pounds)
DFS = Designated fiber stress of poles (pounds/square inch)

## EXHIBIT B: CONTRIBUTORS

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