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Independent Seismic Evaluation of the 24-580-980 South Connector Ramps Response to the South Connector Ramps to a Magnitude 7.25 Hayward Fault Earthquake

David B. McCallen Michael A. Gerhard David J. Trummer Robert C. Murray



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Response of the Oakland, California 24/580/980 Interchange to a Magnitude 7.25 Hayward Fault Earthquake

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Response of the Oakland, California 24/580/980 Interchange to a Magnitude 7.25 Hayward Fault Earthquake

D. McCallen* M. Gerhard* D. Trummer* R. Murray[†]

Lawrence Livermore National Laboratory New Technologies Engineering Division

*Structural Mechanics Group and [†]Geologic and Atmospheric Hazards Project

1.0 Background

The 24/580/980 interchange is located near Oakland California on the Eastern perimeter of the San Francisco Bay (Fig. 1 and Fig. 2). This interchange is a major artery in the Eastern San Francisco Bay area and provides a critical link between major bay area highways. The main Concord line of the Bay Area Rapid Transit System (BART), with ridership of approximately 270,000 per day, runs underneath the interchange.

The interchange site is approximately 4 Km from the Hayward fault and 16 Km from the San Andreas fault. The reinforced concrete interchange was designed and constructed in the mid 1960's and thus the as-built structure has many of the vulnerabilities associated with typical pre-1970's concrete structures (Roberts [1], Zelinski [2], Chai et. al. [3], Priestly and Seible [4]). In 1980 some of the seismic vulnerabilities were addressed as the Interchange was retrofit with deck hinge restrainers as part of the California Department of Transportation (Caltrans) state-wide seismic retrofit of bridge expansion joints. The interchange was subjected to earthquake motion during the 1989 Loma Prieta earthquake and sustained minor damage in some of the concrete diaphragms which support the hinge restrainer forces [5]. Caltrans engineers, working together with their external consultants Imbsen and Associates, have recently completed a seismic retrofit design for portions of the interchange. The retrofit is primarily intended to fix inadequacies in many of the 1960's vintage reinforced concrete elements which constitute the bridge superstructure and foundations.



FIGURE 1. Location of the 24/580/980 interchange.

The fundamental design philosophy which governs Caltrans retrofit strategy is prevention of bridge collapse [6] during earthquakes. Thus the retrofit scheme must insure, to a high degree of reliability, that the WS and ES lines will not collapse due to earthquake ground shaking emanating from the Hayward or San Andreas Faults.

Caltrans requested that the Lawrence Livermore National Laboratory perform an independent seismic analysis evaluation of the 24/580/980 interchange retrofit concept. The scope of work consisted of three main tasks (see Fig. 3):





(small arrows indicate viewing direction).

- ⁽¹⁾ Estimation of the site seismic hazard as quantified in terms of a site rock outcrop motion
- ② Estimation of the bridge superstructure input motion accounting for the site soil response
- ③ Evaluation of the seismic demands on the structure based on computational modeling of the structure with the proposed retrofit design



FIGURE 3. Steps in the seismic hazard evaluation.

The site hazard and soil column response evaluation are reported upon in companion documents [7,8]. The work reported on herein describes the computational modeling and assessment of seismic demands on the retrofit structure.

When subjected to extreme earthquake shaking, structures are generally expected to enter the inelastic range and exhibit some level of damage. It is economically prohibitive to design structures to remain elastic when subjected to the enormous force levels associated with strong earthquake shaking. The seismic design objective is to provide a structure with adequate ductility so that inelastic behavior can occur in a manageable way and catastrophic, brittle failure of the structure can be avoided. Unlike buildings, in which a stiff column - weak beam design philosophy results in inelastic action occurring primarily in the horizontal beam elements, bridge design philosophy attempts to ensure that inelastic action occurs in the vertical support columns. Current Caltrans design practice considers column displacement ductilities as one of the fundamental performance indicators for judging the extent of nonlinear response of concrete structures under severe seismic loading. Consequently, the focus of the LLNL study was estimation of the displacements of the superstructure for extreme earthquake motions.

In order to accurately estimate the displacements of a structure responding in the nonlinear regime, nonlinear behavior must be adequately investigated. Both geometric nonlinerities and material nonlinearities may be significant contributors to structure displacements and the effect which nonlinearities have on system displacements should be addressed. In the current study, nonlinear finite element models were utilized to estimate the response of the WS and ES lines of the 24/580/980 interchange to a moment magnitude 7.25 earthquake occurring on the Hayward Fault. Displacement demands are reported for all of the WS and ES line columns, and the influence of nonlinear concrete behavior on the global structural response (i.e. system displacements) is evaluated in detail. The response of the system for two different earthquake ground motions is investigated. The first earthquake ground motion is based on the site seismic hazard definition provided to LLNL by Caltrans. This ground motion, which was based on months of analysis and Caltrans internal peer review, provided the basis for the design of the Caltrans retrofit strategy. The second earthquake motion consists of the site motion developed independently by LLNL seismologists and geotechnical engineers [7,8]. Parametric studies have been performed to assess the sensitivity of seismic displacement demands to various factors such as steel and concrete material properties, concrete nonlinearity, and the earthquake ground motion characterization. The results of the structural response parametric studies are summarized herein.

2.0 Ground motion estimates for the interchange site

The site at the 24/580/980 interchange location consists of a deep (\equiv 400 ft.) soil formation as discussed in the report by Chen [8]. The site is approximately 4 Km west of the Hayward Fault. Because of the near-field proximity of the site, the existing database of measured earthquake motions provides limited insight into the level of potential ground motion which might be expected. Recent analytical and observational studies of ground motions in the near-field have indicated that unexpectedly large, longer period motions may be present in the near field which are not accounted for in classical probabilistic hazard evaluations. The 1992 Landers California earthquake [9] and the 1995 Kobe Japan earthquake [10] have provided hard evidence of both the high amplitude of shaking and the potential directionality of strong motion in the near field. In particular, large, longer period motions in the fault-normal direction have been observed [9,10]. These observations tend to validate the results of models predicting this type of radiation pattern for seismic waves in the near field.

A site seismic hazard estimate, for establishing site specific ground motions, has been performed by Geomatrix geotechnical consultants for Caltrans. The hazard definition supplied by Geomatrix consisted of a rock outcrop target spectrum for a moment magnitude 7.25 (M_w =7.25) earthquake occurring on the Hayward fault. The rock outcrop motion developed by Geomatrix is shown in Fig. 4a. This hazard definition was based on a median level of motion as a result of Caltrans internal decision making on the level of acceptable risk [11] for this particular interchange.

The rock outcrop motion was fit with existing recorded earthquake time histories, and the time histories were modified by a reduction factor to account for free surface amplification. The reduced time histories were then utilized as input motion to a 1D site soil column. The site response analysis was performed by Caltrans geotechnical staff using the nonlinear site response program *SUMDES* [12]. The surface time history for one component of motion is shown in Fig. 4a.

A number of experts, including Penzien [13], Idriss[14] and Gates[15] were consulted in developing the final surface motion that Imbsen and Associates and Caltrans ultimately used in the analysis and retrofit design for the interchange. Based on the computed Caltrans surface motions, Penzien recommended a smooth design spectra as indicated in Fig. 5. Idriss provided median and 84th percentile surface motion spectra based on empirically derived relationships for deep soil sites and he recommended a design spectra based on median ground motion per Caltrans design criteria (Fig. 5). Gates developed a spectra very similar to that proposed by Idriss as shown in Fig. 5. The final surface ground motions utilized in the Imbsen and Caltrans studies were obtained by using the Gates surface spectra as a target spectra and matching surface time histories to this spectra. The final surface time histories are shown in Fig. 6 and the corresponding spectra are shown in Fig. 7. The Caltrans surface time histories exhibit high frequency noise which one would not expect for a deep soil site. This appears to be an artifact of the fitting of the surface design spectrum.



FIGURE 4. Caltrans ground motion characterization. a) Rock outcrop and computed ground surface spectra; b) rock outcrop and computed surface motion spectra.



FIGURE 5. Proposed surface spectra from Penzien, Idriss and Gates.

Prior to LLNL's independent evaluation of site ground motion, LLNL did not receive a definitive policy statement from Caltrans staff on whether the analysis and retrofit design was based on median or 84th percentile motion. In light of this, ground motion estimates were initially developed for both median and 84th percentile motions. Hutchings et. al. [7] of LLNL utilized a deterministic, Empirical Green's Function (EGF) based approach to estimate ground motions at the 24/580/980 Interchange site. In their independent assessment, they reviewed the relevant geologic and seismologic data and concluded that a Hayward fault earthquake of moment magnitude 7.25 was most appropriate for definition of the hazard at this site. A probabilistic assessment of return period or yearly probability of exceedance was not within the scope of this effort. LLNL seismologists simply relied on existing geophysical data to define the Hayward fault earthquake likely to occur in the next thirty years. This independently determined magnitude matches the magnitude determined in the Caltrans hazard study.

Unlike the target spectrum approach employed in the Caltran's sponsored hazard study, the methodology employed by Hutchings and his coworkers directly generates ground motion time histories. Hutchings and his coworkers considered a suite of possible fault rupture scenarios in their ground motion estimation as detailed in reference 7. One hundred different rupture scenarios were considered and for each rupture scenario rock out-



FIGURE 6. Caltrans surface motions based on SUMDES site response computation and matching of smoothed surface target spectra. a) north component of acceleration time history; b) east component acceleration time history; c) vertical component acceleration time history.



crop ground motion time histories were generated. The one hundred rupture scenarios provided a suite of one hundred sets of ground motion time histories, and response spectra for both the median and 84th percentile motions of this suite were generated (the average of the two horizontal components was used to develop the median and 84th percentile spectra). As the LLNL seismic study progressed, and LLNL presented ground motion results to Caltrans staff, it was determined that Caltrans policy decisions had led to their utilization of median motion. Consequently, the emphasis of the LLNL structural response evaluations were placed on consideration of the median level of earthquake motion.

In order to define ground motion time histories compatible with LLNL's estimates of the median and 84th percentile motion spectra, the rupture scenarios which provided the spectra nearest to the median and 84th percentile spectra were chosen as the rock outcrop motions defining the hazard. This approach was taken, as opposed to developing an artificial time history by matching the median or 84th percentile spectra, so that phasing information in the time history would be preserved. The outcrop motions developed by Hutchings and his coworkers were provided to Chen [8] for the soil site response calculation. Chen performed a *SHAKE* analysis to bring the motions to the surface, and the final surface time histories computed by Chen and the corresponding spectra for the median motion are shown in Fig. 8 and Fig. 9. A comparison between the Caltrans median surface motions and the LLNL median surface motions is shown in Fig. 10. It is noted that the LLNL ground motion estimates are in reasonable agreement with the Caltrans hazard definition.

The input ground motions were applied to the structural model in the appropriate global coordinate directions. The orientation of the ground motion components relative to the structure are shown in Fig. 11. Because of the manner in which the Caltrans hazard definition was developed, there is no physical basis for orienting the ground motion components in any particular direction. The directions shown in Fig. 11 for the Caltrans motions were selected solely to be consistent with the characterization used by Imbsen and Caltrans. The motions developed by LLNL, on the other hand, do have physical significance in that they truly correspond to the estimated motions in the fault normal and fault parallel directions. The directionality of the LLNL motions was accurately represented in the structural model analyses as indicated in Fig. 11.







FIGURE 9. Spectra for the surface motion time histories in Fig. 8.







FIGURE 11. Orientation of the WS and ES lines and ground motion directions.

3.0 Computer model of the existing WS and ES lines

3.1 The as-built structure

The final scope of work for this study, as stipulated by Caltrans, was limited to investigation of the seismic demands on the retrofit WS and ES lines. However, when the project was initiated, the retrofit details and in-house check had not been completed and Caltrans staff was still actively working on the WS and ES lines. Since all of the retrofits were not immediately available, it was decided to first construct a computer model of the as-built structure, and to subsequently alter the as-built model to reflect the retrofits as they became available. This allowed significant progress to be made in the absence of the final retrofit configurations, and it also allowed for comparison of the computer predicted natural modeshapes with modeshapes of the as-built structure which were determined experimentally by Imbsen and Associates.

When constructing the as-built structural model, maximum flexibility was incorporated in the model generation process in order to facilitate model changes as the structural retrofits became available. The model generation process which was implemented is illustrated in Fig. 12. A *Pro-Engineer* [16] solid model was constructed for the ES and WS lines in order to define the three dimensional geometry of the structure. The solid model was then used to provide cartesian coordinates of selected points for the *SLIC* [17] finite element mesh generating program. The *SLIC* generation file was constructed with virtually all of the finite element model information, so that a complete finite element model input file could be generated for the *NIKE3D* [18] finite element analysis program with the push of a button. While requiring a more substantial amount of construction time in the initial stages, this approach proved to be very expedient as upgrades and structural changes became available.

The solid model and finite element model of the as-built structure are shown in Fig. 13 and Fig. 14 respectively. In the finite element model of the as-built structure, adjacent viaduct segments, which were coupled to the ES and WS lines through shared bents, were partially included so that the dynamic coupling effects could be approximately accounted for (see EN, C and SE lines in Fig. 14). The procedure which was used to approximate the adjacent lines included modeling the coupled structures an expansion joint or two away from the location of intersection of the two structures (depending on how close the nearest expansion joint was to the WS or ES line), and supplying vertical restraint to the deck segments at the expansion joints where the decks were truncated. A great deal of effort was not expended on modeling the attached lines since the structures were purposefully decoupled as part of the WS and ES line retrofits, and the coupled lines only impacted the model of the as-built structure. The model shown in Fig. 14 contained 11,578 active degrees of freedom.

The finite element model for the as-built structure utilized a linear elastic model for the concrete constitutive behavior and gross sections with concrete material moduli were used to characterize the concrete members. Since geometric nonlinearities associated with expansion joint behavior and material nonlinearities associated with potential restrainer



FIGURE 12. Model generation process developed to accommodate numerous structural model changes.

cable and rod yielding were to be included, the model was constructed for the nonlinear finite element program *NIKE3D*. *NIKE3D* is a general purpose program for the nonlinear analysis of solids and structures which has been developed at LLNL over approximately the past twenty years.

In order to provide a physical perspective on what the computer model is actually representing, selected segments of the as-built structure are shown in Fig. 15 and Fig. 16. Full appreciation of the massive size and height of the WS and ES line structures can only be obtained from a site visit, where the eighty foot height of the columns near the center of the WS line can be put in proper prospective. The WS line, which crosses the BART tracks is a "flyover" structure in the truest sense of the word.







FIGURE 15. Selected views of WS and ES lines.



FIGURE 16. Selected views of WS and ES lines.

3.1.1 Superstructure section properties

In the computer model of the as-built structure, one dimensional beam elements were used to represent both the box girder deck structure as well as the bent columns and bent cap beams. The accuracy of beam element idealizations of the box girder deck structure has been investigated by McCallen and Romstad [19] by comparison of beam element models with detailed, three dimensional shell based models of box girder decks. Based on this previous work, it was decided that the beam element idealization was sufficiently accurate for the global analysis in this study.

The NIKE3D finite element program has advanced fiber type beam element capabilities which allow the user to define a generalized beam element cross section via user defined integration points (Maker, Whirley and Engelmann [20]). This element definition allows the box girder deck to be subdivided into a number of zones, with each zone defined by its location and area. The program then calculates the appropriate cross section stiffnesses based on the zone definitions and the defined material stress-strain behavior for the particular zone. As discussed in a subsequent section, this fiber element provides a powerful tool for characterizing nonlinear behavior of flexural structural elements such as beams and columns in a bridge structure.

The typical zone definitions for a section of box girder deck are shown in Fig. 17, and the deck cross section definitions for all of the WS and ES Line segments are shown in Appendix B.



FIGURE 17. Box girder deck section and user defined cross section integration zones.

The basic user defined element was used to characterize the deck stiffness properties in the bridge finite element model. In order to assist in accurate representation of the deck torsional dynamics, and to help visually assess the bridge dynamics in computer animations, rigid and massless cross beams and massless and flexible shells were added to the basic deck beam model as indicated in Fig. 18. These added elements allowed a portion of the



FIGURE 18. Reduced order, composite beam/shell/lumped mass model for a box girder deck section.

deck mass to be lumped at the extreme edges of the deck, which enhances the accuracy of the torsional characteristics of the beam element deck model. A comparison of the beam element based model with a three dimensional shell element based model is shown in Fig. 19, and the modal frequencies are summarized in Table 1. The reduced order composite model provides a good approximation of the deck segment dynamic properties.

	Discrete three dimensional shell model	Composite beam/shell model	% difference
Mode #1	6.76 Hz	7.24 Hz	7%
Mode #2	12.46	14.47	16%
Mode #3	17.44	19.42	11%
Mode #4	21.45	20.24	6%

TABLE 1. Modal frequencies from detailed and reduced order models

The model of the as-built structure shown in Fig. 14 (section 3.1), employs the composite deck model for all of the deck segments.



FIGURE 19. Modeshapes of a 100 foot box girder deck segment as computed from detailed discrete and reduced order composite models.

3.1.2 Nonlinear expansion joint model - restraining devices and impact model

Recent numerical simulations of seismic bridge response (Fenves [21]) and measurements of field performance of bridges in earthquakes (Shakal et. al. [22]) have indicated that during significant seismic shaking, geometric nonlinearities associated with impact and tensioning of restraining devices can have a significant influence on the global dynamic bridge response. Based on examination of bridge response records for a major Southern California concrete bridge, Malhotra et. al. [22] found that significant collisions and impact forces can occur between adjacent bridge frames even under relatively modest ground excitation levels (i.e. 0.10 pga).

As a result of deck discontinuities created by expansion hinges, many bridge structures actually behave as a system of partially coupled frames with significantly different coupling in the longitudinal and transverse directions. An accurate numerical model must address the complex, geometrically nonlinear coupling between adjacent bridge frames.

The WS and ES lines contain thirteen expansion hinges as shown in Fig. 20, and the expansion joints divide the overall structure into fourteen distinct frames. The restrainers at the expansion hinges employ both steel rod and cable restrainers as shown in Fig. 20. The length of the expansion joint seats on these particular structures range from fourteen inches to sixteen inches depending on the hinge [23].

The expansion hinge model incorporated in the structural model of the WS and ES lines consists of penalty function based contact surfaces to account for potential impact across the expansion hinge (Fig. 21). In terms of physical interpretation, the penalty contact surface essentially places a stiff, zero length spring between adjacent contacting elements in order to transfer contact forces from adjacent bridge segments across a closed joint. The forces generated by the contact surface ensure displacement compatibility is enforced across a joint, i.e. two contacting surface cannot penetrate one another. When the expansion joint is open, the penalty contact surface algorithm correctly senses that the contact surface has opened, removes the contact springs, and thus provides the appropriate stress free condition across the contact surface interface. The manner in which penalty contact forces are manifested in the global equilibrium equations is summarized in McCallen and Romstad [24].

The potential tensioning of expansion joint restrainers is modeled with discrete elements in the *NIKE3D* finite element model. *NIKE3D* discrete elements can be used to define an arbitrary, linear or nonlinear force-displacement behavior which is generated by relative displacement between two specified model node points. Caltrans load testing of restraining cables and restraining rods has shown that when tensioned, the rod and cables exhibit essentially elasto-plastic behavior once the member yield stress is obtained. Caltrans data for a steel expansion hinge restraining rod is shown in Fig. 22a. The force-deflection characteristics of a tension-only, elasto-plastic discrete member used to model the rod restrainer are shown in Fig. 22. As shown in the comparison in Fig. 22c, the simple tension-only elasto-plastic discrete element adequately represents the restrainer behavior.



FIGURE 20. Expansion joint hinges in the WS and ES lines.



Oblique view of expansion joint model



Typically, adjacent bridge frames are weakly coupled in the longitudinal direction because the expansion seats are specifically designed to accommodate relative bridge displacements. In the transverse direction, however shear keys appear to result in a strong coupling between adjacent bridge frames with minimal relative displacement of adjacent deck segments. To replicate this behavior in the finite element model, contact surfaces and discrete elements were used to model the longitudinal coupling and stiff transverse stiffness elements were used to model the coupling forces provided by transverse shear keys. In the vertical direction, large gravity forces result in continuous contact between adjacent deck segments at the expansion hinge seat and this condition was emulated by enforcing vertical displacement compatibility by master/slaving adjacent deck nodes in the vertical direction.

In the bridge joint idealization employed in this study, frictional forces at the expansion joints, which might add resistance to relative longitudinal motion between adjacent frames, were neglected. The rational for this idealization was the fact that field observations indicate that the frictional forces tend to be small relative to the shear forces in the frame members. Discussions with Fenves [25] indicated that his work tends to confirm the fact that the longitudinal friction forces have little if any influence on the dynamics of the individual frames. In addition, the observations of Shakal et. al. indicate that the friction forces were incapable of preventing significant relative bridge frame motions at 0.1g ground accelerations, and the ground motions in the current study are significantly larger than this.



FIGURE 22. Discrete element model of rod and cable behavior. a) Measured bar forcedeflection; b) discrete element force-deflection; c) comparison of measured and computed behavior; d) tension-compression characteristics of discrete element.

Based on the expansion joint idealizations used in this study, the linearized, small displacement model of two adjacent bridge frames results in the natural modeshapes shown in Fig. 23. The joint model provides the desired coupling between the adjacent bridge segments. Longitudinally, the bridge segments are essentially decoupled with each segment of the linearized model able to vibrate longitudinally independent of the adjacent bridge segment. Transversely and torsionally the bridge segments are closely coupled, and the vertical displacements of the adjacent bridge segments at the hinge location are identical, this type of vertical connectivity is desirable in light of the fact that under gravity deadload, contact should be maintained at the expansion joint seat.

The fourteen distinct frames of the WS and ES line are shown in plan view in Fig. 24. Each frame is bounded by expansion joints or abutments at either end. The retrofit strategy employed by Caltrans is intended to ensure the integrity of all fourteen individual frames against collapse.



FIGURE 24. Subdivision of the overall structure: individual frames delineated by expansion joints and abutments.



FIGURE 23. Natural modeshapes of two frames linearized about the infinitesimal deformation configuration: interaction between adjacent frames.

3.1.3 Column-footing connectivities and representation of foundation compliance

For the analyses of the as-built structure, a rigid foundation assumption was applied for all of the column footings. Thus the flexibility of the column footing/pile/soil system was neglected. Since the primary objective of the study was to investigate the retrofit structure, it was decided that construction of foundation compliance matrices for the as-built structure would not be an effective expenditure of project time. Whereas the as-built superstructure model could be expediently modified to account for the seismic retrofits, the generation of foundation compliances would essentially have to be entirely redone for the retrofit model. Consequently all analysis results for the as-built structure in the following sections are predicated on rigid foundation mat assumptions.

As designated in the as-built construction drawings, the construction details of typical column/footing connections are shown in Fig. 25 and Fig. 26. Based on the construction details, it appears that the small aspect ratio columns from the multiple column bents are intended to be pinned about both axes (i.e. about both "X" and "Y" axes in Fig. 25). The connectivity of the large aspect ratio columns, on the other hand, provides significant moment resisting capability about the longitudinal axis (i.e. the "Y" axis in Fig. 26).

The column-to-footing connectivity actually achieved in the field will likely be dependent on the amplitude of the dynamic response of the structure. For many of the bents the actual footing location is significantly below grade as indicated in Fig. 27. Under low amplitude, ambient type vibration, the actual achieved connectivity between the columns and footings will likely be closer to a fixed connection as the soil overburden helps restrain rotations at the base of the embedded columns. Under strong earthquake excitation however, when the soil surrounding the soil undergoes significantly larger strains and is pushed back from the column, the connections should more closely approximate the intended pinned connections.

As indicated in Fig. 28, the vast majority of the connections between the columns and footings were designed as pinned connections in the original as-built structure. Figure 29 shows the footing connectivity of the columns correlated with the location of each of the major structural frames.

The column - footing connectivites were one of the structural features which received the most attention in the retrofit design. As discussed in a subsequent section, the retrofit design included increasing the column - footing connectivity to a full moment connection for a large number of the columns.



FIGURE 25. As-built construction details for pinned columns (multiple column bent).



FIGURE 26. As-built construction details for pinned columns (single column bent).


.

FIGURE 27. Examples of embedment depth of selected column footings.

35



FIGURE 28. Column - footing connectivity based on the as-built construction details.



FIGURE 29. Column connectivity for each frame.

3.1.4 Natural modeshapes of the structural system

The ultimate aim of the LLNL modeling work was to develop a nonlinear model of the WS and ES line structures. However, a significant amount of information about the dynamic response characteristics of the structures can be obtained from inspection of linear analyses results. Linear, transient analyses can be performed as an economical precursor to fully nonlinear analyses in order to gain insight into the transient response of a complex dynamic system. The degree of correlation between the natural frequencies of the structural system and the dominant frequencies of the dynamic forcing function provides fundamental information on the expected level of dynamic amplification in the structural system. Solution of the eigenproblem for a linearized structural model can also provide a significant measure of model validation by inspection of the reasonableness of the computed modeshapes and by comparison to measured modeshapes if the engineer is fortunate enough to have measured modal quantities.

In the current work, modal analyses were performed to determine the relationship between the structural frequencies and the dominant ground motion frequencies and to compare with measured modeshapes and frequencies obtained by Imbsen and Associates. The natural vibration characteristics of the WS and ES line structures were investigated for two different sets of column boundary conditions. The first set of boundary conditions considered all columns as having complete moment transferring capability between the column and the footing. The second set considered the as-built specification for the column base fixity which consisted primarily of pin fixity between the columns and the footings. The first twelve natural modeshapes computed with the global computer model of the WS and ES lines are shown in Figs 30 and 31 for the fixed base case and the modal frequencies for the first seventy modes are summarized in Table 2.

	Moment connections between column and foundation	Pinned connections between column and foundation (i.e. as- built design details)
Mode Number	Modal Frequency (Hz)	Modal Frequency (HZ)
1	0.776	0.392
2	0.875	0.445
3	1.038	0.514
4	1.043	0.529
5	1.108 (1) [*]	0.566
6	1.121	0.631
7	1.247	0.707
8	1.304	0.715
9	1.332	0.950
10	1.345	1.004

TABLE 2.	Computed	frequencies fo	or the fi	rst seventy	modes of
the ES and	WS lines.				

	Moment connections between column and foundation Pinned connection between column a foundation (i.e. a built design detai	
Mode Number	Modal Frequency (Hz)	Modal Frequency (HZ)
11	1.365	1.067 (1) [*]
12	1.409	1.224
13	1.462	1.285
14	1.572 (2) [*]	1.332
15	1.684	1.361
16	1.713	1.386
17	1.849	1.593
18	1.860	1.622 (2) [*]
19	1.931	1.713
20	1.943	1.778
21	2.013	1.796
22	2.131	1.848
23	2.137	1.863
24	2.147	1.932
25	2.197	1.949
26	2.295	2.009
27	2.349	2.085
28	2.463	2.143
29	2.526	2.257
30	2.550	2.311
31	2.574	2.385
32	2.815	2.422
33	2.868	2.441
34	2.874	2.459
35	2.944	2.599
36	2.999	2.613
37	3.080	2.622
38	3.105	2.623
39	3.186	2.758
40	3.191	2.809
41	3.217	2.841
42	3.270	2.866 (3)*
43	3.304	2.883

TABLE 2. Computed frequencies for the first seventy modes of the ES and WS lines.

	Moment connections between column and foundation	Pinned connections between column and foundation (i.e. as- built design details)
Mode Number	Modal Frequency (Hz)	Modal Frequency (HZ)
44	3.368	2.886
45	3.594 (3) [*]	2.922
46	3.600	3.025
47	3.611 (4) [*]	3.059
48	3.704	3.076
49	3.735	3.136
50	3.858	3.252
51	3.883	3.258
52	3.924	3.301
53	3.967	3.303
54	4.016	3.374
55	4.017	3.449
56	4.074 (5) [*]	3.474 (4)*
57	4.115	3.482
58	4.180	3.511
59	4.236	3.526
60	4.327	3.539
61	4.391	3.560
62	4.402	3.586 (5)*
63	4.478	3.615
64	4.503	3.634
65	4.542	3.656
66	4.571	3.687
67	4.615	3.691
68	4.657	3.724
69	4.700	3.836
70	4.754	3.889

TABLE 2. Computed frequencies for the first seventy modes of the ES and WS lines.

*. Denotes model mode corresponding to experimentally measured mode (experimental mode number shown parenthetically)

As part of their evaluation of the WS and ES lines, Imbsen and Associates instrumented a short segment of the WS line (see inset in Fig. 32), and measured ambient vibrations of







FIGURE 31. Modeshapes 7-12 of the structural model (plan view).

the structure. Imbsen and Associates processed the ambient vibration data in the frequency domain to obtain estimates of the natural frequencies and modeshapes for this portion of the structure. Based on the limited information which was provided to LLNL by Caltrans, it appears that a detailed system identification modal analysis was not performed. Rather, modeshapes were determined by identification of peaks in the Fourier amplitude spectra of measured acceleration time histories.

The modeshapes determined experimentally by Imbsen and Associates are shown in Fig. 32. Figure 32 also shows the modeshapes from the test section portion of the structural model which most closely correspond to the experimentally determined modeshapes. The modeshapes from the moment-transferring base column model are shown in Fig. 32, and the frequencies corresponding to the pinned base column model are shown parenthetically.

The modeshapes corresponding to the first two measured modes were easily identified in the computational model results. The higher modeshapes, on the other hand, required more detailed inspection and interpretation because of a higher modal density in the high frequency range. It is noted that the fifth measured mode corresponds quite well to a strong mode which consists of predominately vertical motion, with second order horizon-tal motion. Imbsen and Associates appear to have associated the fifth measured mode with a transverse mode obtained from their modeling results. However, for the LLNL computational results the vertical mode shown in Fig. 32 appears to provide a better correlation.

The computational model results generally agreed well with the experimentally determined modeshapes, particularly in light of the fact that a very simple approach has been employed to extract modal information from the experimental data and there is a degree of uncertainty associated with both the computational model and the measured modeshapes. Based on inspection of the modeshapes and frequencies obtained from both the fixed base column model and the pinned base column model, the fixed base column model appeared to provide a somewhat better correlation with the measured data. The experimental modeshapes were determined from structural excitation which consisted of ambient vibration and vehicular traffic. At these low levels of excitation it would not be unexpected that the column to footing connection would appear more fixed than pinned.

The relationship between computed structural frequencies and the frequency content of the surface motion employed in the Caltrans design effort is shown in Fig. 33a. The structural frequencies plotted in Fig. 33 correspond to the model with moment connections between the columns and footings. The retrofit structure was of primary concern and foundation retrofits on a large number of columns were intended to emulate this connectivity. Figure 33a shows that the lower structural modes fall into the peak region on the spectra and thus the surface ground motion would tend to strongly excite the WS and ES line structures. Figure 33b shows the structure periods relative to the LLNL developed surface motion and the correlation between the lower modes of the structure and the dominant frequency of the ground motion is also evident for the LLNL motion.







4.0 Computer model of the retrofit WS and ES lines

4.1 The retrofit structure

The 24/580/980 Interchange was designed and constructed in the mid 1960's and therefore has many of the problematic concrete construction details of structures with 1960's vintage. As a result of these design problems, pre-1971 concrete bridge structures in California typically have low ductility capacity and are thus vulnerable to brittle catastrophic failure under strong earthquake excitation. Some of the major problem areas which have been identified for pre-1971 bridges through observed earthquake performance and research studies include (see Chai et. al. [3], Priestly and Seible [4]);

- 1. inadequate expansion joint seat dimensions to prevent separation of adjacent deck segments and loss of deck support
- 2. lack of top bending reinforcement and shear reinforcement in column footing mats leading to potential footing failures
- 3. inadequate shear strength of reinforced concrete columns (typically shear reinforcement utilized #4 bars at 12 inches regardless of column dimensions), poor shear reinforcement also limits flexural strength as outer concrete spalls and longitudinal bars buckle
- 4. poor connectivity between columns and footings as a result of utilization of weak lap splices between footing reinforcement and column longitudinal bars, leading to a potential for pulling out of the longitudinal column reinforcement from the footing and the inability to form a plastic hinge at the base of the columns
- 5. inadequate strength and stiffness of bent cap beams to ensure plastic hinge formation in columns
- 6. inadequate flexural strength of reinforced concrete columns as a result of low lateral force design coefficients
- 7. abutment failures as a result of pounding between the superstructure and abutment.

The as-built 24/580/980 interchange suffers from most of these inadequacies. In 1992 the expansion joints of the ES and WS lines were retrofit with cable or steel rod restrainers as discussed in section 3.1.2. This retrofit was part of Caltrans' state-wide Phase I seismic retrofit of bridges.

The other shortcomings have been addressed in the seismic retrofit design which was recently completed by Caltrans. The proposed retrofits include the strengthening of the columns with oval steel jackets as shown in Fig. 34. Based on research studies at UC San Diego [26], the steel jackets confine the concrete core of the column in a manner similar to modern spiral reinforcement, and greatly enhance the column ductilities. Based on scale-model experimental studies, the jackets also appear to solve the problem associated with pull-out of the lap splices in the column-to-footing connections.

The retrofit strategy also calls for extensive stiffening of bent cap beams. with the addition



FIGURE 34. Retrofit of columns with filled, oval steel jackets



FIGURE 35. Retrofit of bent cap beams with the addition of bolsters

of bolsters to the bent cap beams as indicated in Fig. 35. This will force plastic hinging into the columns as opposed to the bent caps, as required by Caltrans design methodology.

The retrofit design calls for retrofit of many of the column footings with the addition of concrete to confine the poorly reinforced existing footings, with micro piles to tie the footings to the ground (Fig. 36).



FIGURE 36. Retrofit of column footings.



FIGURE 37. Decoupling of ES and WS lines from the EN, C and SE lines.

The Caltrans retrofit design provides for complete physical decoupling of the WS and ES lines from the EN, C and SE lines (see Fig. 14 and Fig. 37). This results in a cleaner system from the structural dynamics standpoint, and eliminates the possibility of complex, three dimensional interactions between the WS and ES lines and the other segments of the interchange.

The other major feature of the retrofit design includes the enhancement of strength and stiffness of the three abutments of the WS and ES lines. At bent WS 75 two large, six foot



diameter drilled shaft concrete members were added as a retrofit (Fig. 38) and at abutment

FIGURE 38. Strengthening by addition of two stiff concrete members at WS 75.



FIGURE 39. Abutment strengthening at WS99 and ES1.

superstructure elements and foundations is summarized in Appendix D. to the end diaphragms of the bridges (see Fig. 39) The entire retrofit design for all of the ES1 and WS99 concrete "deadmans" were added with steel pipe attaching the deadmans

the retrofit features, is shown in Fig. 40. The final computer model of the WS and ES lines of the structure, which includes all of



4.1.1 Foundations and abutments

For the seismic analysis of the retrofit structure, the flexibility of the foundation system for each column, and the flexibility of the three abutments of the WS and ES lines, were accounted for in the structural model. In order to estimate the stiffnesses of the foundations and abutments, substructure models were constructed for ten selected foundations and for two abutment types. The ten foundation substructures were selected so as to be representative of all of the actual foundations throughout the two lines. The ten foundation types, designated A through J, are summarized in Table 3 and the correlation of the foun-

Foundation type	Characteristic bent	Description of characteristic footing
Α	ES1, WS99	abutment retrofit
В	WS76	P12 asbuilt
С	ES2	P23 retrofit
D	WS81	P20 retrofit
Е	WS77	P16 retrofit
F	WS89	P20 retrofit
G	WS85	P36 retrofit
Н	ES3	P41 retrofit
I	WS75	60" column
J	WS90	80" column

TABLE 3. Selected foundations used in determination of foundation compliances

dation type with each bent is summarized in Figure 41.

For each foundation type, a three dimensional substructure model was constructed and unit forces and moments were applied to the foundation mat in order to generate a six by six coupled flexibility matrix for the foundation system. The generated foundation flexibility matrix was then inverted to give a six by six stiffness matrix representation of the foundation stiffness (see Fig. 42). For the foundation substructure analyses, soil material properties were obtained from the *SHAKE* analysis results of Chen [8], thus the foundation stiffness characterizations can be considered an equivalent linear estimate of the strain level dependent foundation properties.

In the structural model of the WS and ES lines, the foundation stiffness matrix was attached to a foundation node, and the base of the corresponding columns were connected to the foundation node with the appropriate column-foundation mat connectivity (see Fig. 43). The column-foundation connectivity reflects the retrofit design in which many of the original pinned connections were upgraded to moment connections by jacketing, addition of concrete to the foundation mat and addition of pin piles at the footings. The idealized column-footing connectivities for all of the foundations of the retrofit structure are shown in Fig. 44.



FIGURE 41. Foundation stiffness characterizations.

Two substructure models were generated for the abutments of the WS and ES lines. One model was developed to represent the retrofit abutments at WS99 and ES1. At these abutments, concrete deadmans were designed with steel pipes connecting the deadmans to the existing bridge segments at the abutment diaphragms. The detailed abutment model is shown in Fig. 45b. This model was used in a load-displacement test to estimate representative spring constants for the abutment system.

The second abutment model, shown in Fig. 45a, was constructed for the existing WS75 abutment configuration. This abutment consisted of an end wall and wing walls. The WS 75 abutment was significantly different than the ES1 and WS99 abutments in that it is a seat type abutment, in which the bridgedeck can slide longitudinally relative to the abutment wall. This was represented in the structural model by inclusion of a contact surface between the end of the bridge and the abutment wall. The details of the finite element model representation of the abutments is illustrated in Fig. 46, and the abutment stiffness values are summarized in Table 4.

As a basis for comparison, Table 4 also shows the abutment stiffness values which are obtained from the simplified hand calculation procedures provided in the Caltrans Design Guide. The stiffnesses determined from the model calculations are in reasonable agreement with the Caltrans Design Guide stiffnesses. At WS75, two very large concrete drilled







FIGURE 43. Representation of foundation compliance in the superstructure model.

shafts were added to enhance the stiffness and capacity of the first frame which is adjacent to the abutment (see Fig. 38). The added shafts are so stiff that the actual load transferred to the abutment will be much smaller than would be the case for the as-built structure. In light of this, and the fact that the construction detail of the seat type abutment at WS75 would not support transfer of large transverse forces between the bridge superstructure and the abutment, the transverse stiffness provided by the abutment at WS75 was conservatively neglected and the concrete shafts were assumed to provide all of the transverse stiffness at the end of the bridge.

Abutment	Longitudir	al stiffness	Transverse stiffness	
	LLNL substructure model	Caltrans Design Guide procedure	LLNL substruc- ture model	Caltrans Design Guide procedure
WS75	8.7e6 lb/in	? 7e6 lb/in	(see note)*	(see note)
WS99/ES1	6.4e6 compression 2.3e6 tension	6.6e6 compression 1.5e6 tension	3.8e6	1.8e6

TABLE 4. Abutment stiffnesses for WS 75, WS99 and ES1









FIGURE 46. Abutment representation in the global finite element model.

*. In our judgement, the detail of the as-built connection between the abutment wall and the deck at WS75 would not provide sufficient strength to develop large transverse shear forces between the deck and the abutment at WS75. In the retrofit design, the massive drilled shafts at WS75 should attract nearly all of the transverse load at the abutment

4.1.2 Nonlinear concrete model

Under strong earthquake excitation, it is expected that many structures will undergo inelastic action. As long as the inelasticity is controlled and the behavior is ductile, the seismic performance of the inelastic structure can be quite good. Inelastic action can be a significant contributor to energy dissipation and can thus help mitigate the maximum force levels in the structure. Adequate structural ductility will also guard against sudden, brittle, explosive type failure associated with nonductile structures. On the other hand, the softening associated with inelastic action may also have less desirable effects which should be addressed. Inelastic action may result in increased structural displacements with a proportionate increase in secondary forces resulting from change of geometry of the structure (i.e. enhanced $P-\Delta$ effect from gravity dead load). Accurate computer simulation of the seismic response of a structure undergoing inelastic seismic deformations necessitates a nonlinear structural model which can adequately represent important nonlinear response features.

In concrete bridge structures, Caltrans' design methodology requires that inelastic action take place in the support columns rather than in the bent caps or deck structure. It is noted that this design philosophy is diametrically opposite to building design philosophy in which a weak-beam, strong-column philosophy prevails. Under extreme seismic events, concrete bridge columns such as those on the 24/580/980 interchange are expected to behave nonlinearly. In the current as-built configuration of the ES and WS lines, the columns lack significant ductility and would most likely fail at a relatively low loading as a result of pull-out of the column longitudinal steel from the footing, brittle fracture in high moment regions of the column because of poor confinement of the concrete core, or shear failure of the shorter columns near the abutments.

As evidenced by experimental tests at UC San Diego [26], steel jacketing of 1960's vintage concrete columns significantly improves the cyclic behavior of the columns and results in columns with enhanced ductility capacity. The extensive jacketing prescribed in the 24/580/980 retrofit design should significantly enhance the seismic performance of the concrete columns in the bridge system.

As ductile concrete columns deform laterally, the compressive gravity stresses in the column are overcome on the tension side of the column and a transverse cracked surface forms across a portion of the column cross section. As lateral displacements continue to increase, the cracked section will continue to propagate across the column, the longitudinal reinforcing steel will yield, and ultimately a plastic hinge will form in the highest moment region of the column. Formation of a plastic hinge in a column results in a drastic reduction in column stiffness with the potential for significant increase in structural displacements and redistribution of load within the structural system.

For the seismic analysis of the 25/580/580 interchange, a nonlinear reinforced concrete material model has been implemented in the *NIKE3D* finite element program. Following the work of Fillipou et. al. [27, 28, 29] the model employs the modified Kent-Park model [30] for the concrete compressive stress-strain behavior and the plasticity model of Menegotto and Pinto [31], for the characterization of the reinforcing steel.



FIGURE 47. Modified Kent - Park concrete compression model.

The concrete compressive model (see Fig. 47) accounts for softening in the concrete and the ultimate compressive strength and the softening slope are a function of the degree of concrete confinement. Poorly confined concrete is represented by a steep softening slope, well confined concrete is represented by a shallower softening slope (Fig. 47).

The concrete constitutive law for compression is governed by three regions of behavior, for $\varepsilon_c \leq \varepsilon_0$

$$\sigma_{c} = K f_{c}^{*} \left[2 \left(\frac{\varepsilon_{c}}{\varepsilon_{0}} \right) - \left(\frac{\varepsilon_{c}}{\varepsilon_{0}} \right)^{2} \right]$$
(EQ 1)

for $\varepsilon_0 \le \varepsilon_c \le \varepsilon_u$

$$\sigma_c = K f_c' \left[1 - Z(\varepsilon_c - \varepsilon_0) \right] \ge 0.2 K f_c'$$
(EQ 2)

for $\varepsilon_c \ge \varepsilon_u$

$$\sigma_c = 0.2K f_c^{\prime} \tag{EQ 3}$$

where

$$\varepsilon_0 = 0.002K \tag{EQ 4}$$

$$K = 1 + \frac{\rho_s f_{yh}}{f_c'} \tag{EQ 5}$$

For simple rectangular columns with horizontal ties shear reinforcement, an empirical relationship has been developed for the Z term. The expression is given by,

$$Z = \frac{0.5}{\frac{3 + 0.29f'_c}{145f'_c - 1000} + 0.75\rho_s \sqrt{\frac{h'}{s_h}} - 0.002K}$$
(EQ 6)

Unloading from the compression curve follows a straight line from the point at which unloading starts (e.g. at strain ε_r in Fig. 47) to a point on the axis denoted by ε_p where ε_p is given by the equations,

$$\frac{\varepsilon_p}{\varepsilon_0} = 0.145 \left(\frac{\varepsilon_r}{\varepsilon_0}\right)^2 + 0.13 \left(\frac{\varepsilon_r}{\varepsilon_0}\right)$$
(EQ 7)

when $\left(\frac{\varepsilon_r}{\varepsilon_0}\right) < 2$ and $\frac{\varepsilon_p}{\varepsilon_0} = 0.707 \left(\frac{\varepsilon_r}{\varepsilon_0} - 2\right) + 0.834$ (EQ 8) when $\left(\frac{\varepsilon_r}{\varepsilon_0}\right) \ge 2$

The existing material properties of the stack interchange are not well quantified. Caltrans did not perform coring samples, thus the existing concrete compressive strength is not precisely known. Significant concrete strengthening has certainly occurred since the 1960's when the structures were first built. In order to develop a representative set of material properties for the 1960's vintage 24/580/980 structure, the effect of continued concrete curing was taken into account. In addition, properties utilized in concrete jacketing tests at UC San Diego were considered (UC San Diego apparently chose properties which would be representative of existing vintage columns which are retrofit candidates), and concrete compressive strengths observed in coring samples from other bridges were considered (Maroney et. al. [32]). The influence of confinement on the effective ultimate compressive strength was also based on information gleaned from representative columns in the UC San Diego tests. The Z factors defining the slope of the concrete softening (Fig. 47) were estimated based on existing Z factors in the literature, and from existing formulas (EQ. 6) for the unjacketed portions of columns. The Z factors for well confined concrete in the jacketed portion of the existing columns and in the spirally reinforced new columns, were deduced by numerical experimentation where computational results were compared to actual tests of well confined, jacketed columns.

Because of uncertainties in the actual properties, two sets of analyses were performed, each with a different set of concrete properties. The properties used in the analyses are summarized in Table 5.

The reinforcing steel material model, which provides a reasonable representation of the Bauschinger effect, takes the form (see Taucher, Spacone and Filippou [29]),

$$\sigma^{n} = b \cdot \varepsilon^{n} + \frac{(1-b) \cdot \varepsilon^{n}}{(1+\varepsilon^{nR})^{\frac{1}{R}}}$$
(EQ 9)

$$\varepsilon^{n} = \frac{\varepsilon - \varepsilon_{r}}{\varepsilon_{o} - \varepsilon_{r}}$$
(EQ 10)

$$\sigma^{n} = \frac{\sigma - \sigma_{r}}{\sigma_{o} - \sigma_{r}}$$
(EQ 11)

This model provides the initial yield plateau typical of ductile steels upon first yield, and subsequently provides smoothed hysteresis loops for the saturated elasto-plastic behavior as shown in Fig. 48. This model provides good agreement with cyclic tests for reinforcing

	Material description	Effective concrete compressive strength	Reinforcing steel yield strength	
	Original concrete, unretrofit, poorly con- fined	6000 psi	45.7 ksi	
Matarial	(column core)			
Property	Original concrete, ret- rofit, well confined	7500 psi	45.7 ksi	
Set #1	(column core)			
	New retrofit concrete, well confined	7000 psi	68.0 ksi	
	(column core)			
	Original concrete, unretrofit, poorly con- fined	5000 psi	40.0 ksi	
Material				
Property	rofit, well confined	6500 psi	40.0 ksi	
Set #2	(column core)			
	New retrofit concrete, well confined	6000 psi	60.0 ksi	
	(column core)			

TABLE 5. Material property sets assumed for the seismic analyses

bars.

The nonlinear concrete and steel models were implemented in the *NIKE3D* finite element program fiber beam element. This element discretizes the column cross section into a number of user defined zones, with the uniaxial stress-strain behavior of each zone assigned the appropriate concrete or steel stress-strain law (see Fig. 49). An evaluation of the nonlinear concrete model was performed by comparison with a jacketed concrete col-



FIGURE 48. Menegotto-Pinto elastoplastic model for reinforcing bars.

umn test performed by Seible [26]. In a UC San Diego experiment, a partially jacketed scale model column was loaded cyclically up to displacement ductilities of 8. The test apparatus for the column test and the resulting force-displacement behavior is shown in Fig. 50. Based on the material properties supplied in the Seible study, a model of the concrete column was constructed with multiple beam elements representing both the confined and unconfined concrete regions. A comparison of the computed force-displacement relationship with the measured force-displacement relationship is shown in Fig. 51.

The correlation between computed and measured response is acceptable given the uncertainties in actual material properties. The computational model has appropriate pinching of the hysteresis loops and the energy loss per cycle, as defined by the area under the hysteresis loops, appears quite reasonable. The primary shortcoming of the nonlinear model is that the continued degradation of the loading stiffness with loading cycle is not very accurately reflected. Attempts to improve this aspect of the model by increasing the concrete softening behavior resulted in numerical difficulties. Future developments and improvements in the model will address this issue. In light of the reasonable comparison with experiment, the nonlinear concrete model was judged sufficiently accurate for the engineering evaluation of the 24/580/980 interchange.

The nonlinear fiber model requires definition of the column cross section for each column element which the model will be used for. In the global finite element model of WS and ES lines, a selected number of representative column cross sections were identified. The column cross sections are shown in Fig. 52 through Fig. 55 and the column section which applies to each bent is indicated in Table 6.

For each of the column cross section definitions, the column user defined integration points must be generated as input to the *NIKE3D* program. The global finite element model must update the stress at each user defined column cross section integration point at









FIGURE 50. Measured force - displacement behavior of a jacketed column from a UC San Diego experiment (Ref. 26).



FIGURE 51. Comparison of *NIKE3D* nonlinear concrete fiber element with experimental test of UC San Diego (column in Fig. 49).



Column section #1

DQ

0000

Column section #3

0

0





FIGURE 52. Representative column cross sections (sections 1-4).



<u>_ _ _ p _ _ d _ _ _ g _ _ _ g _ _ _ g _ _ g _ _ g _ _ g _</u> . . . 0 0 0 000 000 0 0 0 . . . 000 0 0 0

Column section #6

n

Column section #8

D

0 0

пр

۵ Column section #10

п

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8

g

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11

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ō ρ С



Column section #7



Column section #9

		0	
0			C
0			

0

Column section #12



FIGURE 53. Representative column cross sections (sections 5-12).



FIGURE 54. Representative column cross sections (sections 13-20).



FIGURE 55. Representative column cross sections (sections 21-26).

each of the three thousand or so time steps of the earthquake response computation. In addition, for post-processing, the strains at each user defined integration point were dumped into an output file so that the potential for concrete crushing could be evaluated for each column at each instant in time. This results in a very large database which must be dealt with. For the 24/580/980 interchange project, special software features were developed and implemented which allowed expedient generation of the column cross sections and automated evaluation of the voluminous output files. This automation of the generation and post processing made the actual time effort of the engineering analyst minimal.

Column section #	UDI set #	Associated bents
		WS97
		WS98
		ES2
1	56	ES3
		ES9
		ESI0 ES11
		ESTI
2	57	ES4
3	58	ES5 Right
4	59	ES5 Left (2)
5	60	ES6
6	61	ES7
		WS83
		WS84
		WS93
7	62	WS95
		WS96
		ES8
		ES12
8	63	WS75
9	64	WS76
10	65	WS77 middle
11	66	WS77 right
12	67	WS78
12	<u> </u>	WS79
15	00	WS81
14	69	WS80 left
15	70	WS80 right
16	71	WS85
10	/1	WS90
17	72	WS86 left
18	52	WS86 right (skewed)
19	73	WS87 left (new)
20	74	WS87 center
20		WS88
21	75	WS89
22	76	WS91 lower
23	77	WS91 upper
24	78	WS92

TABLE 6. User defined cross section integration (UDI) sets for representative columns.

•

Column section #	UDI set #	Associated bents
25	79	WS94
26	80	WS92 companion WS94 companion

. •

TABLE 6. User defined cross section integration (UDI) sets for representative columns.

4.1.3 Transient seismic response computations

The response of the ES and WS lines has been estimated for a moment magnitude 7.25 Hayward fault earthquake. The computations performed for the response estimates consisted of transient, nonlinear, time history solutions for thirty seconds of strong motion.

Two nonlinear finite element models were utilized in the response computations. The first computer model incorporated geometric nonlinearites including finite deformation effects, which allows for accurate representation of P- Δ influence on stresses and displacements, contact and impact at expansion hinges and one-way cable tensioning at the expansion hinges. The second nonlinear model included geometric nonlinearities, and material non-linearities were also included with the nonlinear beam fiber model for concrete columns. The sources of nonlinearity in the fully nonlinear model are summarized in Fig. 56.

For all of the computational analyses, Rayleigh mass and stiffness proportional damping was used to represent energy dissipation in the structure/foundation system. The damping representation is thus,

$$[C] = \alpha[K] + \lambda[M]$$
(EQ 12)

The damping was set to 5% critical at periods of one second and three-tenths of a second respectively as indicated in Fig. 57. The same damping was assigned for cases of linear and nonlinear concrete models. For the nonlinear concrete model, the hysteresis will augment the energy dissipation developed from the Rayleigh damping. Consideration was given to lowering the Rayleigh damping in the nonlinear concrete model, however for a structure undergoing strong shaking, it was felt that the effective damping will in all likelihood be quite high, and enhanced damping is not any less defensible than a lower damping value. Existing information on strong motion structural response is simply inadequate to evaluate effective damping in structures undergoing extreme nonlinear response.

All of the analyses which were performed utilized three components of input ground motion. A *Silicon Graphics* 8000 work station was the compute platform used for the seismic calculations and the nonlinear analyses for thirty seconds of earthquake motion required on the order of twenty five hours per run. A double precision version of the *NIKE3D* program was developed for the *Silicon Graphics* work station so that all computations could be performed in 64 bit arithmetic. Early attempts at running the highly nonlinear model in standard 32 bit arithmetic proved problematic in achieving convergence of the solution. The *NIKE3D* program utilizes a quasi-Newton solution scheme in which the tangent stiffness is updated economically without the full reformation of the stiffness associated with a classical full Newton solution algorithm. Time stepping was achieved with standard Newmark-Beta time integration. The transient analyses were performed at .02 second time steps which allowed resolution of frequencies of approx.mately 5 Hertz.

For all of the transient analyses, a complete database of response information (i.e. structural displacements, member force resultants, concrete and steel stresses at each user defined integration point) was generated which contained the response information for each time step. This resulted in an extremely large database of earthquake response information and special features were implemented in the *TAURUS* [33] post processing rou-


in the fully



FIGURE 57. Assignment of modal damping in the structural model with a mass and stiffness proportional damping matrix

tine in order to handle management of the large volume of information. In addition, special purpose software was developed to browse the *TAURUS* database and identify members in which concrete crushing was a possibility.

4.1.4 Seismic demands

The principal objective of the LLNL study was to provide Caltrans with an independent assessment of the seismic demands that a Hayward fault earthquake would place on the ES and WS lines of the 24/580/980 interchange. Caltrans has completed their own assessment of the member capacities and an independent evaluation of demands, obtained from the LLNL detailed nonlinear global model of the structure, provides Caltrans additional data for assessing demand to capacity ratios.

Caltrans engineers requested that the seismic demands on the structural columns be reported in terms of maximum seismic displacement at the top of the individual columns. The columns of the bridge model are supported on foundation matrices which allow for translation and rotation at the base of the column, and the displacements of a given column include rigid body components due to translation and rotation of the column base as shown in Fig. 58. Caltrans developed their displacement capacity information including the displacement due to the foundation and thus Caltrans requested that the displacement demands be reported with the bottom of column translation and rotation components included. The LLNL reporting of displacements would thus be based on total nodal dis-



FIGURE 58. Determination of deformational displacement demands for individual columns (single column bent, moment connection between column and footing).

placement relative to the input ground motion (i.e. displacement Δ_J in Fig. 58) rather than the true column deformational displacement (Δ_d in Fig. 58). Inspection of the LLNL finite element results indicates that displacements due to rigid body translation (Δ_{rt} in Fig. 58) are generally small to the point of being negligible, but the rigid body rotational displacements (Δ_{rt} in Fig. 58) are capable of significant contribution to the total displacement.

The nodal displacements in the finite element model are given in terms of global coordinate directions and thus it is necessary to resolve displacements into the local column directions. A post-processing feature was added to the *TAURUS* program to vectorially resolve global displacements into the column local coordinate systems. This required input defining the orientation of each column relative to the global coordinate system (i.e. an α for each column as indicated in Fig. 59). The top of column displacements were reported in the principal column coordinate directions, which for the most part are the transverse and longitudinal directions of the bridge.



FIGURE 59. Rotation from global axes to column local principal axes.

Multiple seismic response computations were carried out in order to determine the sensitivity of system response to a number of parameters. For each analysis, the maximum displacement which occurred at the top of each column was determined and written to a database. The first analysis set considered the nonlinear response of the structure in which geometric nonlinearities were included and material nonlinearity in the concrete was neglected. The analyses were based on Caltrans' definition of the surface earthquake ground motion. For this particular model idealization, two different modeling approaches were investigated for the concrete. In the first approach, the user defined integration beam element was employed in which linear material properties were assigned to the various concrete and steel integration points. The second approach treated the concrete as a linear material, but the column stiffnesses were based on a homogenous, uncracked rectangular cross section with an elastic modulus corresponding to the linear concrete modulus. A comparison of the two modeling approaches was developed in order to verify the accuracy of the sophisticated user defined fiber model for the simple case of linear concrete. The top of column displacements for these two modeling approaches are shown in Fig. 60 and Fig. 61¹. From the figures, it is observed that the fiber model is in good agreement with the gross section model. The maximum displacements occur between bents WS 81 and WS 89 where the column displacements approach 15 inches.

The second set of analyses considered the nonlinear response of the structure when the fully nonlinear concrete model was employed, and the ground motion was defined by the Caltrans motion. The top of column displacements from the computational model are summarized in Fig. 62 through Fig. 65. In these figures the nonlinear concrete results are compared to the linear concrete model in order to clearly show the effect of nonlinearity in the concrete. In addition, two different material property sets were considered (see section 4.1.2) so that the sensitivity of response to material properties could be judged. The fully nonlinear model results show that the concrete nonlinearity has a pronounced influence on the displacements of the structure. The column displacements in the trunk portion of the structure, between bents WS 75 and WS 82, show a significant increase in the longitudinal direction (which corresponds to the column "t" direction). In the transverse direction, the columns exhibit significant increases in displacements but the increases are spread throughout the structure and are not as limited to the trunk region. Top of column displacements for the nonlinear analysis with the Caltrans ground motions are tabularized in Table 7 and member stress resultants are tabularized in Table 8. The element stress resultants are reported for the top and bottom of each column as indicated in Fig. 70. The NIKE3D program provides stress resultants at the element center for the beam elements, and short beam elements were defined in the finite element model at the ends of the columns so that resultants would be obtained in the maximum moment regions. Top of column displacements for the nonlinear analysis with the LLNL ground motions are tabularized in Table 9.

A similar set of nonlinear analyses has been performed for the LLNL median earthquake motion and the results of these analyses are summarized in Fig. 66 through Fig. 69. Comparison of the nonlinear results with Caltrans and LLNL motions shows that the two hazard estimates are in reasonable agreement in terms of structural demands.

^{1.} For these two early linear runs, the connectivity at the top of the columns at multiple column bents WS 86, WS 89 and WS 91 assumed a moment connection between the columns and the bent cap. Subsequent runs utilized a pinned connection at the top of these columns to more accurately reflect the as-built detail.



FIGURE 60. Top of column s displacements for the WS and ES lines.



FIGURE 61. Top of column t displacements for the WS and ES lines.















FIGURE 65. Top of column t displacements for the WS and ES lines.







FIGURE 67. Top of column t displacements for the WS and ES lines.







FIGURE 69. Top of column s displacements for the WS and ES lines.



FIGURE 70. Column element orientation and local coordinate system. a) Element local coordinate system; b) orientation of elements in each bent model; c) Nike3d stress resultants at the element centroid.

Displacement demands Model node **Bent number** Column "t" Column "s" number Vector direction (in) direction(in) resultant (in) 2 WS 75 1.0636E+01 5.6968E+00 1.0636E+01 4 WS 75 1.0531E+01 5.6984E+00 1.0532E+01 6 WS 76 1.0699E+01 5.4088E+00 1.0705E+01 8 WS 76 1.0569E+01 5.4112E+00 1.0579E+01 **WS 77** 1.0647E+01 10 7.0261E+00 1.0675E+01 12 WS 77 1.0599E+01 7.0292E+00 1.0630E+01 14 WS 78 1.0631E+01 1.0422E+01 1.0634E+01 WS 78 1.3540E+01 1.0425E+01 16 1.3542E+01 18 WS 79 1.1588E+01 1.3664E+01 1.4453E+01 20 WS 79 1.4419E+01 1.3662E+01 1.5806E+01 22 WS 80 1.0391E+01 1.7994E+01 1.8527E+01 WS 80 1.7999E+01 24 1.2093E+01 1.8802E+01 26 WS 81 1.4300E+01 1.7231E+01 1.8678E+01 WS 81 1.3370E+01 1.7237E+01 28 1.8378E+01 30 WS 82 1.4524E+01 1.4024E+01 1.6459E+01 WS 82 1.3749E+01 1.4043E+01 32 1.5781E+01 34 WS 82 1.3104E+01 1.4069E+01 1.5399E+01 WS 83 1.3619E+01 1.0822E+01 36 1.4810E+01 WS 84 1.3736E+01 1.0399E+01 1.5740E+01 38 40 WS 85 1.1860E+01 1.6966E+01 1.7818E+01 1.2488E+01 2.2722E+01 42 WS 86 2.2397E+01 WS 86 1.0990E+01 44 2.2682E+01 2.2683E+01 46 WS 87 1.6528E+01 1.7268E+01 2.1279E+01 48 WS 87 1.5806E+01 1.7553E+01 2.1098E+01 WS 88 1.5610E+01 1.5057E+01 1.9720E+01 50 52 WS 89 1.4715E+01 1.3157E+01 1.9124E+01 54 1.5300E+01 1.3286E+01 1.9413E+01 WS 89 WS 90 9.0882E+00 1.3653E+01 56 1.4257E+01 WS 91 8.1807E+00 9.3796E+00 9.8191E+00 58 60 WS 91 7.8799E+00 9.6367E+00 9.6750E+00 62 WS 92 9.2312E+00 5.5413E+00 9.2359E+00 WS 92c 7.2324E+00 8.8779E+00 9.2316E+00 64

TABLE 7. Top of column displacements (relative to free-field ground motion) for the M_w =7.25 Hayward fault earthquake: Caltrans surface motion, *NIKE3D* model with geometric nonlinearities and the nonlinear concrete model (property set #2).

Madal nada		Displacement demands			
number	Bent number	Column "t" direction (in)	Column "s" direction(in)	Vector resultant (in)	
66	WS 92c	7.2246E+00	8.6440E+00	8.9855E+00	
68	WS 93	8.5483E+00	6.1226E+00	8.5689E+00	
70	WS 94	8.4632E+00	5.5853E+00	8.4661E+00	
72	WS 94c	5.9824E+00	8.4438E+00	8.4834E+00	
74	WS 94c	5.9141E+00	8.3833E+00	8.4083E+00	
76	WS 95	7.5971E+00	5.4901E+00	7.6097E+00	
78	WS 96	7.4032E+00	4.1263E+00	7.4108E+00	
80	WS 97	2.6758E+00	2.2685E+00	2.6826E+00	
82	WS 98	2.4160E+00	8.3789E-01	2.4297E+00	
84	ES 12	1.3568E+01	1.0587E+01	1.3952E+01	
86	ES 11	1.3093E+01	1.1951E+01	1.4901E+01	
88	ES 10	1.0472E+01	1.8543E+01	1.9680E+01	
90	ES 9	8.5595E+00	1.5648E+01	1.7048E+01	
92	ES 8	6.1991E+00	1.3101E+01	1.4121E+01	
94	ES 7	5.9048E+00	1.0124E+01	1.1209E+01	
- 96	ES 6	4.6588E+00	9.3842E+00	9.6458E+00	
98	ES 5	6.4746E+00	3.0552E+00	6.5013E+00	
100	ES 5	5.8711E+00	3.0566E+00	5.9020E+00	
102	ES 5	6.1885E+00	2.5688E+00	6.2834E+00	
104	ES 4	3.5391E+00	2.4702E+00	4.1319E+00	
106	ES 4	3.5498E+00	2.5908E+00	4.2273E+00	
108	ES 4	3.5605E+00	2.7065E+00	4.3219E+00	
110	ES 4	3.5713E+00	2.8242E+00	4.4209E+00	
112	ES 4	3.5830E+00	2.9658E+00	4.5231E+00	
114	ES 3	1.6688E+00	1.9725E+00	2.3548E+00	
116	ES 2	1.6638E+00	8.9142E-01	1.7892E+00	

TABLE 7. Top of column displacements (relative to free-field ground motion) for the M_w =7.25 Hayward fault earthquake: Caltrans surface motion, *NIKE3D* model with geometric nonlinearities and the nonlinear concrete model (property set #2).

TABLE 8. Column maximum stress resultants for the M _w = 7.25 Hayward fault earthquake:
Caltrans surface motion, NIKE3D model with geometric nonlinearities and the nonlinear concrete
model (property set #2).

	Element numbers	Maximum stress resultants					
Column description	bottom/ top	N (lb)	V _s (lb)	V _t (lb)	M _s (in-lb)	M _t (in-lb)	T (in-lb)
WS75 Compan-	3	8.9629E+05	3.7589E+05	5.8497E+05	7.2755E+07	1.1586E+08	9.1744E+05
ion Column 1	9	8.2481E+05	3.4280E+05	5.7697E+05	2.0568E+06	3.4581E+06	1.8890E+02
WS75 Compan-	10	9.3441E+05	3.6757E+05	5.7890E+05	7.4755E+07	1.1702E+08	9.0216E+05
ion Column 2	16	8.5423E+05	3.4876E+05	5.7624E+05	2.0886E+06	3.4545E+06	8.7339E+01
WS76 Column	37	1.2919E+06	2.3533E+05	2.6651E+05	1.4126E+06	1.5990E+06	9.7839E+01
1	43	1.2495E+06	1.9436E+05	2.4211E+05	7.7003E+07	9.0726E+07	7.7595E+05
	44	1.4920E+06	2.9368E+05	2.9149E+05	1.7528E+06	1.7445E+06	6.7648E+01
WS76 Column2	50	1.3783E+06	2.3728E+05	2.4481E+05	9.9241E+07	9.7777E+07	8.5004E+05
WS77 Column	59	3.0330E+06	1.2205E+06	1.3614E+06	2.5861E+08	2.9368E+08	1.3495E+07
2	65	3.0380E+06	1.1201E+06	1.3055E+06	2.5710E+08	2.9107E+08	1.3373E+07
WS77 Column	66	9.4184E+05	1.4119E+05	1.7981E+05	8.4717E+05	1.0816E+06	8.1735E+01
3	72	8.8476E+05	9.9948E+04	1.8520E+05	5.0197E+07	4.0233E+07	2.6883E+05
WS78 Column	81	1.4578E+06	2.5899E+05	2.1010E+05	1.5584E+06	1.2606E+06	4.1626E+01
1	87	1.3521E+06	2.2145E+05	3.3402E+05	1.1100E+08	8.8780E+07	6.4737E+05
WS78 Column	88	2.1938E+06	3.1790E+05	2.5750E+05	1.9074E+06	1.5447E+06	1.2211E+01
2	94	2.0985E+06	2.4391E+05	2.6988E+05	1.3742E+08	1.0690E+08	7.5300E+05
WS79 Column	103	2.4774E+06	2.9282E+05	2.7819E+05	1.7568E+06	1.6688E+06	1.5541E+02
1	109	2.3377E+06	2.3352E+05	2.4942E+05	1.5117E+08	1.0320E+08	1.1244E+06
WS79 Column	110	1.6429E+06	2.8706E+05	2.3342E+05	1.7222E+06	1.4006E+06	3.8402E+01
2	116	1.4836E+06	2.2827E+05	2.4661E+05	1.4498E+08	8.4404E+07	9.9469E+05
WS80 Column	126	1.4176E+06	2.8576E+05	1.9492E+05	1.7151E+06	1.1692E+06	7.4993E+02
1	132	1.2560E+06	2.2862E+05	2.4549E+05	1.3911E+08	5.9814E+07	8.1712E+05
WS80 Column	133	2.8054E+06	3.9005E+05	1.8793E+05	2.3468E+06	1.1278E+06	1.5688E+02
2	139	2.5103E+06	3.6574E+05	2.9400E+05	2.1212E+08	7.7726E+07	1.7275E+06
WS81 Column	148	1.5717E+06	2.6323E+05	2.1619E+05	1.5762E+06	1.2968E+06	1.4770E+02
1	154	1.4730E+06	2.1618E+05	2.3508E+05	1.4934E+08	8.7394E+07	1.3055E+06
WS81 Column	155	3.0184E+06	2.5318E+05	1.8908E+05	1.5186E+06	1.1347E+06	6.5185E+01
2	161	2.7289E+06	2.3730E+05	2.5306E+05	1.4473E+08	8.5412E+07	8.6845E+05
WS82 Column	176	1,9008E+06	1.7060E+05	1.7680E+05	1.0238E+06	1.0608E+06	1.3364E+02
1	182	1.6796E+06	1.9446E+05	2.3603E+05	8.2544E+07	5.9068E+07	4.8643E+05
WS82 Column	183	1.4084E+06	1.6001E+05	1.7785E+05	9.6010E+05	1.0638E+06	4.8258E+01
2	189	1.1958E+06	1.6646E+05	1.8039E+05	7.4051E+07	5.8388E+07	4.2750E+05
WS82 Column	190	2.6961E+06	1.7822E+05	1.9236E+05	1.0528E+06	1.1385E+06	3.0091E+02
3	196	2.4544E+06	1.5084E+05	2.2575E+05	9.6193E+07	5.1162E+07	2.8454E+05
WS83 Column	213	2.3145E+06	6.4468E+05	3.8763E+05	2.5435E+08	9.2540E+07	1.0347E+07
1	219	1.5655E+06	5.5904E+05	3.9616E+05	2.2360E+08	7.6998E+07	9.7749E+06
WS84 Column	227	2.6160E+06	5.4877E+05	3.8459E+05	2.3432E+08	9.3360E+07	9.6477E+06
1	233	1.6054E+06	4.2583E+05	3.0579E+05	1.7448E+08	8.1244E+07	8.6548E+06
WS85 Column	241	2.8983E+06	1.4629E+06	7.7961E+05	7.8949E+08	2.1787E+08	5.0353E+07
1	247	1.4511E+06	1.2343E+06	4.9384E+05	6.0778E+08	1.8970E+08	4.8272E+07

TABLE 8. Column maximum stress resultants for the $M_w = 7.25$ Hayward fault earthquake: Caltrans surface motion, NIKE3D model with geometric nonlinearities and the nonlinear concrete model (property set #2).

	Element numbers	Maximum stress resultants					
Column description	bottom/ top	N (lb)	V _s (lb)	V _t (lb)	M _s (in-lb)	M _t (in-lb)	T (in-lb)
WS86 Column	255	1.0124E+07	7.8895E+05	6.0189E+05	1.4863E+08	9.1949E+07	2.0651E+05
1	261	4.7418E+06	2.2184E+06	1.8655E+06	2.6762E+07	1.9536E+07	1.2950E+05
WS86 Column	262	2.0924E+06	4.1046E+05	3.4865E+05	2.1587E+08	1.0667E+08	1.1674E+06
2	268	3.5133E+06	6.4954E+05	3.3778E+05	4.5121E+06	5.0957E+06	2.2516E+03
WS87 Column	280	2.1074E+06	4.4995E+05	4.7383E+05	1.3515E+08	1.7799E+08	8.1230E+06
1(new to left)	286	1.8396E+06	3.8594E+05	2.7006E+05	1.7413E+08	1.3994E+08	8.3960E+06
WS87 Column	287	3.4047E+06	9.5161E+05	4.2995E+05	4.1184E+08	1.7041E+08	2.1826E+07
2	293	2.7848E+06	7.1242E+05	2.6400E+05	3.6209E+08	1.5090E+08	2.2374E+07
WS88 Column	302	2.3738E+06	9.0786E+05	4.7538E+05	4.7242E+08	1.4685E+08	2.2214E+07
1	308	1.6910E+06	6.8982E+05	3.2861E+05	4.0381E+08	1.3960E+08	2.2683E+07
WS89 Column	316	2.4427E+06	2.2800E+05	1.8769E+05	8.0836E+07	5.9492E+07	2.5340E+05
1	328	1.9638E+06	1.3715E+05	1.2755E+05	8.2284E+05	7.6527E+05	9.0518E+01
WS89 Column	329	1.0412E+06	1.6067E+05	3.0934E+05	6.0276E+07	5.0680E+07	1.8991E+05
2	341	7.5361E+05	1.1103E+05	1.6899E+05	2.4673E+06	3.7366E+06	6.2305E+02
WS90 Column	351	2.7453E+06	1.4329E+06	5.8448E+05	7.4455E+08	1.8864E+08	3.6842E+07
1	357	1.4781E+06	9.7442E+05	4.5895E+05	5.1473E+08	1.6680E+08	3.5031E+07
WS91 Column	365	1.9856E+06	5.9548E+05	4.6649E+05	2.7325E+08	2.6645E+08	4.1044E+05
1	377	1.3252E+06	3.6273E+05	3.9426E+05	2.1763E+06	2.3655E+06	1.3172E+02
WS91 Column	378	1.8596E+06	6.6297E+05	5.1323E+05	2.9464E+08	2.4875E+08	6.4594E+05
2	390	1.1198E+06	5.0085E+05	3.7405E+05	3.0052E+06	5.2480E+06	2.9810E+02
WS92 Column	401	2.7321E+06	1.6040E+06	5.4327E+05	6.8770E+08	2.0553E+07	6.4069E+07
1	407	1.9764E+06	1.3652E+06	5.0866E+05	4.5400E+08	1.9974E+08	6.3967E+07
WS92 Compan-	415	2.2332E+06	4.1539E+05	2.9903E+05	1.4222E+08	1.1685E+08	1.0191E+07
ion Column 1	421	1.9406E+06	3.3876E+05	2.7818E+05	1.3672E+08	1.3956E+07	1.0110E+07
WS92 Compan-	422	3.2667E+06	4.6807E+05	2.6378E+05	1.5097E+08	1.3560E+08	1.0332E+07
ion Column 2	428	2.9965E+06	3.3105E+05	2.7187E+05	1.3542E+08	1.5211E+07	1.0341E+07
WS93 Column	435	2.1940E+06	6.8982E+05	4.5845E+05	2.4733E+08	8.6552E+07	4.6315E+06
1	441	1.8178E+06	5.1401E+05	3.5472E+05	1.7301E+08	8.9111E+07	4.7058E+06
WS94 Column	449	2.6790E+06	1.2278E+06	5.4415E+05	5.2776E+08	2.0736E+07	1.5656E+07
1	455	1.8374E+06	9.2714E+05	5.0472E+05	3.1302E+08	1.5408E+08	1.5521E+07
WS94 Compan-	463	4.4002E+06	4.2366E+05	2.8265E+05	1.5026E+08	1.2409E+08	3.6652E+06
ion Column 1	469	3.9526E+06	3.0163E+05	3.3940E+05	1.1011E+08	1.5962E+07	3.6891E+06
WS94 Compan-	470	1.7942E+06	3.7854E+05	3.4778E+05	1.3419E+08	1.2973E+08	3.7461E+06
ion Column 2	476	1.8525E+06	3.0138E+05	2.7532E+05	1.1538E+08	1.4607E+07	3.7656E+06
WS95 Column	484	2.7328E+06	6.7563E+05	5.0059E+05	2.3425E+08	9625E+07	3.8231E+06
1	490	1.7888E+06	5.3525E+05	6.2876E+05	1.6577E+08	9.3687E+07	3.3428E+06
WS96 Column	498	4.8312E+06	7.1389E+05	7.1014E+05	2.1355E+08	9.3045E+07	4.9784E+06
1	504	3.9286E+06	5.4115E+05	8.2587E+05	1.5269E+08	8.9423E+07	4.9663E+06
WS97 Column	512	7.0329E+06	6.0336E+05	5.6408E+05	1.6213E+08	6.4877E+07	4.4426E+06
1	518	1.6379E+07	5.7131E+05	6.1634E+05	2.1317E+08	8.2460E+07	4.2607E+06

TABLE 8. Column maximum stress resultants for the $M_w = 7.25$ Hayward fault earthquake: Caltrans surface motion, *NIKE3D* model with geometric nonlinearities and the nonlinear concrete model (property set #2).

	Element numbers	Maximum stress resultants					
Column description	bottom/ top	N (lb)	V _s (lb)	V _t (lb)	M _s (in-lb)	M _t (in-lb)	T (in-lb)
WS98 Column	526	1.3729E+07	3.5120E+05	8.0774E+05	1.7260E+08	1.7147E+08	3.5949E+06
1	532	1.9391E+07	5.7772E+05	1.1379E+06	1.3430E+08	1.0062E+08	3.5843E+06
ES12 Column 1	1030	2.0205E+06	7.2669E+05	3.8155E+05	2.6656E+08	8.9795E+07	2.1193E+07
ES12 Column 1	1036	1.4860E+06	6.3440E+05	4.2517E+05	2.2631E+08	8.1797E+07	2.1136E+07
ES11 Column 1	1044	2.7158E+06	7.0462E+05	4.7189E+05	2.1752E+08	7.7422E+07	1.3701E+07
ESTI Column I	1050	1.7952E+06	5.4528E+05	3.5940E+05	1.7997E+08	7.4451E+07	1.4161E+07
ES10 Column 1	1058	4.3743E+06	8.8104E+05	5.9587E+05	2.3401E+08	7.0143E+07	8.5051E+06
ESTO Column 1	1064	3.9872E+06	6.5676E+05	4.5596E+05	2.7767E+08	6.5205E+07	9.1897E+06
ECO Column 1	1072	2.5066E+06	9.0479E+05	3.8156E+05	2.2357E+08	8.0013E+07	1.0416E+07
ES9 Column I	1078	1.9812E+06	5.9546E+05	5.8073E+05	1.8288E+08	6.7903E+07	1.0771E+07
	1086	1.8840E+06	8.2949E+05	4.0405E+05	2.6389E+08	7.6296E+07	1.2488E+07
ES8 Column I	1092	1.4560E+06	6.4568E+05	4.4058E+05	2.1696E+08	7.4548E+07	1.3382E+07
	1100	2.0948E+06	1.6210E+06	4.2360E+05	5.9260E+08	8.2413E+06	3.7160E+07
ES7 Column 1	1106	1.4841E+06	1.4124E+06	2.9687E+05	4.5333E+08	1.2130E+08	3.7167E+07
	1114	2.9330E+06	1.4082E+06	8.1499E+05	4.1332E+08	1.9639E+08	2.1707E+07
ES6 Column 1	1120	2.1529E+06	1.2352E+06	5.6442E+05	4.4104E+08	1.5924E+08	2.1654E+07
ES5 Column 1a	1128	8.9889E+05	3.6903E+05	2.8359E+05	6.7792E+07	5.1127E+07	2.7988E+06
(Yoke)	1134	7.6960E+05	3.2535E+05	2.2029E+05	6.8268E+07	5.0267E+07	2.7634E+06
ES5 Column 1b	1135	1.0939E+06	4.0750E+05	3.9020E+05	7.4845E+07	5.9791E+07	2.7954E+06
(Yoke)	1141	9.8315E+05	3.4320E+05	3.2632E+05	8.0718E+07	5.2451E+07	2.7867E+06
	1142	2.2447E+06	1.1127E+06	5.6517E+05	2.1636E+08	9.4647E+07	9.5313E+06
ESS Column 2	1148	2.0544E+06	1.0430E+06	4.7010E+05	2.2437E+08	1.0221E+08	9.5219E+06
	1167	5.3027E+05	1.1430E+05	9.9125E+04	1.6354E+07	1.2462E+07	4.4378E+05
ES4 Column I	1173	4.9739E+05	1.0647E+05	9.8966E+04	1.6285E+07	1.1617E+07	4.3892E+05
	1174	3.9480E+05	1.0441E+05	9.0911E+04	1.4570E+07	1.1724E+07	4.3696E+05
ES4 Column 2	1180	3.5279E+05	9.5325E+04	8.2873E+04	1.4610E+07	1.1550E+07	4.2759E+05
E94 Q-1	1181	3.0550E+05	1.0506E+05	9.9766E+04	1.4849E+07	1.2886E+07	4.3203E+05
ES4 Column 3	1187	2.6588E+05	9.5633E+04	7.7130E+04	1.4292E+07	1.3057E+07	4.2035E+05
F84 G 1	1188	4.4294E+05	1.1363E+05	1.0479E+05	1.5545E+07	1.4221E+07	4.2662E+05
ES4 Column 4	11 94	4.0696E+05	9.9253E+04	8.4748E+04	1.5446E+07	1.4281E+07	4.1532E+05
EQ4 Column 5	1195	5.8751E+05	1.1793E+05	1.1744E+05	1.6546E+07	1.5826E+07	4.2168E+05
ES4 Column 5	1201	5.4576E+05	1.0477E+05	9.5123E+04	1.6869E+07	1.6198E+07	4.0593E+05
F02 G 1	1213	1.6292E+06	1.0185E+06	3.5344E+05	1.6738E+08	5.5285E+07	6.9291E+06
ES3 Column I	1219	1.3514E+06	9.4638E+05	2.9298E+05	1.4099E+08	5.1471E+07	6.8586E+06
	1227	9,9198E+06	6.7809E+05	4.9053E+05	1.1401E+08	6.0417E+07	5.5970E+06
ES2 Column 1	1233	1.0111E+07	5.8097E+05	4.3491E+05	8.2048E+07	5.2304E+07	5.6149E+06

TABLE 9. Top of column displacements (relative to free-field ground motion) for the M_w =7.25 Hayward fault earthquake: LLNL surface motion, *NIKE3D* model with geometric nonlinearities and the nonlinear concrete model (property set #2).

		Displacement demands			
number	Bent number	Column "t" direction (in)	Column "s" direction(in)		
2	WS 75	14.465	5.3755		
4	WS 75	14.266	5.3727		
6	WS 76	14.561	4.6151		
8	WS 76	14.299	4.6170		
10	WS 77	14.451	6.1850		
12	WS 77	14.268	6.1884		
14	WS 78	15.168	10.072		
16	WS 78	16.060	10.079		
18	WS 79	15.482	14.701		
20	WS 79	16.402	14.708		
22	WS 80	15.050	21.819		
24	WS 80	15.674	21.820		
26	WS 81	17.132	19.431		
28	WS 81	16.625	19.435		
30	WS 82	17.175	14.324		
32	WS 82	16.828	14.341		
34	WS 82	16.517	14.367		
36	WS 83	16.738	9.9515		
38	WS 84	16.804	10.161		
40	WS 85	16.591	13.887		
42	WS 86	16.646	18.729		
44	WS 86	17.575	18.889		
46	WS 87	16.134	19.146		
48	WS 87	18.816	16.743		
50	WS 88	16.207	18.721		
52	WS 89	16.170	17.865		
54	WS 89	16.370	17.921		
56	WS 90	11.906	12.864		
58	WS 91	13.156	8.8872		
60	WS 91	11.114	8.8999		
62	WS 92	11.307	7.2438		
64	WS 92c	9.0215	10.260		
66	WS 92c	8.9785	9.9731		

TABLE 9. Top of column displacements (relative to free-field ground motion) for the M_w =7.25 Hayward fault earthquake: LLNL surface motion, *NIKE3D* model with geometric nonlinearities and the nonlinear concrete model (property set #2).

Madel node		Displacement demands			
number	Bent number	Column "t" direction (in)	Column "s" direction(in)		
68	WS 93	9.7319	6.9775		
70	WS 94	9.4456	6.1278		
72	WS 94c	6.8145	9.3418		
74	WS 94c	6.7441	9.1943		
76	WS 95	8.4618	4.5918		
78	WS 96	8.1674	3.1824		
80	WS 97	3.2997	2.0074		
82	WS 98	2.8525	0.87305		
84	ES 12	16.102	8.9774		
86	ES 11	13.810	11.900		
88	ES 10	10.722	15.092		
90	ES 9	8.6418	13.650		
92	ES 8	6.2175	11.269		
94	ES 7	5.2702	9.8404		
96	ES 6	4.2175	9.5408		
98	ES 5	6.0957	2.6235		
100	ES 5	5.4375	2.6274		
102	ES 5	5.7959	2.3945		
104	ES 4	3.1445	2.3833		
106	ES 4	3.1563	2.4146		
108	ES 4	3.1670	2.4448		
110	ES 4	3.1777	2.4761		
112	ES 4	3.1885	2.5083		
114	ES 3	1.3582	1.5343		
116	ES 2	1.1829	0.63207		

4.1.5 Capacities and demand/capacity ratios

In order to provide a basis for comparison of their own capacity determinations, Caltrans requested that LLNL perform capacity calculations for three selected bents of the structure. The bents which Caltrans requested capacity information on included ES 4, the WS 94 companion bent and WS 96 (see Fig. 71). A simple monotonic push-over analysis was performed in order to determine the nonlinear response of each bent in the longitudinal and transverse directions. Per Caltrans' request, the push over computations included the displacements due to foundation flexibility.

The transverse and longitudinal responses of the three bents are shown in Fig. 72 through Fig. 74. For each bent, displacements were imposed at the top of the bent as indicated in Fig. 71, and the shear force at the top of a selected column was plotted as a function of transverse displacement. On each plot, displacement ductilities are labeled and, where applicable, the displacement at first concrete crush is noted. Concrete crush is identified when the concrete compressive strain reaches .005 at any point in the column for poorly confined concrete and at a strain of .015 for well confined concrete [35].

Using jacketed column tests performed at UC San Diego as general guidance, significant deterioration of stiffness might be expected when displacement ductilities reach the level of six or seven. Thus a displacement ductility of six was assumed as an upper bound capacity for well confined columns, unless of course concrete crushing sets in prior to achieving this level of displacement ductility.

The allowable ductilities for the columns in each bent are indicated with bold numbers in Fig. 72 to Fig. 74. For the new columns in the ES 4 bent and the WS 94 companion bent, the allowable displacements are controlled by concrete crushing. The grade 60 reinforcing steel in the newer columns leads to greater compression demands in the concrete and concrete compression failure becomes more critical. The retrofit WS 96 column does not experience concrete crushing prior to achieving a displacement ductility of six.

It must be noted that assessing concrete column capacities with a simple push over test has some serious limitations. First, the columns undergo significant biaxial behavior when the structure is subjected to earthquake ground motions. The interaction between directional responses, which will tend to superpose in an additive fashion in some quadrant of the column, is not addressed with uniaxial capacity information. Second, the boundary conditions which exist at the bottom and top of an actual bridge column are a function of the displacements and deformations of the entire frame to which the given column is attached and the curvature of the columns obtained in a simple push over test may not be representative of the curvature distribution in the actual bridge column. This would be particularly true for the single column bents and multiple column bents in the longitudinal direction because the rest of the frame will provide rotation restraint at the top of these columns, and this is not accounted for in the simple push over computations.

With these caveats in mind, a rough, first order check of demand to capacity can be made for these selected columns. Figure 75 and Fig. 76 show the column capacities estimated



FIGURE 71. Capacity evaluation models for bents ES4, WS94 (companion) and WS96.

from the simple push over calculations compared to the column demands. For the selected columns the capacities exceed demands by a good margin.

In an attempt to provide a more rational evaluation of concrete capacity and demand estimates, a post processing procedure was developed to scan all of the concrete compressive strains in each column of the WS and ES lines at each instant of time throughout the earthquake response. The search was made to determine if concrete crushing was occurring in any of the columns. In the well confined portion of the retrofit columns, the allowable concrete compressive strain was taken as .015, in the poorly confined unretrofit columns the allowable compressive strain was taken as .005 and in the new concrete columns and drilled shafts the compressive strain was taken as .015. It is noted that inspection of the actual column strains from the global model response computations fully accounts for biaxial effects on concrete strains and the appropriate column boundary conditions are represented at each instant of time.

A plot of the ratio of maximum concrete compressive strain to the allowable concrete compressive strain is shown in Fig. 77 for the Caltrans ground motion hazard and in Fig. 78 for the LLNL ground motion response. The columns for which demand exceeds capacity are highlighted with the striped bar. Both ground motions indicated problems in the ES line near the ES line to WS line juncture. In particular, the single columns bents ES 9, ES 10 and ES 12 exhibit potential failure in the top portion of the columns. Both ground motion sets also indicated problems in Frame #1 at the very trunk of the structure.



FIGURE 72. Bent ES4 column shear-displacement. a) Transverse direction; b) longitudinal direction.



FIGURE 73. Bent WS94 (companion) column shear-displacement. a) Transverse direction; b) longitudinal direction.



FIGURE 74. Bent WS96 (companion) column shear-displacement. a) Transverse direction; b) longitudinal direction.



FIGURE 75. Displacement demands and capacities for selected bents (transverse direction).







FIGURE 77. Demand to capacity ratio for concrete compressive strains (Caltrans ground motion)



FIGURE 78. Demand to capacity ratio for concrete compressive strains (LLNL ground motion)

5.0 Summary of results and observations

A seismic response study has been completed for the ES and WS lines of the 24/580/980 interchange in Oakland California. As stipulated by Caltrans, the LLNL work focused on the estimation of the structural demands which would be placed on this structure as a result of a Hayward Fault earthquake. As requested by Caltrans, the fundamental measure of structural demands was expressed in terms of maximum displacements at the top of each column of the structure. The displacement demands computed using both Caltrans and LLNL median surface ground motions are summarized in Fig. 79.



FIGURE 79. Column displacement demands based on Caltrans and LLNL median motions.

LLNL seismologists and geotechnical engineers developed an independent estimation of the ground motion at this site which would result from a $M_w = 7.5$ Hayward Fault earthquake. Based on the Caltrans policy decision to use median level motion for this structure, the LLNL ground motion was based on the median level obtained from a suite of 100 possible Hayward Fault earthquakes. The LLNL median motion was in reasonable concurrence with the Caltrans ground motion definition.

Nonlinear, transient, earthquake response computations have been completed using a three dimensional nonlinear finite element model of the WS and ES lines. The nonlinear model accounted for potential impact and restrainer tensioning at expansion joints, finite deformation with accurate representation of associated P- Δ effects, and nonlinear hysteretic behavior of the concrete columns with softening of the concrete and plastic yielding of the reinforcing bars. Response computations have been completed for both Caltrans and LLNL ground motions.

The computed displacement demands for the columns were estimated to be on the order of two feet for the tallest columns in the structure. The concrete nonlinearity was found to have a pronounced effect on the global displacements of the structure, particularly near the trunk of the bridge system and in the ES line near the structure junction as indicated in Fig. 80. In the trunk region, the longitudinal displacements increased by more than a factor



FIGURE 80. Regions in which concrete nonlinearity has a pronounced influence on structural displacements.

of two when the nonlinearity of the concrete was included.

As requested by Caltrans, simple nonlinear, static push over analyses were performed for three selected bents (ES 4, WS 94 companion bent and WS 96). The displacement capacities estimated from the push over analyses were found to exceed the displacement demands on these bents by a comfortable margin. However, a more rigorous and thorough investigation of column demands pointed to some potential problem locations for the retrofit structure. By extensive post processing of the response history database, the concrete strains in all of the bridge columns were assessed at each instant of the earthquake response and compared to appropriate allowables for poor or well confined concrete. This check illustrated that significant overstressing problems exist in the top of some of the tall single column bents on the ES lines (ES 9, ES 10 and ES 12). Marginal overstressing problems are also evident in the very end of the trunk at WS 75, and WS 77 with the ground Caltrans ground motion characterization, and significant overstressing of the WS 75 WS 76 and WS 77 columns was observed with the LLNL median motion. Both ground motion characterizations indicated overstressing in the column of bent WS 85.

Many of the overstressing problems could be addressed with additional column jacketing. For example, if column WS 85 was jacketed at the base, and Columns ES8, ES9, ES10 and ES12 were jacketed through full height, the problems in these columns would be mitigated. Figure 81 and Fig. 82 show an approximation to the compressive strain demand to capacity ratios for the existing retrofit and for a retrofit which includes the additional jacketing. The plots of Fig. 81b and Fig. 82b are approximate in that a complete reanalysis of the structure was not performed, the plots were simply obtained by utilizing the same demand and increasing the strain capacity by a factor of three to reflect the effect of steel jacket confinement. There would be additional strength of the columns as a result of the jacketing, however the change in displacement demands as a result of the jacketing should be small and the plots of Fig. 81b and Fig. 82b are felt to provide a good estimation of the strain demand to capacity when additional jackets are added. Figures 81b and 82b indicate that the specified jacketing potentially solves of number of the indicated problems.

The problems associated with WS 75 and WS 77 are more fundamental and cannot be fixed with additional jacketing. Based on the results presented here, the drilled shafts at bent WS 75 and the columns of bent WS 77 appear to be susceptible to crushing failure of the concrete. Since the concrete of these members is already well confined, these members would require a different mitigation technique. One potential option consists of increasing the member dimensions of the drilled shafts in order to lower the member stresses.

The current retrofit design does not provide for any column retrofit for the multiple column bents of Frame #2 and Frame #3 (see Fig. 83). For these two frames, it is our opinion that careful consideration should be given to the overall frame shear capacity. Although an evaluation of shear capacity to demand was beyond the scope of the LLNL effort, and Caltrans has apparently assessed the adequate of the shear capacity of the columns [34], the shear capacity of the column-to-footing pinned connections on Frame #2 and Frame #3 does not appear to be well quantifiable. There is some research available on the shear strength of pinned connections for circular columns [36], however there seems to be a lack of information for larger rectangular columns. Based on the information available to LLNL there appears to be a significant degree of uncertainty about potential failure modes and strength capacity of these connections. Caltrans may want to consider additional retrofit schemes for the connections in light of the relative uncertainty in the capacity of these connections

Finally, based on the work of Hutchings et. al. [7], it must be noted that the possibility exists that this interchange could be subjected to motion significantly larger than the median level design basis earthquake. Caltrans may want to consider the implications of a beyond design basis event for this structure. Particularly in light of the fact that this site is situated within 4 Km of the fault and the probability of a major earthquake on the Hayward fault is continually being revised upward.


FIGURE 81. Column compressive strain demand to capacity ratios. a) existing retrofit design; b) estimation for modified retrofit design.



FIGURE 82. Column compressive strain demand to capacity ratios. a) existing retrofit design; b) estimation for modified retrofit design.



FIGURE 83. Location of Frames 1, 2 &3.

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Deck Section	Deck cross-section number	Nike material number	Nike user defined integration number
WSDI	7	105	1
WSD2	6	106	2
WSD3(a)	5 (8)	107 (108)	3 (4)
WSD4	4	109	5
WSD5	3	110	6
WSD6(a)	2 (9)	112(111)	8 (7)
WSD7	1	113	9
WSD8(a)	1 (10)	114 (115)	10 (11)
WSD9	1	116	12
WSD10	1	117	13
WSD11(a)	1 (1)	118 (119)	14 (15)
WSD12	1	120	16
WSD13	1	121	17
WSD14	1	122	18
WSD15(a)	1 (10)	124 (123)	20 (19)
WSD16	1	125	21
WSD17	1	126	22
WSD18(a)	1 (11)	128 (127)	24 (23)
WSD19	1	129	25
WSD20(a)	1 (11)	131 (130)	27 (26)
WSD21	1	132	28
WSD22(a)	1 (10)	134 (133)	30 (29)
WSD23	1	135	31
WSD24	1	136	32
ESDI	1	137	33
ESD2(a)	1 (10)	138 (139)	34 (35)
ESD3	1	140	36
ESD4(a)	1 (10)	141 (142)	37 (38)
ESD5	1	143	39
ESD6(a)	1 (10)	144 (145)	40 (41)
ESD7	1	146	42
ESD8	1	147	43
ESD9(a)	1 (13)	149 (148)	45 (44)
ESD10	1	150	46
ESD11(a)	1 (12)	152 (151)	48 (47)
ESD12	1	153	49
ESD13	1	154	50

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Deck Section	Cross-Sectional Area (in2)	Length (ft)
WSD1	9275	80.8
WSD2	9549	97.2
WSD3	10220	97.1
WSD4	10750	97.2
WSD5	11700	97.2
WSD6	12230	97.1
WSD7	6593	97.1
WSD8	6593	97.1
WSD9	6593	98.3
WSD10	6593	99.1
WSD11	6593	85.7
WSD12	6593	88.6
WSD13	6593	69.5
WSD14	6593	69.9
WSD15	6593	96.3
WSD16	6593	99.4
WSD17	6593	112.0
WSD18	6593	118.5
WSD19	6593	117.3
WSD20	6593	117.3
WSD21	6593	115.6
WSD22	6593	96.1
WSD23	6593	96.1
WSD24	6593	69.6
ESD1	6593	97.1
ESD2	6593	95.1
ESD3	6593	100.1
ESD4	6593	98.9
ESD5	6593	99.0
ESD6	6593	98.9
E\$D7	6593	85.8
ESD8	6593	104.7
ESD9	6593	124.0
ESD10	6593	99.6
ESDII	6593	78.5
ESD12	6593	78.6
ESD13	6593	56.4

Area	η	Ę	Weight
1	960784	.780824	102.000
2	806373	.780824	299.6250
3	575980	.780824	299.6250
4	345588	.780824	299.6250
5	115196	.780824	299.6250
6	.115196	.780824	299.6250
7	.345588	.780824	299.6250
8	.575980	.780824	299.6250
9	.806373	.780824	299.6250
10	.960784	.780824	102.0000
11	901961	.429491	128.3336
12	450980	.429491	128.3336
13	.000000	.429491	128.3336
14	.450980	.429491	128.3336
15	.901961	.429491	128.3336
16	901961	073344	128.3329
17	450980	073344	128.3328
18	.000000	073344	128.3328
19	.450980	073344	128.3328
20	.901961	073344	128.3328
21	901961	576180	128.3335
22	450980	576180	128.3336
23	.000000	576180	128.3336
24	.450980	576180	128.3336
25	.901961	576180	128.3335
26	806373	913799	258.5000
27	575980	913799	258.5000
28	345588	913799	258.5000
29	115196	913799	258.5000
30	.115196	913799	258.5000
31	.345588	913799	258.5000
32	.575980	913799	258.5000
33	.806373	913799	258.5000

Section #1 Arel=.2533 B=408.0000 H=63.8047

Area	n n	Ę	Weight
1	965523	.799891	102.0000
2	884973	.799891	287.2734
3	766085	.799891	287.2734
4	647197	.799891	287.2734
5	528310	.799891	287.2734
6	- 409422	799891	287 2734
7	- 290534	799891	287 2734
8	. 171646	799891	287 7734
9	052759	799891	287 2734
10	066129	799891	287 2734
11	185017	799891	287 2734
12	303905	799891	287 2734
13	.422792	.799891	287,2734
14	.541680	.799891	287,2734
15	.660568	.799891	287.2734
16	.779456	.799891	287.2734
17	.898344	.799891	287.2734
18	.978894	.799891	102.0000
19	933864	.444797	128.3335
20	751822	.444797	128.3336
21	509100	.444797	128.3336
22	266377	.444797	128.3336
23	023655	.444797	128.3336
24	.219067	.444797	128.3336
25	.461790	.444797	128.3336
26	.704512	.444797	128.3334
27	.947234	.444797	128.3335
28	933864	063423	128.3328
29	751822	063423	128.3329
30	509100	063423	128.3328
31	266377	063423	128.3328
32	023655	063423	128.3328
33	.219067	063423	128.3328
34	.461790	063423	128.3329
35	.704512	063423	128.3329
36	.947234	063423	128.3328
37	933864	571643	128.3336
38	751822	571643	128.3335
39	509100	571643	128.3336
40	266377	571643	128.3336
41	023655	571643	128.3336
42	.219067	571643	128.3336
43	.461790	571643	128.3335
44	.704512	571643	128.3337
45	.947234	571643	128.3337
46	884973	912877	-247.8438
47	-,766085	912877	247.8438

Area	η	ξ	Weight
48	647197	912877	247.8438
49	528310	912877	247.8438
50	409422	912877	247.8438
51	290534	912877	247.8438
52	171646	912877	247.8438
53	052759	912877	247.8438
54	.066129	912877	247.8438
55	.185017	912877	247.8438
56	.303905	912877	247.8438
57	.422792	912877	247.8438
58	.541680	912877	247.8438
59	.660568	912877	247.8438
60	.779456	912877	247.8438
61	.898344	912877	247.8438

Section #2 Arel=.255577 B=758.0679 H=63.1288

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Area	η	ξ	Weight	
1	934589	.800434	102.000	
2	854096	.800434	269.3438	
3	737330	.800434	269.3438	
4	620564 .800434		269.3438	
5	503797	.800434	269.3438	
6	387031	.800434	269.3438	
7	270265	.800434	269.3438	
8	153499	.800434	269.3438	
9	036732	.800434	269.3438	
10	.080034	.800434	269.3438	
11	.196800	.800434	269.3438	
12	.313566	.800434	269.3438	
13	.430333	.800434	269.3438	
14	.547099	.800434	269.3438	
15	.663865	.800434	269.3438	
16	.780631	.800434	269.3438	
17	.897398	.800434	269.3438	
18	.977890	.800434	102.0000	
19	901425	.445232	128.3337	
20	835096	.445232	128.3335	
21	580836	.445232	128.3336	
22	326575	.445232	128.3336	
23	072315	.445232	128.3336	
24	.181945	.445232	128.3336	
25	.436206	.445232	128.3336	
26	.690466	.445232	128.3335	
27	.944726	.445232	128.3336	
28	901425	063141	128.3328	
29	835096	063141	128.3329	
30	580836	063141	128.3328	
31	326575	063141	128.3328	
32	072315	063141	128.3328	
33	.181945	063141	128.3328	
34	.436206	063141	128.3329	
35	.690466	063141	128.3329	
36	.944726	063141	128.3328	
37	901425	571513	128.3335	
38	835096	571513	128.3336	
39	580836	571513	128.3336	
40	326575	571513	128.3336	
41	072315	571513	128.3336	
42	.181945	571513	128.3336	
43	.436206571513 128.3336		128.3336	
44	.690466	571513	128.3336	
45	.944726	571513	128.3336	
46	854096	912850	232.3750	
47	737330	912850	232.3750	

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Area	η	ξ	Weight
48	620564	912850	232.3750
49	503797	912850	232.3750
50	387031	912850	232.3750
51	270265	912850	232.3750
52	153499	912850	232.3750
53	036732	912850	232.3750
54	.080034	912850	232.3750
55	.196800	912850	232.3750
56	.313566	912850	232.3750
57	.430333	912850	232.3750
58	.547099	912850	232.3750
59	.663865	912850	232.3750
60	.780631	912850	232,3750
61	.897398	912850	232.3750

Section #3 Arel=.256106 B=723.6679 H=63.1098

1 961135 .797017 102.000 2 869643 .797017 286.4197 3 734710 .797017 286.4192 4 599778 .797017 286.4192 5 464845 .797017 286.4192 6 329912 .797017 286.4192 8 060047 .797017 286.4192 8 060047 .797017 286.4192 9 .074886 .797017 286.4193 11 .344751 .797017 286.4192 14 .749549 .797017 286.4192 14 .749549 .797017 286.4197 15 .884481 .797017 286.4197 16 .975974 .797017 102.0000 17 .925096 .442490 128.3335 20 .165269 .442490 128.3335 20 .165269 .442490 128.3326 21 .111032 .442490	Area	n	Ł	Weight	
1 1	1	961135	.797017	102.000	
3 734710 .797017 286.4199 4 599778 .797017 286.4192 5 464845 .797017 286.4192 6 329912 .797017 286.4192 7 194980 .797017 286.4192 8 060047 .797017 286.4192 8 060047 .797017 286.4193 10 .209818 .797017 286.4193 11 .344751 .797017 286.4192 14 .749683 .797017 286.4192 14 .749549 .797017 286.4192 14 .749549 .797017 286.4191 15 .884481 .797017 102.0000 17 .925096 .442490 128.3335 20 .165269 .442490 128.3336 21 .111032 .442490 128.3336 22 .38733 .442490 128.3336 23 .663634 .442490 <td< td=""><td>2</td><td>869643</td><td>.797017</td><td>286,4197</td></td<>	2	869643	.797017	286,4197	
4 599778 97017 286.4192 5 464845 97017 286.4192 6 329912 97017 286.4198 7 194980 97017 286.4192 8 660047 97017 286.4193 9	3	734710	.797017	286.4199	
1 1.33778 1.37701 286.4198 5 464845 .797017 286.4198 6 329912 .797017 286.4198 7 194980 .797017 286.4192 8 060047 .797017 286.4191 9 .074886 .797017 286.4193 10 .209818 .797017 286.4193 11 .344751 .797017 286.4192 14 .749569 .797017 286.4192 14 .749569 .797017 286.4191 15 .884481 .797017 286.4192 14 .749569 .797017 102.0000 17 .925096 .442490 128.3337 18 .717871 .442490 128.3336 20 .165269 .442490 128.3336 21 .111032 .442490 128.3336 22 .387333 .442490 128.3326 25 .925096 .064918	4	- 599778	797017	286.4192	
5	4		797017	286.4192	
3 329912 .197017 286.4192 7 194980 .797017 286.4192 8 060047 .797017 286.4192 9 .074886 .797017 286.4193 10 .209818 .797017 286.4193 11 .344751 .797017 286.4193 12 .479683 .797017 286.4192 14 .749549 .797017 286.4192 14 .749549 .797017 286.4192 15 .884481 .797017 286.4197 16 .975974 .797017 102.0000 17 925096 .442490 128.3335 20 .165269 .442490 128.3335 21 .111032 .442490 128.3336 22 .387333 .442490 128.3336 23 .663634 .442490 128.3336 24 .939935 .442490 128.3328 25 925096 .064918 <		320012	707017	286.4198	
7		529912	.797017	280.4196	
8 00007 1.97017 226.4199 9 .074886 .797017 286.4199 10 .209818 .797017 286.4193 11 .344751 .797017 286.4193 12 .479683 .797017 286.4192 14 .749549 .797017 286.4192 14 .749549 .797017 286.4192 16 .975974 .797017 286.4197 16 .975974 .797017 102.0000 17 925096 .442490 128.3335 20 .165269 .442490 128.3335 20 .165269 .442490 128.3336 21 .111032 .442490 128.3336 22 .387333 .442490 128.3336 23 .663634 .442490 128.3326 24 .939935 .442490 128.3326 25 925096 .064918 128.3328 26 .717871 .064918 <t< td=""><td></td><td>060047</td><td>.797017</td><td>280.4192</td></t<>		060047	.797017	280.4192	
9 .074885 .197017 226.4199 10 .209818 .797017 286.4193 11 .344751 .797017 286.4193 12 .479683 .797017 286.4192 14 .749549 .797017 286.4192 14 .749549 .797017 286.4192 14 .749549 .797017 286.4197 16 .975974 .797017 102.0000 17 925096 .442490 128.3335 19 .441570 .442490 128.3335 20 .165269 .442490 128.3336 21 .111032 .442490 128.3336 22 .387333 .442490 128.3336 23 .663634 .442490 128.3326 24 .939935 .442490 128.3326 25 .925096 .064918 128.3328 26 .717871 .064918 128.3328 27 .441570 .064918 <t< td=""><td>0</td><td>000047</td><td>.797017</td><td>280.4198</td></t<>	0	000047	.797017	280.4198	
10 .20915 .797017 286.4193 11 .344751 .797017 286.4193 12 .479683 .797017 286.4192 13 .614616 .797017 286.4192 14 .749549 .797017 286.4192 14 .749549 .797017 286.4192 16 .975974 .797017 102.0000 17 925096 .442490 128.3335 18 717871 .442490 128.3335 20 165269 .442490 128.3336 21 .111032 .442490 128.3336 22 .387333 .442490 128.3336 23 .663634 .442490 128.3326 24 .939935 .442490 128.3326 25 925096 .064918 128.3328 26 .717871 .064918 128.3328 27 .441570 .064918 128.3328 30 .387333 .064918	10	.0/4680	.797017	286,4199	
11	11	207818	.797017	286.4193	
12 .4.5663 .1.97017 286.4192 13 .614616 .797017 286.4192 14 .749549 .797017 286.4192 15 .884481 .797017 286.4197 16 .975974 .797017 102.0000 17 925096 .442490 128.3337 18 717871 .442490 128.3335 20 165269 .442490 128.3336 21 .111032 .442490 128.3336 22 .387333 .442490 128.3336 23 .663634 .442490 128.3336 24 .939935 .442490 128.3326 25 925096 .064918 128.3328 26 .717871 .064918 128.3328 27 .441570 .064918 128.3328 28 .165269 .064918 128.3328 30 .387333 .064918 128.3328 31 .663634 .064918	11		.797017	200.4196	
13 .614616 .19/017 286.4192 14 .749549 .797017 286.4199 15 .884481 .797017 286.4197 16 .975974 .797017 102.0000 17 925096 .442490 128.3337 18 717871 .442490 128.3336 19 441570 .442490 128.3336 20 165269 .442490 128.3336 21 .111032 .442490 128.3336 22 .387333 .442490 128.3336 23 .663634 .442490 128.3336 24 .939935 .442490 128.3326 25 925096 .064918 128.3329 26 717871 .064918 128.3328 29 .111032 .064918 128.3328 30 .387333 .064918 128.3328 31 .663634 .064918 128.3328 32 .939935 .064918	12	,4/9063	./9/01/	280.4197	
14 .199349 .197017 286.4197 15 .884481 .797017 102.0000 17 .925096 .442490 128.3337 18 .717871 .442490 128.3335 20 .165269 .442490 128.3336 21 .111032 .442490 128.3336 22 .387333 .442490 128.3336 23 .663634 .442490 128.3336 24 .939935 .442490 128.3336 25 .925096 .064918 128.3328 26 .717871 .064918 128.3329 27 .441570 .064918 128.3328 26 .717871 .064918 128.3328 27 .441570 .064918 128.3328 30 .387333 .0064918 128.3328 31 .663634 .064918 128.3328 32 .939935 .064918 128.3335 34 .717871 .572326 <		.014010	.797017	286.4192	
1.5	14	./49349	./9/01/	280.4199	
16 .9/39/4 .19/01/ 102,0000 17 925096 .442490 128,3337 18 717871 .442490 128,3336 19 441570 .442490 128,3336 20 165269 .442490 128,3336 21 .111032 .442490 128,3336 22 .387333 .442490 128,3336 23 .663634 .442490 128,3336 24 .939935 .442490 128,3336 25 925096 064918 128,3328 26 717871 064918 128,3328 26 717871 064918 128,3328 28 .165269 064918 128,3328 30 .387333 064918 128,3328 31 .663634 064918 128,3328 32 .939935 064918 128,3336 34 717871 572326 128,3336 35 441570 5723	15	.884481	./9/01/	286.4197	
17 9.25096 .44,490 128,3357 18 717871 .442490 128,3336 19 441570 .442490 128,3336 20 165269 .442490 128,3336 21 .111032 .442490 128,3336 22 .387333 .442490 128,3336 23 .663634 .442490 128,3336 24 .939935 .442490 128,3336 25 925096 .064918 128,3328 26 717871 .064918 128,3328 26 .717871 .064918 128,3328 28 .165269 .064918 128,3328 29 .111032 .064918 128,3328 30 .387333 .064918 128,3328 31 .663634 .064918 128,3326 32 .939935 .064918 128,3336 34 .717871 .572326 128,3336 35 .441570 .572326	16	.9/39/4	./9/017	102.0000	
16 /1/8/1 .442490 128.3336 19 441570 .442490 128.3335 20 165269 .442490 128.3336 21 .111032 .442490 128.3336 22 .387333 .442490 128.3336 23 .663634 .442490 128.3336 24 .939935 .442490 128.3336 25 925096 064918 128.3328 26 717871 064918 128.3328 28 165269 064918 128.3328 29 .111032 064918 128.3328 30 .387333 064918 128.3328 30 .387333 064918 128.3328 31 .663634 064918 128.3326 32 .939935 064918 128.3336 34 717871 572326 128.3336 35 441570 572326 128.3336 35 441570 57	17	+.923096	.442490	128.3557	
19 441570 .442490 128,335 20 165269 .442490 128,3336 21 .111032 .442490 128,3336 22 .387333 .442490 128,3336 22 .387333 .442490 128,3336 23 .663634 .442490 128,3336 24 .939935 .442490 128,3336 25 925096 064918 128,3328 26 717871 064918 128,3329 27 441570 064918 128,3328 29 .111032 064918 128,3328 30 .387333 064918 128,3328 30 .387333 064918 128,3328 31 .663634 064918 128,3328 32 .939935 064918 128,3335 34 717871 572326 128,3336 35 441570 572326 128,3336 36 165269 .57232	18	/178/1	.442490	128.3336	
20 165269 .442490 128.3356 21 .111032 .442490 128.3336 22 .387333 .442490 128.3336 23 .663634 .442490 128.3336 24 .939935 .442490 128.3336 25 925096 064918 128.3328 26 717871 064918 128.3329 27 441570 064918 128.3328 29 .111032 064918 128.3328 30 .387333 064918 128.3328 30 .387333 064918 128.3328 31 .663634 064918 128.3328 32 .939935 064918 128.3326 33 925096 572326 128.3335 34 717871 572326 128.3336 35 441570 572326 128.3335 36 165269 572326 128.3335 37 .111032 5	19	441570	.442490	128.3335	
21 .111032 .442490 128.3350 22 .387333 .442490 128.3337 23 .663634 .442490 128.3336 24 .939935 .442490 128.3336 25 925096 064918 128.3328 26 717871 064918 128.3329 27 441570 064918 128.3328 28 165269 064918 128.3328 29 .111032 064918 128.3328 30 .387333 064918 128.3328 31 .663634 064918 128.3328 32 .939935 064918 128.3328 33 925096 572326 128.3335 34 717871 572326 128.3336 35 441570 572326 128.3336 36 165269 572326 128.3335 36 165269 572326 128.3335 38 .387333 .	20	165269	.442490	128.3336	
22 .387333 .442490 128.337 23 .663634 .442490 128.3336 24 .939935 .442490 128.3336 25 925096 064918 128.3328 26 717871 064918 128.3329 27 441570 064918 128.3328 28 165269 064918 128.3328 29 .111032 064918 128.3328 30 .387333 064918 128.3328 30 .387333 064918 128.3328 31 .663634 064918 128.3328 32 .939935 064918 128.3326 33 925096 572326 128.3335 34 717871 572326 128.3336 35 441570 572326 128.3336 36 165269 572326 128.3335 36 165269 572326 128.3335 38 .387333 .	21	.111032	.442490	128.3336	
23 .663634 .442490 128.3336 24 .939935 .442490 128.3336 25 925096 064918 128.3328 26 717871 064918 128.3329 27 441570 064918 128.3329 28 165269 064918 128.3328 29 .111032 064918 128.3328 30 .387333 064918 128.3328 30 .387333 064918 128.3328 31 .663634 064918 128.3328 32 .939935 064918 128.3326 33 925096 572326 128.3335 34 717871 572326 128.3336 35 441570 572326 128.3336 36 165269 572326 128.3335 36 165269 572326 128.3335 39 .663634 572326 128.3335 39 .663634 <td< td=""><td>22</td><td>.387333</td><td>.442490</td><td>128.3337</td></td<>	22	.387333	.442490	128.3337	
24 .939935 .442490 128.3336 25 925096 064918 128.3328 26 717871 064918 128.3329 27 441570 064918 128.3329 28 165269 064918 128.3328 29 .111032 064918 128.3328 30 .387333 064918 128.3328 30 .387333 064918 128.3328 31 .663634 064918 128.3328 32 .939935 064918 128.3326 33 925096 572326 128.3335 34 717871 572326 128.3336 35 441570 572326 128.3336 36 165269 572326 128.3335 36 165269 572326 128.3335 39 .663634 572326 128.3335 39 .663634 572326 128.3335 40 .939935 <t< td=""><td>23</td><td>.663634</td><td>.442490</td><td>128.3336</td></t<>	23	.663634	.442490	128.3336	
25 925096 064918 128.3328 26 717871 064918 128.3329 27 441570 064918 128.3329 28 165269 064918 128.3328 29 .111032 064918 128.3328 30 .387333 064918 128.3328 30 .387333 064918 128.3328 31 .663634 064918 128.3328 32 .939935 064918 128.3329 33 925096 572326 128.3335 34 717871 572326 128.3336 35 441570 572326 128.3336 36 165269 572326 128.3335 36 165269 572326 128.3335 38 .387333 572326 128.3335 39 .663634 572326 128.3335 40 .939935 572326 128.3335 41 869643	24	.939935	.442490	128.3336	
26 717871 064918 128.3329 27 441570 064918 128.3329 28 165269 064918 128.3328 29 .111032 064918 128.3328 30 .387333 064918 128.3328 31 .663634 064918 128.3328 32 .939935 064918 128.3329 33 925096 572326 128.3335 34 717871 572326 128.3336 35 441570 572326 128.3336 36 165269 572326 128.3336 36 165269 572326 128.3335 38 .387333 572326 128.3335 39 .663634 572326 128.3335 40 .939935 572326 128.3335 41 869643 .913016 247.1072 42 734710 .913016 247.1073 43 .599778 <t< td=""><td>25</td><td>925096</td><td>064918</td><td>128.3328</td></t<>	25	925096	064918	128.3328	
27 441570 064918 128.3329 28 165269 064918 128.3328 29 .111032 064918 128.3328 30 .387333 064918 128.3328 31 .663634 064918 128.3328 32 .939935 064918 128.3329 33 925096 572326 128.3335 34 717871 572326 128.3336 35 441570 572326 128.3336 36 165269 572326 128.3336 36 165269 572326 128.3336 37 .111032 572326 128.3335 38 .387333 572326 128.3335 39 .663634 572326 128.3335 40 .939935 572326 128.3335 41 869643 .913016 247.1072 42 734710 .913016 247.1073 43 .599778 <td< td=""><td>26</td><td>717871</td><td>064918</td><td>128.3329</td></td<>	26	717871	064918	128.3329	
28 165269 064918 128.3328 29 .111032 064918 128.3328 30 .387333 064918 128.3328 31 .663634 064918 128.3328 32 .939935 064918 128.3329 33 925096 572326 128.3335 34 717871 572326 128.3336 35 441570 572326 128.3336 36 165269 572326 128.3336 36 165269 572326 128.3336 37 .111032 572326 128.3335 38 .387333 572326 128.3335 39 .663634 572326 128.3335 40 .939935 572326 128.3335 41 869643 913016 247.1072 42 734710 913016 247.1073 43 599778 913016 247.1073 44 464845	27	441570	064918	128.3329	
29 .111032 .064918 128.3328 30 .387333 .064918 128.3328 31 .663634 .064918 128.3328 32 .939935 .064918 128.3328 33 925096 .572326 128.3335 34 .717871 .572326 128.3336 35 .441570 .572326 128.3336 36 .165269 .572326 128.3336 36 .165269 .572326 128.3335 38 .387333 .572326 128.3335 39 .663634 .572326 128.3335 40 .939935 .572326 128.3335 41 .869643 .913016 247.1072 42 .734710 .913016 247.1073 43 .599778 .913016 247.1072 45 .329912 .913016 247.1073 46 .194980 .913016 247.1073 46 .194980 .913016 <	28	165269	064918	128.3328	
30 .387333 .064918 128.3328 31 .663634 .064918 128.3328 32 .939935 .064918 128.3329 33 925096 .572326 128.3335 34 .717871 .572326 128.3336 35 .441570 .572326 128.3336 36 .165269 .572326 128.3336 37 .111032 .572326 128.3335 38 .387333 .572326 128.3335 39 .663634 .572326 128.3335 40 .939935 .572326 128.3335 41 .869643 .913016 247.1072 42 .734710 .913016 247.1073 43 .599778 .913016 247.1072 44 .464845 .913016 247.1073 45 .329912 .913016 247.1073 46 .914980 .913016 247.1073 45 .329912 .913016 <	29	.111032	064918	128.3328	
31 .663634 .064918 128.3328 32 .939935 .064918 128.3329 33 925096 572326 128.3335 34 717871 572326 128.3336 35 441570 572326 128.3336 36 165269 572326 128.3336 37 .111032 572326 128.3335 38 .387333 572326 128.3335 39 .663634 572326 128.3335 40 .939935 572326 128.3335 41 869643 913016 247.1072 42 734710 913016 247.1073 43 599778 913016 247.1072 44 464845 913016 247.1073 45 329912 913016 247.1073 46 914980 913016 247.1073 46 914980 913016 247.1073 46 914980	30	.387333	064918	128.3328	
32 .939935 .064918 128.3329 33 925096 .572326 128.3335 34 .717871 .572326 128.3336 35 .441570 .572326 128.3336 36 .165269 .572326 128.3336 36 .165269 .572326 128.3336 37 .111032 .572326 128.3335 38 .387333 .572326 128.3335 39 .663634 .572326 128.3335 40 .939935 .572326 128.3335 41 .869643 .913016 247.1072 42 .734710 .913016 247.1073 43 .599778 .913016 247.1072 44 .464845 .913016 247.1073 45 .329912 .913016 247.1073 46 .194980 .913016 247.1073 45 .329912 .913016 247.1073 46 .914980 .913016 <	31	.663634	064918	128.3328	
33 925096 572326 128.3335 34 717871 572326 128.3336 35 441570 572326 128.3336 36 165269 572326 128.3336 36 165269 572326 128.3336 37 .111032 572326 128.3335 38 .387333 572326 128.3335 39 .663634 572326 128.3335 40 .939935 572326 128.3335 41 869643 913016 247.1072 42 734710 913016 247.1073 43 599778 913016 247.1072 44 464845 913016 247.1073 45 329912 913016 247.1073 46 194980 913016 247.1068 47 060047 913016 247.1073	32	.939935	064918	128.3329	
34 717871 572326 128.3336 35 441570 572326 128.3336 36 165269 572326 128.3336 37 .111032 572326 128.3336 38 .387333 572326 128.3335 39 .663634 572326 128.3335 40 .939935 572326 128.3335 41 869643 913016 247.1072 42 734710 913016 247.1073 43 599778 913016 247.1072 44 464845 913016 247.1073 45 329912 913016 247.1073 46 194980 913016 247.1073 47 060047 913016 247.1073	33	925096	572326	128.3335	
35 441570 572326 128.3336 36 165269 572326 128.3336 37 .111032 572326 128.3336 38 .387333 572326 128.3335 39 .663634 572326 128.3335 40 .939935 572326 128.3335 41 869643 913016 247.1072 42 734710 913016 247.1073 43 599778 913016 247.1072 44 464845 913016 247.1073 45 329912 913016 247.1073 46 194980 913016 247.1073 47 060047 913016 247.1073	34	717871	572326	128.3336	
36 165269 572326 128.3336 37 .111032 572326 128.3336 38 .387333 572326 128.3335 39 .663634 572326 128.3335 40 .939935 572326 128.3335 41 869643 913016 247.1072 42 734710 913016 247.1073 43 599778 913016 247.1072 44 464845 913016 247.1073 45 329912 913016 247.1073 46 194980 913016 247.1073 47 060047 913016 247.1073	35	441570	572326	128.3336	
37 .111032 572326 128.3336 38 .387333 572326 128.3335 39 .663634 572326 128.3335 40 .939935 572326 128.3335 41 869643 913016 247.1072 42 734710 913016 247.1073 43 599778 913016 247.1072 44 464845 913016 247.1073 45 329912 913016 247.1073 46 194980 913016 247.1073 47 060047 913016 247.1073	36	165269	572326	128.3336	
38 .387333 572326 128.3335 39 .663634 572326 128.3335 40 .939935 .572326 128.3335 41 869643 .913016 247.1072 42 734710 913016 247.1073 43 599778 913016 247.1072 44 464845 .913016 247.1072 45 329912 913016 247.1073 46 194980 913016 247.1068 47 060047 913016 247.1073	37	.111032	572326	128.3336	
39 .663634 572326 128.3335 40 .939935 572326 128.3335 41 869643 .913016 247.1072 42 734710 913016 247.1073 43 599778 913016 247.1068 44 464845 913016 247.1072 45 329912 913016 247.1073 46 194980 913016 247.1068 47 060047 913016 247.1073	38	.387333	572326	128.3335	
40 .939935 572326 128.3335 41 869643 .913016 247.1072 42 734710 913016 247.1073 43 599778 913016 247.1072 44 464845 913016 247.1072 45 329912 913016 247.1073 46 194980 913016 247.1068 47 060047 913016 247.1073	39	.663634	572326	128.3335	
41 869643 913016 247.1072 42 734710 913016 247.1073 43 599778 913016 247.1068 44 464845 913016 247.1072 45 329912 913016 247.1073 46 194980 913016 247.1068 47 060047 913016 247.1073	40	.939935	572326	128.3335	
42 734710 913016 247.1073 43 599778 913016 247.1068 44 464845 913016 247.1072 45 329912 913016 247.1073 46 194980 913016 247.1068 47 060047 913016 247.1073	41	869643	913016	247.1072	
43 599778 913016 247.1068 44 464845 913016 247.1072 45 329912 913016 247.1073 46 194980 913016 247.1068 47 060047 913016 247.1073	42	734710	913016	247.1073	
44 464845 913016 247.1072 45 329912 913016 247.1073 46 194980 913016 247.1068 47 060047 913016 247.1073	43	599778	913016	247.1068	
45 329912 913016 247.1073 46 194980 913016 247.1068 47 060047 913016 247.1073	44	464845	913016	247.1072	
46 194980 913016 247.1068 47 060047 913016 247.1073	45	329912	913016	247.1073	
47060047913016 247.1073	46	194980	913016	247.1068	
La construction de la constructi	47	060047	913016	247.1073	

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Area	η	ξ	Weight
48	.074886	913016	247.1073
49	.209818	913016	247.1068
50	.344751	913016	247.1073
51	.479683	913016	247.1073
52	.614616	913016	247.1068
53	.749549	913016	247.1073
54	.884481	913016	247.1072

Section #4 Arel=.255380 B=655.9407 H=63.2298

r	r	r	r	
Area	η	ξ	Weight	
1	.925966	.797485	102.000	
2	834555	.797485	265.9287	
3	702417	.797485	265.9287	
4	570278	.797485	265.9286	
5	438139	.797485	265.9287	
6	306001	.797485	265.9280	
7	173862	.797485	265.9286	
8	041723	.797485	265.9287	
9	.090415	.797485	265.9287	
10	.222554	.797485	265.9287	
11	.354693	.797485	265.9287	
12	.486831	.797485	265.9281	
13	.618970	.797485	265.9286	
14	.751109	.797485	265.9287	
15	.883247	.797485	265.9287	
16	.974658	.797485	102.0000	
17	887954	.442865	128.3336	
18	811929	.442865	128.3337	
19	520500	.442865	128.3335	
20	229071	.442865	128.3336	
21	.062358	.442865	128.3336	
22	.353788	.442865	128.3336	
23	.645217	.442865	128.3336	
24	.936646	.442865	128.3337	
25	887954	064675	128.3328	
26	811929	064675	128.3329	
27	520500	.064675	128.3329	
28	229071	064675	128.3328	
29	.062358	064675	128.3328	
30	.353788	064675	128.3328	
31	.645217	064675	128.3328	
32	.936646	064675	128.3329	
33	887954	572215	128.3336	
34	811929	572215	128.3335	
35	520500	572215	128.3336	
36	229071	572215	128.3336	
37	.062358	572215	128.3336	
38	.353788	572215	128.3336	
39	.645217	572215	128.3336	
40	.936646	572215	128.3334	
41	834555	912993	229.4286	
42	702417	912993	229.4287	
43	570278	912993	229.4286	
44	438139	912993	229.4286	
45	306001	912993	229.4281	
46	173862	912993	229.4286	
47	041723	912993	229.4286	

η	ξ	Weight
.090415	912993	229.4286
.222554	912993	229.4286
.354693	912993	229.4287
.486831	912993	229.4281
.618970	912993	229.4286
.751109	912993	229.4287
.883247	912993	229.4286
	η .090415 .222554 .354693 .486831 .618970 .751109 .883247	η ξ .090415 912993 .222554 912993 .354693 912993 .486831 912993 .618970 912993 .751109 912993 .883247 912993

Section #5 Arel=.256044 B=631.3713 H=63.2133

×.

Area	n	ξ	Weight	
1	972973	.793091	102.0000	1
2	867117	.793091	297.5002	
3	709459	.793091	297.5002	1
4	551802	.793091	297.4996	1
5	394144	.793091	297.5002	
6	236486	.793091	297,4996	1
7	078829	.793091	297.5002	1
8	.078829	.793091	297,5002	1
9	.236486	.793091	297.4996	1
10	394144	793091	297 5002	
11	.551802	793091	297.5002	4
12	709459	793091	297 4996	
13	867117	793091	297,5002	1
14	977973	793001	102,000	
15	.932432	410139	128 3336	ł
16	532432	410138	128 3336	
17	- 310811	430338	128.3330	
1/	510811	430330	128 3330	
10	210811	.439338	128.3330	
19	.310811	.439338	128.3330	
AU	.621622	.439338	128.3330	
21	.932432	.439338	128.3336	
	932432	066961	128.3329	
23	621622	066961	128.3329	
24	310811	066961	128.3328	
25	.000000	066961	128.3328	
26	.310811	066961	128.3328	
27	.621622	066961	128.3328	
28	.932432	066961	128.3330	
29	932432	573261	128.3336	
30	621622	573261	128.3335	
31	310811	573261	128.3336	
32	.000000	573261	128.3336	
33	.310811	573261	128.3336	
34	.621622	573261	128.3335	
35	.932432	573261	128.3336	
36	867117	913206	256.6669	
37	709459	913206	256.6669	
38	551802	913206	256.6663	
39	394144	913206	256.6669	
40	236486	913206	256.6663	
41	078829	913206	256.6668	
42	.078829	913206	256.6668	
43	.236486	913206	256.6663	
44	.394144	913206	256.6669	Section #6
. 45	.551802	913206	256.6669	Arel=.254545
46	.709459	913206	256.6663	B=592.0000
47	867117	913206	256.6669	H=63.3682

AreaηξWeight1955477793240102.00002849599793240285.28133693614793240285.28134537629793240285.28135381644793240285.28136225659793240285.28137069674793240285.28138.086311793240285.28139242296793240285.281310398281793240285.281311554266793240285.281312710251793240285.281313866236793240285.281314972114793240102.000015913648439458128.333616673135439458128.333617352451439458128.333618011767439458128.333620609602439458128.332821930286439458128.332822913648666844128.332823673135666884128.332824352451666884128.332825031767666884128.332826288918666884128.332827609602673225128.333633288918573225128.333634.				
1 955477 .793240 102.000 2 849599 .793240 285.2813 3 693614 .793240 285.2813 4 537629 .793240 285.2813 5 381644 .793240 285.2813 6 225659 .793240 285.2813 7 069674 .793240 285.2813 8 .086311 .793240 285.2813 9 .242296 .793240 285.2813 10 .396281 .793240 285.2813 11 .554266 .793240 285.2813 12 .710251 .793240 285.2813 13 .866236 .793240 285.2813 14 .972114 .793240 102.0000 15 .913648 .439458 128.3336 16 .673135 .439458 128.3336 17 .352451 .439458 128.3328 20 .010602 .439458 1	Area	η	Ę	Weight
2 849599 .793240 285.2813 3 693614 .793240 285.2813 4 537629 .793240 285.2813 5 381644 .793240 285.2813 6 225659 .793240 285.2813 7 069674 .793240 285.2813 8 .086311 .793240 285.2813 10 .396281 .793240 285.2813 11 .554266 .793240 285.2813 12 .710251 .793240 285.2813 13 .866236 .793240 285.2813 14 .972114 .793240 285.2813 15 .913648 .439458 128.3336 16 .673135 .439458 128.3336 17 .352451 .439458 128.3336 18 .031767 .439458 128.3336 21 .930286 .439458 128.3328 22 .913648 .066884 <td< td=""><td>1</td><td>955477</td><td>.793240</td><td>102.0000</td></td<>	1	955477	.793240	102.0000
3 693614 .793240 285.2813 4 537629 .793240 285.2813 5 381644 .793240 285.2813 6 225659 .793240 285.2813 7 069674 .793240 285.2813 8 .086311 .793240 285.2813 9 .242296 .793240 285.2813 10 .398281 .793240 285.2813 11 .554266 .793240 285.2813 12 .710251 .793240 285.2813 13 .866236 .793240 285.2813 14 .972114 .793240 285.2813 15 913648 .439458 128.3336 16 673135 .439458 128.3336 17 .352451 .439458 128.3336 20 .609602 .439458 128.3334 22 .913648 .066884 128.3328 23 .673135 066884 <	2	849599	.793240	285.2813
4 537629 .793240 285.2813 5 381644 .793240 285.2813 6 225659 .793240 285.2813 7 069674 .793240 285.2813 8 .086311 .793240 285.2813 9 .242296 .793240 285.2813 10 .396281 .793240 285.2813 11 .554266 .793240 285.2813 12 .710251 .793240 285.2813 13 .866236 .793240 285.2813 14 .972114 .793240 102.0000 15 .913648 .439458 128.3336 16 .673135 .439458 128.3336 17 .352451 .439458 128.3336 20 .609602 .439458 128.3336 21 .930286 .439458 128.3328 22 .913648 .066884 128.3328 23 .673135 .066884	3	693614	.793240	285.2813
5 381644 .793240 285.2813 6 225659 .793240 285.2813 7 069674 .793240 285.2813 8 .086311 .793240 285.2813 9 .242296 .793240 285.2813 10 .398281 .793240 285.2813 11 .554266 .793240 285.2813 12 .710251 .793240 285.2813 13 .866236 .793240 285.2813 14 .972114 .793240 102.0000 15 .913648 .439458 128.3336 16 673135 .439458 128.3336 17 .352451 .439458 128.3336 20 .609602 .439458 128.3328 21 .930286 .439458 128.3328 22 .913648 .066884 128.3328 23 .673135 .066884 128.3328 24 .352451 .066884 <td< td=""><td>4</td><td>537629</td><td>.793240</td><td>285,2813</td></td<>	4	537629	.793240	285,2813
6 225659 .793240 285.2813 7 069674 .793240 285.2813 8 .086311 .793240 285.2813 9 .242296 .793240 285.2813 10 .398281 .793240 285.2813 11 .554266 .793240 285.2813 12 .710251 .793240 285.2813 13 .866236 .793240 285.2813 14 .972114 .793240 102.0000 15 .913648 .439458 128.3336 16 673135 .439458 128.3336 17 .352451 .439458 128.3336 18 031767 .439458 128.3336 20 .609602 .439458 128.3328 21 .930286 .439458 128.3328 22 .913648 .066884 128.3328 23 .673135 .573225 128.3328 24 .332451 .066884 <t< td=""><td>5</td><td>381644</td><td>.793240</td><td>285.2813</td></t<>	5	381644	.793240	285.2813
7 069674 .793240 285.2813 8 .086311 .793240 285.2813 9 .242296 .793240 285.2813 10 .398281 .793240 285.2813 11 .554266 .793240 285.2813 12 .710251 .793240 285.2813 13 .866236 .793240 285.2813 14 .972114 .793240 102.0000 15 913648 .439458 128.3336 16 673135 .439458 128.3336 17 352451 .439458 128.3336 18 .031767 .439458 128.3336 20 .609602 .439458 128.3328 21 .930286 .439458 128.3328 22 .913648 .066884 128.3328 23 .673135 .566884 128.3328 24 .332451 .066884 128.3328 25 .031767 .566884 <	6	225659	.793240	285,2813
8 .086311 .793240 285.2813 9 .242296 .793240 285.2813 10 .398281 .793240 285.2813 11 .554266 .793240 285.2813 12 .710251 .793240 285.2813 13 .866236 .793240 285.2813 14 .972114 .793240 102.0000 15 .913648 .439458 128.3336 16 .673135 .439458 128.3336 17 .352451 .439458 128.3336 18 .031767 .439458 128.3336 20 .609602 .439458 128.3336 21 .930286 .439458 128.3328 22 .913648 .066884 128.3328 23 .673135 .066884 128.3328 24 .332451 .066884 128.3328 25 .031767 .066884 128.3328 26 .288918 .066884	7	069674	.793240	285,2813
9 242296 793240 285,2813 10 .398281 .793240 285,2813 11 .554266 .793240 285,2813 12 .710251 .793240 285,2813 13 .866236 .793240 285,2813 14 .972114 .793240 102,0000 15 913648 .439458 128,3336 16 673135 .439458 128,3336 17 352451 .439458 128,3336 18 .031767 .439458 128,3336 20 .609602 .439458 128,3336 21 .930286 .439458 128,3328 22 .913648 .066884 128,3328 23 673135 .066884 128,3328 24 .332451 .066884 128,3328 25 .031767 .066884 128,3328 26 .288918 .066884 128,3328 25 .031767 .573225 <	8	086311	.793240	285 2813
1 1.193.0 1.193.20 1.193.20 2.20.12 10 .398281 .793240 285,2813 11 .554266 .793240 285,2813 12 .710251 .793240 285,2813 13 .866236 .793240 285,2813 14 .972114 .793240 102,0000 15 913648 .439458 128,3336 16 673135 .439458 128,3336 17 352451 .439458 128,3336 18 .031767 .439458 128,3336 20 .609602 .439458 128,3336 21 .930286 .439458 128,3328 22 .913648 .066884 128,3328 23 .673135 .066884 128,3328 24 .332451 .066884 128,3328 25 .031767 .066884 128,3329 28 .930286 .066884 128,3328 27 .609602		242296	793240	285 2813
1 .554266 .793240 285.2813 11 .554266 .793240 285.2813 12 .710251 .793240 285.2813 13 .866236 .793240 285.2813 14 .972114 .793240 102.0000 15 913648 .439458 128.3336 16 673135 .439458 128.3336 17 352451 .439458 128.3336 18 .031767 .439458 128.3336 20 .609602 .439458 128.3336 21 .930286 .439458 128.3328 22 .913648 .066884 128.3328 23 673135 .066884 128.3328 24 .332451 .066884 128.3328 25 .031767 .066884 128.3328 26 .288918 .066884 128.3328 27 .609602 .066884 128.3329 28 .930286 .066884	10	398281	793240	285 2813
11	10	554266	793240	285 2813
12	12	710251	793240	285.2013
13	12	966736	202240	285,2813
14	-13	.800230	702240	103,0000
15	14	.9/2/14	430449	128 2226
16 6/3135 .4.59838 128.3336 17 352451 .439458 128.3336 18 031767 .439458 128.3336 19 .288918 .439458 128.3336 20 .609602 .439458 128.3336 21 .930286 .439458 128.3328 22 913648 066884 128.3328 23 673135 066884 128.3328 24 .352451 .066884 128.3328 25 .031767 .066884 128.3328 26 .288918 .066884 128.3328 27 .609602 .066884 128.3329 28 .930286 .066884 128.3329 29 913648 .573225 128.3336 30 .673135 .573225 128.3336 31 .332451 .573225 128.3336 32 .031767 .573225 128.3336 33 .288918 .573225	15	913048	.439438	128,3336
17 332451 .459458 128.3356 18 031767 .439458 128.3336 19 .288918 .439458 128.3336 20 .609602 .439458 128.3336 21 .930286 .439458 128.3324 22 913648 066884 128.3328 23 673135 066884 128.3328 24 .352451 .066884 128.3328 25 .031767 .066884 128.3328 26 .288918 .066884 128.3328 26 .288918 .066884 128.3329 28 .930286 .066884 128.3329 29 913648 .573225 128.3336 30 .673135 .573225 128.3336 31 .352451 .573225 128.3336 32 .031767 .573225 128.3336 33 .288918 .573225 128.3336 34 .609602 .573225	10	0/3135	.439438	128.3336
18 031767 4.39458 128.3356 19 .288918 4.39458 128.3336 20 .609602 4.39458 128.3336 21 .930286 4.39458 128.3334 22 913648 066884 128.3328 23 673135 066884 128.3328 24 352451 066884 128.3328 25 031767 066884 128.3328 26 .288918 066884 128.3328 27 .609602 066884 128.3329 28 .930286 066884 128.3329 29 913648 573225 128.3336 30 673135 573225 128.3336 31 352451 573225 128.3336 32 031767 573225 128.3336 33 .288918 573225 128.3337 34 .609602 573225 128.3337 35 .930286 -	17	•.352451	.439438	128.3336
19 .288918 .439438 (28.3336) 20 .609602 .439458 128.3336 21 .930286 .439458 128.3334 22 .913648 .066884 128.3328 23 .673135 .066884 128.3328 24 .352451 .066884 128.3328 25 .031767 .066884 128.3328 26 .288918 .066884 128.3328 27 .609602 .066884 128.3329 28 .930286 .066884 128.3329 28 .930286 .066884 128.3329 29 .913648 .573225 128.3336 30 .673135 .573225 128.3336 31 .332451 .573225 128.3336 32 .031767 .573225 128.3336 33 .288918 .573225 128.3337 34 .609602 .573225 128.3337 35 .930286 .573225 <	18	031767	.439458	128.3336
20 .609602 .439458 128.3336 21 .930286 .439458 128.3334 22 .913648 .066884 128.3328 23 .673135 .066884 128.3328 24 .332451 .066884 128.3328 25 .031767 .066884 128.3328 26 .288918 .066884 128.3328 27 .609602 .066884 128.3329 28 .930286 .066884 128.3329 29 .913648 .573225 128.3336 30 .673135 .573225 128.3336 31 .332451 .573225 128.3336 32 .031767 .573225 128.3336 33 .288918 .573225 128.3336 34 .609602 .573225 128.3337 35 .930286 .573225 128.3337 36 .849599 .913198 246.1250 37 .693614 .913198 <t< td=""><td>19</td><td>.288918</td><td>.439458</td><td>128,3336</td></t<>	19	.288918	.439458	128,3336
21 .930286 .439458 128.3334 22 .913648 .066884 128.3328 23 .673135 .066884 128.3328 24 .332451 .066884 128.3328 25 .031767 .066884 128.3328 26 288918 .066884 128.3329 28 .930286 .066884 128.3329 28 .930286 .066884 128.3329 29 .913648 .573225 128.3336 30 .673135 .573225 128.3336 31 .352451 .573225 128.3336 32 .031767 .573225 128.3336 33 .288918 .573225 128.3336 34 .609602 .573225 128.3337 35 .930286 .573225 128.3337 36 .549599 .913198 246.1250 37 .693614 .913198 246.1250 38 .537629 .913198 <td< td=""><td>20</td><td>.609602</td><td>.439458</td><td>128,3336</td></td<>	20	.609602	.439458	128,3336
22 913648 066884 128.3328 23 673135 066884 128.3328 24 352451 066884 128.3328 25 031767 066884 128.3328 26 288918 066884 128.3328 27 .609602 066884 128.3329 28 .990286 066884 128.3329 29 913648 573225 128.3336 30 673135 573225 128.3336 31 352451 573225 128.3336 32 031767 573225 128.3336 33 288918 573225 128.3336 34 .609602 573225 128.3337 35 .930286 573225 128.3337 36 849599 .913198 246.1250 37 693614 .913198 246.1250 38 537629 .913198 246.1250 40 225659 <td< td=""><td>21</td><td>.930286</td><td>.439458</td><td>128.3334</td></td<>	21	.930286	.439458	128.3334
23 673135 066884 128.3328 24 .352451 .066884 128.3328 25 .031767 .066884 128.3328 26 288918 .066884 128.3328 27 .609602 .066884 128.3329 28 .930286 .066884 128.3329 29 .913648 .573225 128.3336 30 .673135 .573225 128.3336 31 .352451 .573225 128.3336 32 .031767 .573225 128.3336 33 288918 .573225 128.3336 34 .609602 .573225 128.3337 35 .930286 .573225 128.3337 36 .849599 .913198 246.1250 37 693614 .913198 246.1250 38 .537629 .913198 246.1250 40 .225659 .913198 246.1250 41 .069674 .913198 <	22	913648	066884	128.3328
24 352451 066884 128.3328 25 031767 066884 128.3328 26 288918 .066884 128.3328 27 .609602 .066884 128.3329 28 .930286 .066884 128.3329 29 913648 .573225 128.3336 30 673135 .573225 128.3336 31 .352451 .573225 128.3336 32 .031767 .573225 128.3336 33 .288918 .573225 128.3336 34 .609602 .573225 128.3337 35 .930286 .573225 128.3337 36 .849599 .913198 246.1250 37 .693614 .913198 246.1250 38 .537629 .913198 246.1250 39 .381644 .913198 246.1250 40 .225659 .913198 246.1250 41 .069674 .913198	23	673135	066884	128.3328
25 031767 066884 128.3328 26 .288918 066884 128.3328 27 .609602 066884 128.3329 28 .930286 066884 128.3329 29 913648 573225 128.3336 30 673135 573225 128.3336 31 352451 573225 128.3336 32 031767 573225 128.3336 33 .288918 573225 128.3336 34 .609602 573225 128.3337 35 930286 573225 128.3337 36 849599 913198 246.1250 37 693614 913198 246.1250 38 537629 913198 246.1250 39 381644 913198 246.1250 40 225659 913198 246.1250 41 069674 913198 246.1250 42 086311	24	352451	066884	128.3328
26 288918 066884 128.3328 27 .609602 066884 128.3329 28 .930286 066884 128.3329 29 913648 573225 128.3336 30 673135 573225 128.3336 31 352451 573225 128.3336 32 031767 573225 128.3336 33 .288918 573225 128.3336 34 .609602 573225 128.3337 35 .930286 573225 128.3337 36 849599 .913198 246.1250 37 693614 .913198 246.1250 38 537629 .913198 246.1250 39 381644 .913198 246.1250 40 225659 .913198 246.1250 41 .069674 .913198 246.1250 42 .086311 .913198 246.1250 43 .242296 .9131	25	031767	066884	128.3328
27 .609602 066884 128.3329 28 930286 066884 128.3329 29 913648 573225 128.3336 30 673135 573225 128.3336 31 352451 573225 128.3336 32 031767 573225 128.3336 33 .288918 573225 128.3336 34 .609602 573225 128.3337 36 849599 913198 246.1250 37 693614 913198 246.1250 38 537629 913198 246.1250 39 381644 913198 246.1250 40 225659 913198 246.1250 41 069674 913198 246.1250 42 .086311 913198 246.1250 43 .242296 913198 246.1250 44 398281 913198 246.1250 45 554266	26	.288918	066884	128.3328
28	27	.609602	066884	128.3329
29 913648 573225 128.3336 30 673135 573225 128.3336 31 352451 573225 128.3336 32 031767 573225 128.3336 33 .288918 573225 128.3336 34 .609602 573225 128.3337 35 .930286 573225 128.3337 36 849599 913198 246.1250 37 693614 913198 246.1250 38 537629 913198 246.1250 39 381644 913198 246.1250 40 225639 913198 246.1250 41 069674 913198 246.1250 42 .086311 913198 246.1250 43 .242296 913198 246.1250 44 .398281 913198 246.1250 45 .554266 913198 246.1250 45 .554266	28	.930286	066884	128,3329
30 673135 573225 128.3336 31 352451 573225 128.3336 32 031767 573225 128.3336 33 .288918 573225 128.3336 34 .609602 573225 128.3337 35 .930286 573225 128.3337 36 849599 913198 246.1250 37 693614 913198 246.1250 38 537629 913198 246.1250 39 381644 913198 246.1250 40 225659 913198 246.1250 41 069674 913198 246.1250 42 .086311 913198 246.1250 43 .242296 913198 246.1250 44 .398281 913198 246.1250 45 .554266 913198 246.1250 45 .554266 913198 246.1250 46 .710251 <	29	913648	573225	128,3336
31 352451 573225 128.3336 32 031767 573225 128.3336 33 .288918 573225 128.3336 34 .609602 573225 128.3337 35 .930286 573225 128.3337 36 849599 913198 246.1250 37 693614 913198 246.1250 38 537629 913198 246.1250 39 381644 913198 246.1250 40 225659 913198 246.1250 41 069674 913198 246.1250 42 .086311 913198 246.1250 43 .242296 913198 246.1250 44 .398281 913198 246.1250 45 .554266 913198 246.1250 46 .710251 913198 246.1250 46 .710251 913198 246.1250 46 .710251 <t< td=""><td>30</td><td>673135</td><td>573225</td><td>128.3336</td></t<>	30	673135	573225	128.3336
32 031767 573225 128.3336 33 .288918 573225 128.3336 34 .609602 573225 128.3335 35 .930286 573225 128.3337 36 849599 913198 246.1250 37 693614 913198 246.1250 38 537629 913198 246.1250 39 381644 913198 246.1250 40 225659 913198 246.1250 41 069674 913198 246.1250 42 .086311 913198 246.1250 43 .242296 913198 246.1250 44 98281 913198 246.1250 45 554266 913198 246.1250 45 554266 913198 246.1250 46 .710251 913198 246.1250 46 710251 913198 246.1250 46 710251	31	352451	573225	128.3336
33 .288918 573225 128.3336 34 .609602 573225 128.3335 35 .930286 573225 128.3337 36 849599 913198 246.1250 37 693614 913198 246.1250 38 537629 913198 246.1250 39 381644 913198 246.1250 40 225659 913198 246.1250 41 069674 913198 246.1250 42 .086311 913198 246.1250 43 .242296 913198 246.1250 44 98281 913198 246.1250 45 554266 913198 246.1250 46 .710251 913198 246.1250 46 913198 246.1250 47 .866236 913198 246.1250	32	031767	573225	128.3336
34 .609602 573225 128.3335 35 .930286 573225 128.3337 36 849599 913198 246.1250 37 693614 913198 246.1250 38 537629 913198 246.1250 39 381644 913198 246.1250 40 225659 913198 246.1250 41 069674 913198 246.1250 42 .086311 913198 246.1250 43 .242296 913198 246.1250 44 .398281 913198 246.1250 45 .554266 913198 246.1250 46 .710251 913198 246.1250 46 .710251 913198 246.1250 47 .866236 913198 246.1250	33	.288918	573225	128.3336
35 930286 573225 128.3337 36 849599 913198 246.1250 37 693614 913198 246.1250 38 537629 913198 246.1250 39 381644 913198 246.1250 40 225659 913198 246.1250 41 069674 913198 246.1250 42 .086311 913198 246.1250 43 .242296 913198 246.1250 44 .398281 913198 246.1250 45 .554266 913198 246.1250 46 .710251 913198 246.1250 46 .710251 913198 246.1250 47 .866236 913198 246.1250	34	.609602	573225	128.3335
36 849599 913198 246.1250 37 693614 913198 246.1250 38 537629 913198 246.1250 39 381644 913198 246.1250 40 225659 913198 246.1250 41 069674 913198 246.1250 42 .086311 913198 246.1250 43 .242296 913198 246.1250 44 .398281 913198 246.1250 45 .554266 913198 246.1250 46 .710251 913198 246.1250 47 .866236 913198 246.1250	35	.930286	573225	128.3337
37 693614 913198 246.1250 38 537629 913198 246.1250 39 381644 913198 246.1250 40 225659 913198 246.1250 41 069674 913198 246.1250 42 .086311 913198 246.1250 43 .242296 .913198 246.1250 44 .398281 .913198 246.1250 45 .554266 .913198 246.1250 46 .710251 .913198 246.1250 47 .866236 .913198 246.1250	36	- 849599	913198	246,1250
38 537629 913198 246.1250 39 381644 913198 246.1250 40 225659 913198 246.1250 41 069674 913198 246.1250 42 .086311 913198 246.1250 43 .242296 .913198 246.1250 44 .398281 .913198 246.1250 45 .554266 .913198 246.1250 46 .710251 .913198 246.1250 47 .866236 .913198 246.1250	37	- 693614	- 913198	246.1250
30 381644 913198 246.1250 39 381644 913198 246.1250 40 225659 913198 246.1250 41 069674 913198 246.1250 42 .086311 913198 246.1250 43 .242296 913198 246.1250 44	39	437679	- 913198	246 1250
35	20	-391644	- 013198	246 1250
40 225039 913198 246.1250 41 069674 913198 246.1250 42 .086311 913198 246.1250 43 .242296 913198 246.1250 44 .398281 913198 246.1250 45 .554266 913198 246.1250 46 .710251 913198 246.1250 47 .866236 913198 246.1250	40		012108	246 1250
41 00907/4 915195 246.1250 42 .086311 913198 246.1250 43 .242296 .913198 246.1250 44 .398281 .913198 246.1250 45 .554266 .913198 246.1250 46 .710251 .913198 246.1250 47 .866236 .913198 246.1250	40	223039	913198	246,1250
42	41	0090/4	-,913196	246,1230
43 .242296 913198 246.1250 44 .398281 913198 246.1250 45 .554266 913198 246.1250 46 .710251 913198 246.1250 47 .866236 913198 246.1250	42	.056311	913198	246,1250
44	43	.242296	913198	246.1250
45 .554266 913198 246.1250 46 .710251 913198 246.1250 47 .866236 913198 246.1250	44	.398281	913198	246.1250
46 .710251 913198 246.1250 47 .866236 913198 246.1250	45	.554266	913198	246.1250
47 .866236913198 246.1250	46	.710251	913198	246.1250
	47	.866236	913198	246.1250

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Area	η	ξ	Weight
1	952720	.818700	86.0625
2	864798	.818700	285.5089
3	729682	.818700	285,5088
4	594565	.818700	285.5089
5.	459449	.818700	285.5094
6	324333	.818700	285,5089
7	- 189217	.818700	285,5089
8	054100	.818700	285,5088
9	.081016	.818700	285,5088
10	216132	.818700	285.5088
11	351248	.818700	285 5088
12	486364	818700	285 5094
13	621481	818700	285 5083
13	756507	818700	285.5085
15	891713	\$18700	285 5088
15	070636	819700	86.0625
10	.979030	450906	208 6421
1/	775605	450905	208.3421
10	123093	.437873	208.5422
	-,448135	.439893	208,3421
20	170376	.437893	208.3421
21	.100983	450904	208.3421
	.384342	.439893	208.5420
23	.002102	.439893	208.5421
24	.939001	.439893	208.5422
25	912/46	053636	208.5408
	723095	053636	208,5409
2/	448135	053636	208.5408
	170576	053636	208.5408
	.106983	033636	206.5406
30	.384542	053636	208.5408
31	.662102	053636	208.5409
32	.939661	053636	208.5409
33	•.912746	.30/166	208.5421
34	725695	- 567166	208.5420
35	448135	567166	208.5420
36	170576	- 567166	208,5421
37	.106983	567166	208.5421
38	.384542	567166	208.5420
39	.662102	567166	208.5420
40	.939661	567166	208.5421
41	864798	911966	246.3214
42	729682	911966	246.3213
43	594565	-,911966	246.3214
44	459449	911966	246.3219
45	324333	911966	246.3213
46	189217	911966	246.3214
47	054100	911966	246.3214

Area	η	ξ	Weight	
48	.081016	911966	246.3214	
49	.216132	911966	246.3214	
50	.351248	911966	246.3213	
51	.486364	911966	246.3219	
52	.621481	911966	246.3208	
53	.756597	911966	246.3219	
54	.891713	911966	246.3214	

Section #8 Arel=.304775 B=662.9214 H=62.4759

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4.001		¥	Weight
Area	1 007960	820584 86.06	
1	957880	.820384	80.0023
2	8804/0	.820384	280.4700
3	761461	.820384	286.4766
4	642447	.820584	286.4760
5	523433	.820584	286.4766
6	404418	.820584	286.4766
7	285404	.820584	286.4766
8	166390	.820584	286.4766
9	047376	.820584	286.4766
10	.071639	.820584	286.4766
11	.190653	.820584	286.4766
12	.309667	.820584	286.4766
13	.428682	.820584	286.4766
14	.547696	.820584	286.4766
15	.666710	.820584	286.4766
16	.785725	.820584	286.4766
17	.904739	.820584	286.4766
18	.982123	.820584	86.0625
19	922768	.461407	208.5422
20	758565	.461407	208.5420
21	514908	.461407	208.5421
22	271252	.461407	208.5421
23	027595	.461407	208.5421
24	.216062	.461407	208.5421
25	.459718	.461407	208.5421
26	.703375	.461407	208.5420
27	.947031	.461407	208.5421
28	922768	052656	208.5408
29	758565	052656	208.5410
30	514908	052656	208.5409
31	271252	052656	208.5408
32	027595	052656	208.5408
33	.216062	052656	208.5408
34	.459718	052656	208.5408
35	.703375	052656	208.5407
36	.947031	052656	208.5409
37	922768	566718	208.5420
38	758565	566718	208.5420
39	514908	566718	208.5420
40	271252	566718	208.5421
41	027595	566718	208.5421
42	.216062	566718	208.5421
43	.459718	566718	208.5420
44	.703375	566718	208.5420
45	.947031	566718	208.5420
46	880476	911875	247.1563
47	761461	911875	247.1563
	.	J	A

Area	η	Ę	Weight	
48	642447	911875	247.1563	
49	523433	911875	247.1563	
50	404418	911875	247.1563	
51	285404	911875	247.1563	
52	166390	911875	247.1563	
53	047376911875		247.1563	
54	.071639911875		247.1563	
55	.190653	911875	247.1563	
56	.309667	67911875		
57	.428682	28682911875		
58	58 .54769691187		247.1563	
59	.666710911875		247.1563	
60	.785725	911875	247.1563	
61	.904739	911875	247.1563	

Section #9 Arel=.304279 B=755.1613 H=62.4113

Area	η	ξ	Weight
1	966912	.807006	86.0625
2	817096	.807006	303.6094
3	583640	.807006	303.6094
4	350184	.807006	303.6094
5	116728	.807006	303.6094
6	.116728	.807006	303.6094
7	.350184	.807006	303.6094
8	.583640	.807006	303.6094
9	.817096	.807006	303.6094
10	.966912	.807006	86.0625
11	901961	.450508	208.5421
12	450980	.450508	208.5421
13	.000000	.450508	208.5421
14	.450980	.450508	208.5421
15	.901961	.450508	208.5421
16	901961	059721	208.5409
17	450980	059721	208.5408
18	.000000	059721	208.5408
19	.450980	059721	208.5408
20	.901961	059721	208.5408
21	901961	569949	208.5420
22	450980	569949	208.5421
23	000000.	569949	208.5421
24	.450980	569949	208.5421
25	.901961	569949	208.5420
26	817096	912532	261.9375
27	583640	912532	261.9375
28	350184	912532	261.9375
29	116728	912532	261.9375
30	.116728	912532	261.9375
31	.350184	912532	261.9375
32	.583640	912532	261.9375
33	.817096	912532	261.9375

Section #10 Arel=.304992 B=408.0000 H=62.8802

Алеа	η	ξ	Weight
1	968137	.811358	82.8750
2	819240	.811358	304.4063
3	585172	.811358	304.4063
4	351103	.811358	304.4063
5	117034	.811358	304.4063
6	.117034	.811358	304.4063
7	.351103	.811358	304.4063
8	.585172	.811358	304.4063
9	.819240	.811358	304.4063
10	.968137	.811358	82.8750
11	901961	.454001	224.5838
12	450980	.454001	224.5838
13	.000000	.454001	224.5838
14	.450980	.454001	224.5838
15	.901961	.454001	224.5837
16	901961	057456	224.5824
17	450980	057456	224.5825
18	.000000	057456	224.5824
19	.450980	057456	224.5824
20	.901961	057456	224.5825
21	901961	568913	224.5838
22	450980	568913	224.5838
23	.000000	568913	224.5838
24	.450980	568913	224.5838
25	.901961	568913	224.5838
26	819240	912322	262.6250
27	585172	912322	262.6250
28	351103	912322	262.6250
29	·.117034	912322	262.6250
30	.117034	912322	262.6250
31	.351103	912322	262.6250
32	.585172	912322	262.6250
33	.819240	912322	262.6250
a .:	•		

Section #11 Arel=.315344 B=408.0000 H=62.7292

Area	η	ξ	Weight
1	963235	.792295	95.6250
2	810662	.792295	301.2188
3	579044	.792295	301.2188
4	347426	.792295	301.2188
5	115809	.792295	301.2188
6	.115809	.792295	301.2188
7	.347426	.792295	301.2188
8	.579044	.792295	301.2188
9	.810662	.792295	301.2188
10	.963235	.792295	95.6250
11	901961	.438699	160.4169
12	450980	.438699	160.4170
13	.000000	.438699	160.4170
14	.450980	.438699	160.4170
15	.901961	.438699	160.4170
16	901961	067376	160.4160
17	450960	067376	160.4160
18	.000000	067376	160.4160
19	.450980	067376	160.4160
20	.901961	067376	160.4160
21	901961	573450	160.4170
22	450980	573450	160.4170
23	.000000	573450	160.4170
24	.450980	573450	160.4170
25	.901961	573450	160.4170
26	810662	913244	259.8750
27	579044	913244	259.8750
28	347426	913244	259.8750
29	115809	913244	259.8750
30	.115809	913244	259.8750
31	.347426	913244	259.8750
32	.579044	913244	259.8750
33	.810662	913244	259.8750

Section #12 Arel=.273963 B=408.0000 H=62.3964

.

Arca	η	η ξ	
1	973039	.826562	70.125
2	827819	.826562	307.5938
3	591299	.826562	307.5938
4	.354779	.826562	307.5938
5	118260	.826562	307.5938
6	.118260	.826562	307.5938
7	.354779	.826562	307.5938
8	.591299	.826562	307.5938
9	.827819	.826562	307.5938
10	.973039	.826562	70.1250
11	901961	.466206	288.7506
12	450980	.466206	288.7505
13	.000000	.466206	288.7506
14	.450980	.466206	288.7506
15	.901961	.466206	288.7505
16	901961	049545	288.7489
17	450980	049545	288.7488
18	.000000	049545	288.7488
19	.450980	049545	288.7488
20	.901961	049545	288.7488
21	901961	565295	288.7505
22	450980	565295	288.7506
23	.000000	565295	288.7506
24	.450980	565295	288.7506
25	.901961	565295	288.7505
26	827819	911586	265.3750
27	591299	911586	265.3750
28	354779	911586	265.3750
29	118260	911586	265.3750
30	.118260	911586	265.3750
31	.354779	911586	265.3750
32	.591299	911586	265.3750
33	.827819	911586	265.3750
	·		

Section #13 Arel=.356780 B=408.0000 H=62.2070



















				Pa	rameters for each discrete element		
Hinge Number and restrainer type	Number of discrete elements	Discrete material number	Loading direction	Yield force lb	Load curve pairs defining loading Ib-in load curve number	Load curve pairs defining uncoading lb-in load curve number	
L (ESHI)			Positive	960,000.	(-50.,-2.) (-25.,-1.) (0.,0.)	(-50,-2) (0.,0.) (93.,63900000.) 32	
Steel rods	2	16	Negative	-1.	(1.40,960000.) (14.95,1050000.) 31		
2 (ESH2)			Positive	907,200.	(-50.,-2.) (-25.,-1.) (0.,0.)	(-50,-2) (0,0.)	
Cables	4	15	Negative	-1.	(2.37,907200.) (5.92,1145000.) 29	(59.,22680000.) 30	
	_		Positive	800,000.	(-50.,-2.) (-25.,-1.) (0.,0.)	(-50,-2,)(0,0)(00,53250000)	
3 (ESH3)	2	14	Negative	-1.	(1.48,800000.) (15.79,875000.) 27	28	
Steel rods			Positive	960,000.	(-50.,-2.) (-25.,-1.) (0.,0.)	(-50.,-2.) (0.,0.)	
	2	13	Negative	-1 .	- (1.67,960000.) (17.89,1050000.) 25	(112.,63900000.) 26	
A (ESHA)			Positive	640,000.	(-50.,-2.) (-25.,-1.) (0.,0.)	(-50.,-2) (0.,0.)	
Steel rods	4	12	Negative	-1.	(1.67,640000.) (17.89,700000.) 23	(112.,42600000.) 24	
S (ESHS)			Positive	640,000.	(-50.,-2.) (-25.,-1.) (0.,0.) (1.77,640000.) (18.95,700000.) 21	(-50,-2) (0.,0.)	
Steel rods	4	11	Negative	-1,		(118.,42600000.) 22	
6 (WSHI)			Positive	960,000.	(-50.,-2.) (-25.,-1.) (0.,0.)	(-50.,-2) (0.,0.)	
Steel rods	3	1	Negative	-1.	(1.73,960000.) (18.46,1050000.) 1	(115.,63900000.) 2	
7 (145H2)			Positive	907200.	(-50.,-2.) (-25.,-1.) (0.,0.)	(-50.,-2.) (0.,0.)	
Cables	3	2	Negative	-1.	(1.46,907200.) (3.64,1145000.) 3	(26.,22680000.)	
			Positive	960,000.	(-50.,-2.) (-25.,-1.) (0.,0.)	(-50.,-2.) (0.,0.) (112.,63900000	
8 (WSH3)	2	3	Negative	-1.	(1.68,960000.) (17.89,1050000.) 5	6	
Steel rods	_		Positive	800,000.	(-502) (-251.) (0.0.) (-502) (0.0)	(-50.,-2.) (0.,0.) (112.,53250000	
	2	4	Negative	-1.	(1.68,800000.) (17.89,875000.) 7	8	
9 (WSH4)		<u></u>	Positive	907,200.	(-50.,-2.) (-25.,-1.) (0.,0.)	(-50.,-2.) (0.,0.) (36.,22680000.	
Cables	3	5	Negative	-1.	(1,46,907200.) (3.64,1145000.) 9	10	
		_	Positive	960,000.	(-50.,-2.) (-25.,-1.) (0.,0.)	(-50.,-2.) (0.,0.) (174.,63900000	
10 (WSH5)	2	6	Negative	-1.	(2.61,960000.) (27.86,1090000.) 11	12	
Steel rods		_	Positive	640,000.	(-50.,-2.) (-25.,-1.) (0.,0.)	(-50.,-2.) (0.,0.) (174.,42600000	
	2	7	Negative	-1.	13	14	
LL OWSHID			Positive	907200.	(-50.,-2.) (-25.,-1.) (0.,0.)	(-50.,-2.) (0.,0.) (36.,22680000.	
Cables	4	8	Negative	-1.	- (1.46,907200.) (3.64,1145000.) 15	16	
12 (WSH7)		-	Positive	907200.	(-50.,-2.) (-25.,-1.) (0.,0.) (1.46,907200.) (3.64,1145000.) 17	- (-50,-2) (-25,-1) (0,0) (1.46,907200) (3.64,1145000.) 17 (-50,-2.) (0,0.	(-50.,-2.) (0.,0.) (36.,22680000
Cables	4	9	Negative	-1.			18
13 (WSHR)	4		Positive	640,000.	(-502.) (-25.,-1.) (0.,0.)	(-50.,-2.) (0.,0.) (122.,42600000	
Steel rods		4	4 10	Negative	-1.	- (1.84,640000.) (19.58,700000.) 19	20
















































1	1	r	T	
Area	ξ	ξ η		
1	-0.535714	-0.535714 -0.820513		
2	-0.178571	-0.967949	121.3191	
3	0.178571	-0.967949	121.3191	
4	0.535714	-0.820513	126.2233	
5	0.821429	-0.544872	88,3159	
6	0.964286	-0.192308	65.1066	
7	0.964286	0.192308	65.1066	
8	0.821429	0.544872	88.3159	
9	0.535714	0.820513	126.2233	
10	0.178571	0.967949	121.3191	
11	-0.178571	0.967949	121.3191	
12	-0.535714	0.820513	126.2233	
13	-0.821429	0.544872	88.3159	
14	-0.964286	0.192308	65.1066	
15	-0.964286	-0.192308	65.1066	
16	-0.821429	-0.544872	88.3159	
17	-0.500000	-0.628205	447.0000	
18	-0.166667	-0.701923	583.5000	
19	0.166667	-0.701923	583.5000	
20	0.500000	-0.628205	447.0000	
21	-0.500000	0.628205	447.0000	
22	-0.166667	0.701923	583.5000	
23	0.166667	0.701923	583.5000	
24	0.500000	0.628205	447.0000	
25	-0.720238	-0.435897	255.0000	
26	0.720238	-0.435897	255.0000	
27	-0.791667	-0,150641	350,5000	
28	0.791667	-0.150641	350.5000	
29	-0.791667	0.150641	350.5000	
30	0.791667	0.150641	350.5000	
31	-0.720238	0.435897	255.0000	
32	0.720238	0.435897	255.0000	
33	-0.309524	-0.217949	884.0000	
34	0.309524	-0.217949	884.0000	

Area	Ę	η	Weight
35	-0.309524	0.217949	884.0000
36	0.309524	0.217949	884.0000

Bent WS88

 $A_{rel} = 0.891625$ $f_{avg} = 0.9$ b = 168h = 78

Area	ξ η		Weight
1	-0.584416	-0.800000	127.4398
2	-0.194805	-0.962500	121.5030
3	0.194805	-0.962500	121.5030
4	0.584416	-0.800000	127.4398
5	0.863636	-0.512500	74.0907
6	0.974026	-0.175000	58.6777
7	0.974026	0.175000	58.6777
8	0.863636	0.512500	74.0907
9	0.584416	0.800000	127.4398
10	0.194805	0.962500	121.5030
11	-0.194805	0.962500	121.5030
12	-0.584416	0.800000	127.4398
13	-0.863636	0.512500	74.0907
14	-0.974026	0.175000	58.6777
15	-0.974026	-0.175000	58.6777
16	-0.863636	-0.512500	74.0907
17	-0.545455	-0.612500	450.0000
18	-0.181818	-0.693750	605.0000
19	0.181818	-0.693750	605.0000
20	0.545455 -0.612500		450.0000
21	-0.545455 0.612500		450.0000
22	-0.181818	0.693750	605.0000
23	0.181818	0.693750	605.0000
24	0.545455	0.612500	450.0000
25	-0.7 6948 1	-0.415625	206.2500
26	0.769481	-0.415625	206.2500
27	-0.824675	-0.140625	264.2500
28	0.824675	-0.140625	264.2500
29	-0.824675	0.140625	264.2500
30	0.824675 0.140625		264.2500
31	-0.769481	0.415625	206.2500
32	0.769481	0.415625	206.2500
33	33 -0.506494		221.0000
34	-0.168831	-0.318750 221.0000	
35	0.168831	-0.318750	221.0000
14	0 506494	-0 318750	221.0000

Area	Ę	η	Weight]
37	-0.506494	-0.106250	221.0000	
38	-0.168831	-0.106250	221.0000	1
39	0.168831	-0.106250	221.0000	
40	0.506494	-0.106250	221.0000	1
41	-0.506494	0.106250	221.0000	
42	-0.168831	0.106250	221.0000	
43	0.168831	0.106250	221.0000	
44	0.506494	0.106250	221.0000	
45	-0.506494	0.318750	221.0000	$A_{rel} = 0.906237$
46	-0.168831	0.318750	221.0000	$f_{avg} = 0.9$
47	0.168831	0.318750	221.0000] b=154
48	0.506494	0.318750	221.0000	h=80

Bents WS83, WS84, WS87, WS93, WS96, WS97, WS98 ES2, ES8, ES9, ES10, ES11, ES12